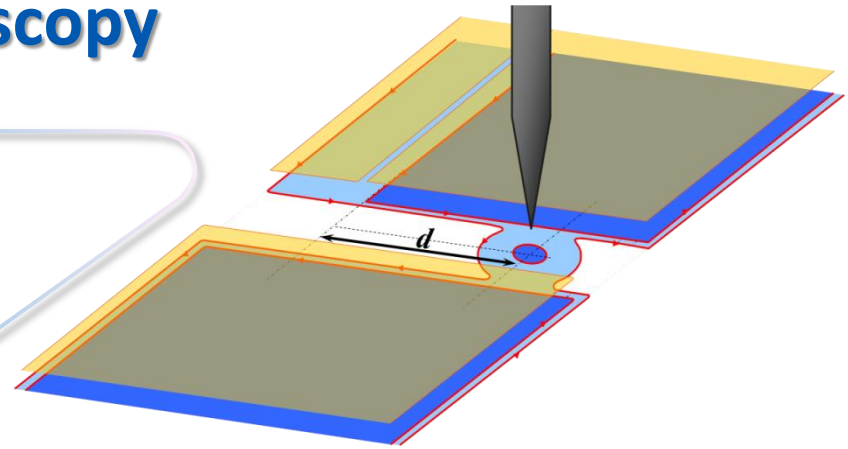


Exploring the physics of one-dimensional systems by scanning gate microscopy



Stefan Heun

*NEST, Istituto Nanoscienze-CNR and
Scuola Normale Superiore, Pisa, Italy*

NEST, Pisa, Italy:

Experiment:

Nicola Paradiso

Andrea Iagallo

Stefano Roddaro

Lucia Sorba

Fabio Beltram

Theory:

Davide Venturelli

Fabio Taddei

Vittorio Giovannetti

Rosario Fazio

Samples from:

Laboratorio TASC, Trieste, Italy:

Giorgio Biasiol

Princeton University, USA:

Loren N. Pfeiffer

Ken W. West

ETH Zurich, Switzerland:

Christian Reichl

Werner Wegscheider

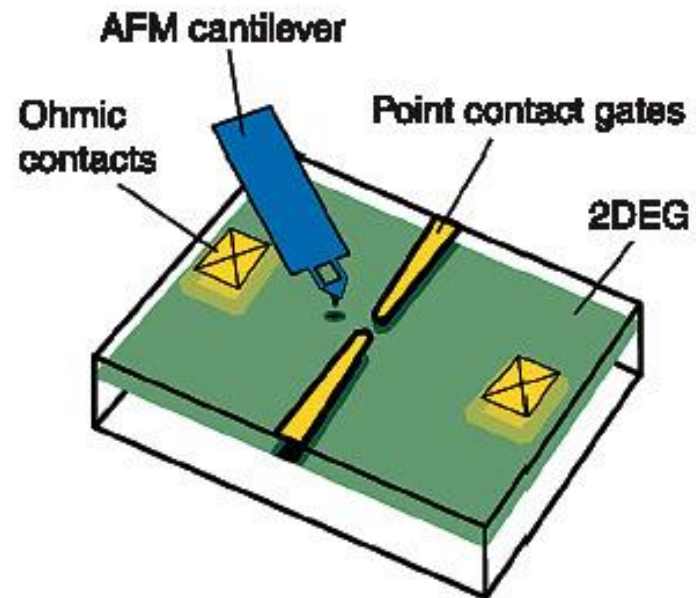


- **Basics of Scanning Gate Microscopy (SGM)**
- **Quantum Point Contact w/o magnetic field**
- **QPC in the quantum Hall regime**
- **Edge channel equilibration**

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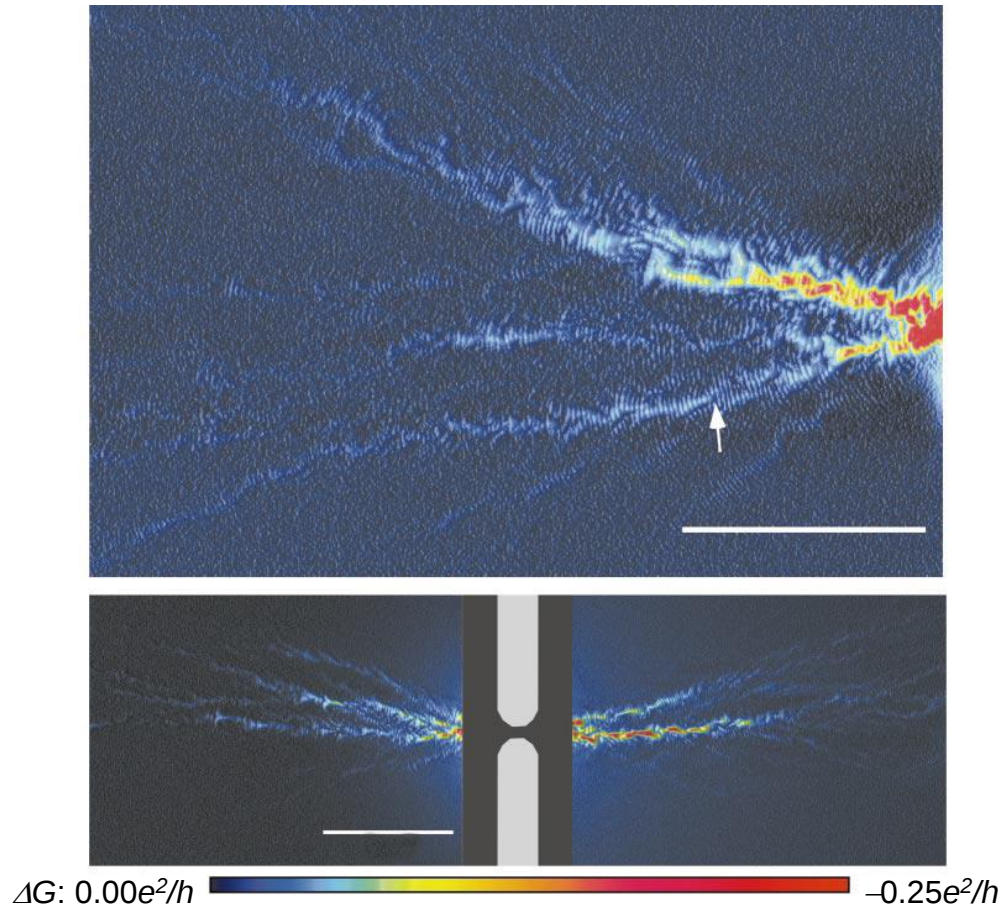
Scanning Gate Microscopy

- AFM with conductive tip
- Tip at negative bias (local gate - locally depletes the 2DEG), no current flows
- SGM performed in constant height mode (10-50 nm above surface), no strain



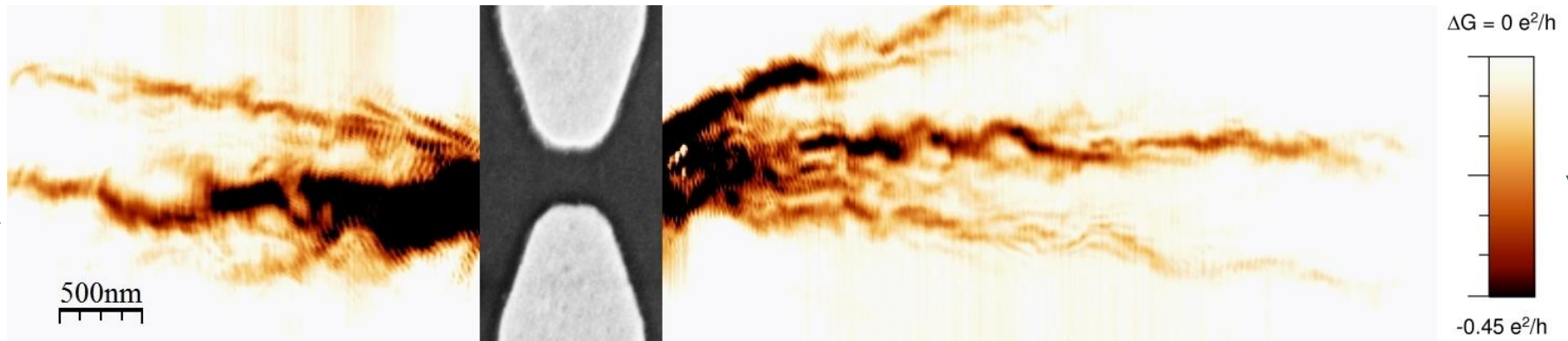
M. A. Topinka et al.:
Science **289** (2000) 2323.

Coherent branched flow of electrons



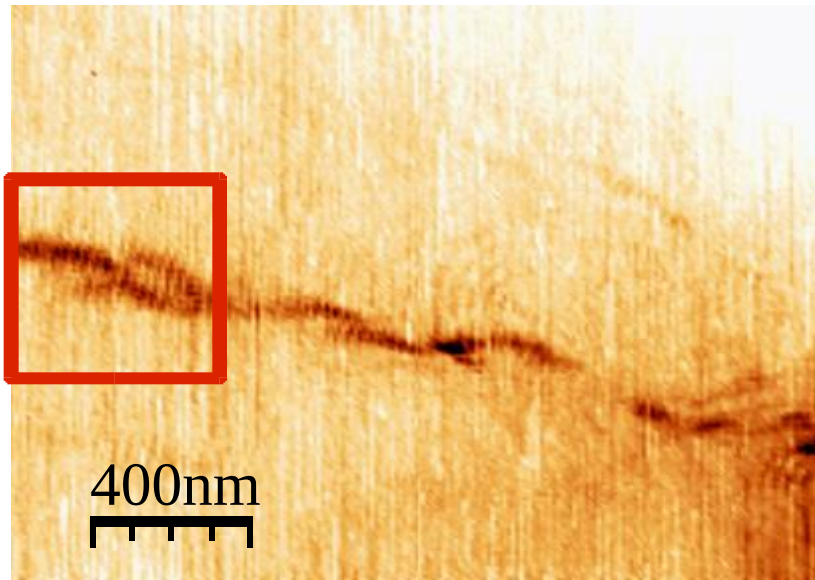
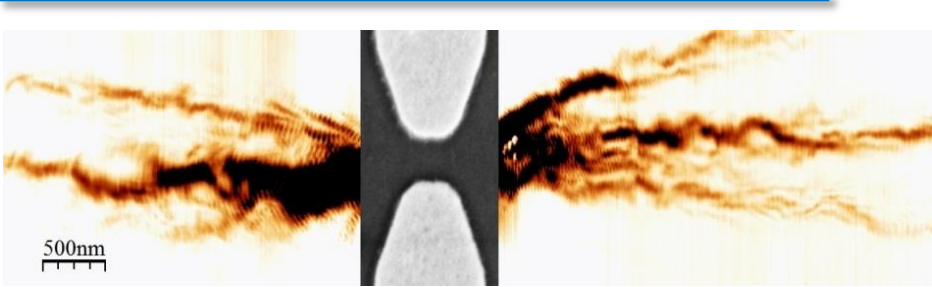
M. A. Topinka et al., Nature 410 (2001) 183.

Branched flow of electrons

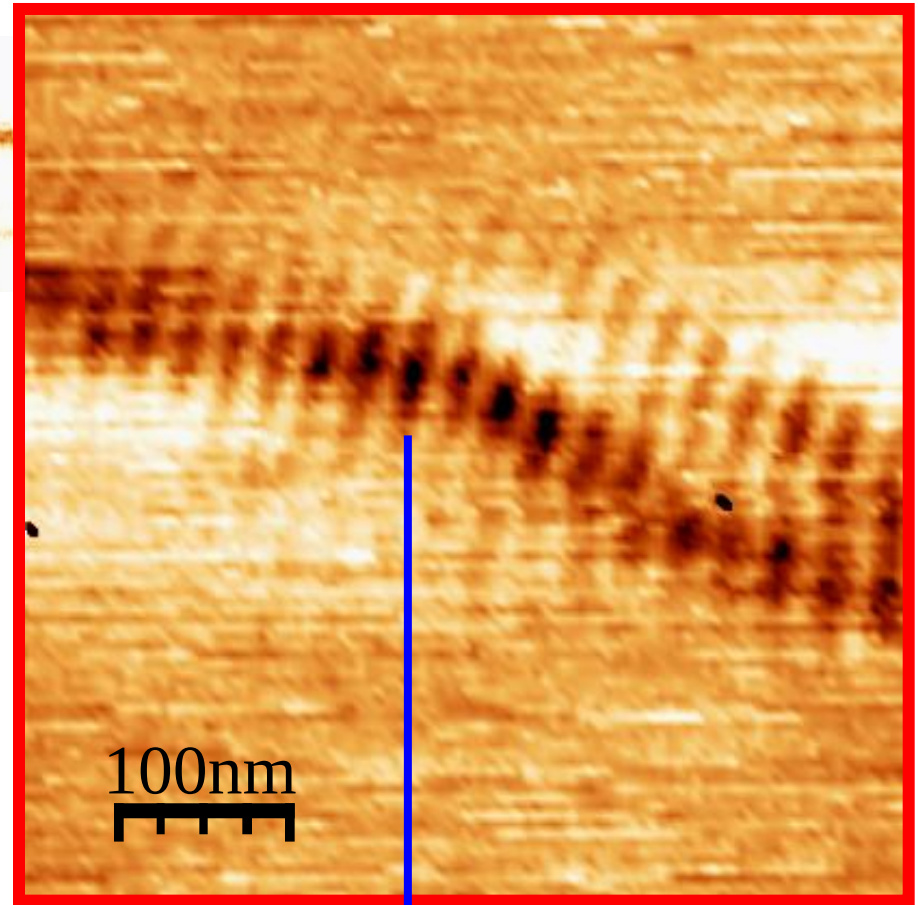


- No magnetic field ($B = 0$)
- QPC conductance $G = 6 e^2/h$ (3rd plateau)
- Tip voltage $V_{\text{tip}} = -5$ V, height $h_{\text{tip}} = 10$ nm
- see also M. A. Topinka et al., Nature **410** (2001) 183.

Appendix: branched flow and interference fringes



- QPC conductance $G = 6 e^2/h$ (3rd plateau)
- Tip voltage $V_{\text{tip}} = -5$ V, height $h_{\text{tip}} = 10$ nm
- see also M. A. Topinka et al., *Nature* **410** (2001) 183.



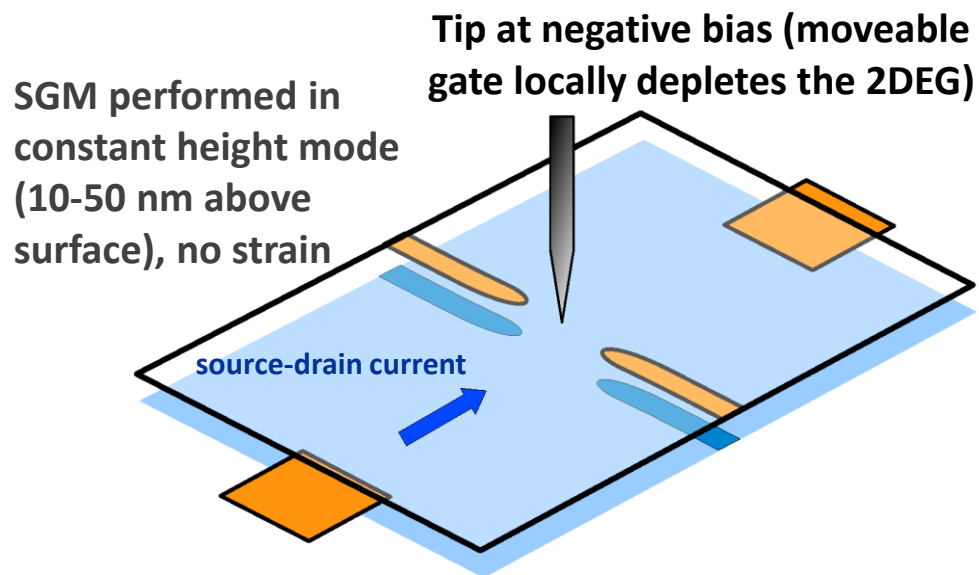
Fringe periodicity: $\lambda_F/2 = 20$ nm

N. Paradiso et al., *Physica E* **42** (2010) 1038.

The SGM @NEST lab in Pisa

Setup:

- AFM non-optical detection scheme (tuning fork)
- With vibration and noise isolation system
- ^3He insert (cold finger base temp. :300 mK)
- 9 T cryomagnet



Pioneering work by:

M. A. Topinka et al.: Science **289** (2000) 2323.

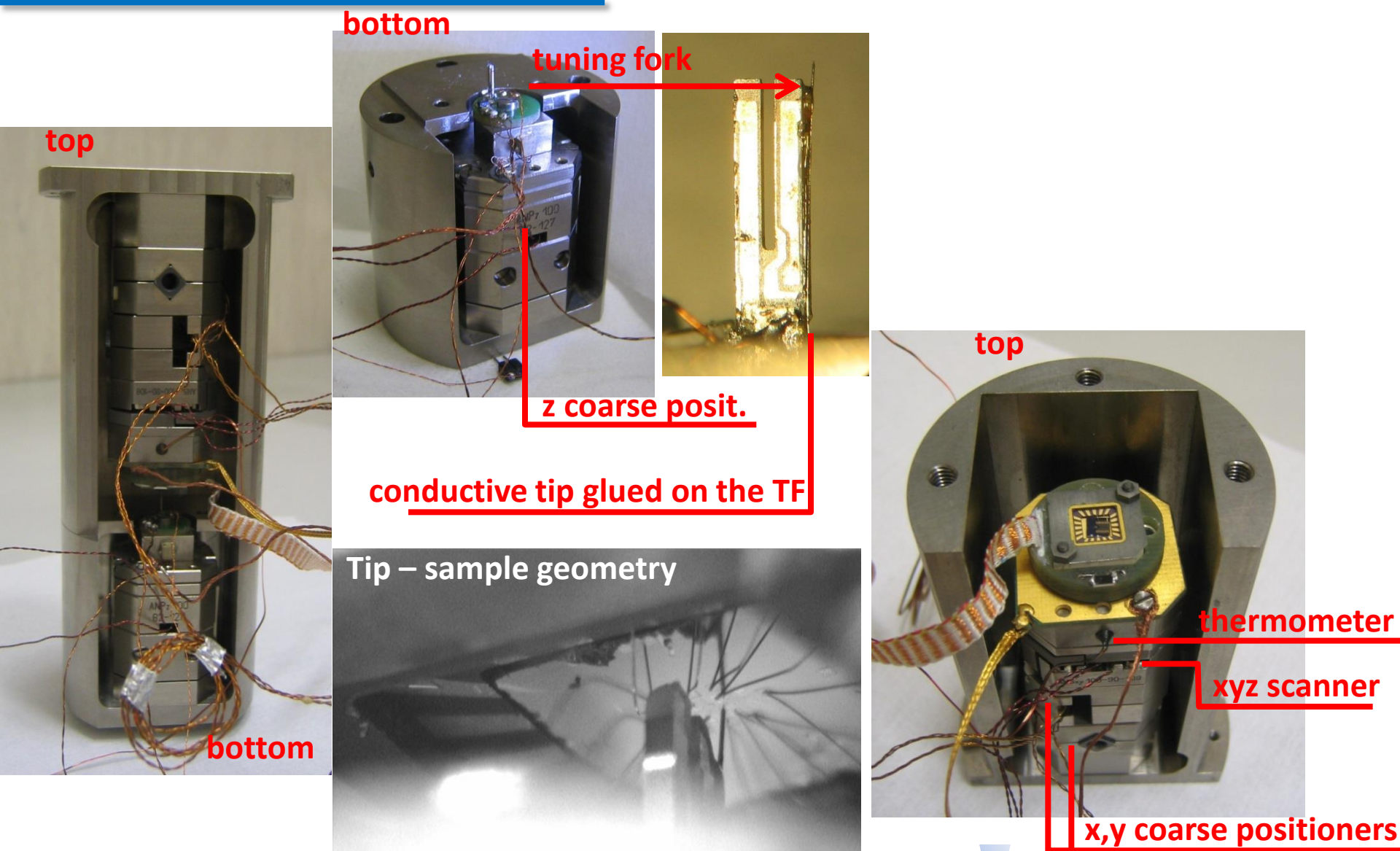
 **attocube systems**
explore your nanoworld

SGM Group

National Enterprise for nanoScience and nanoTechnology

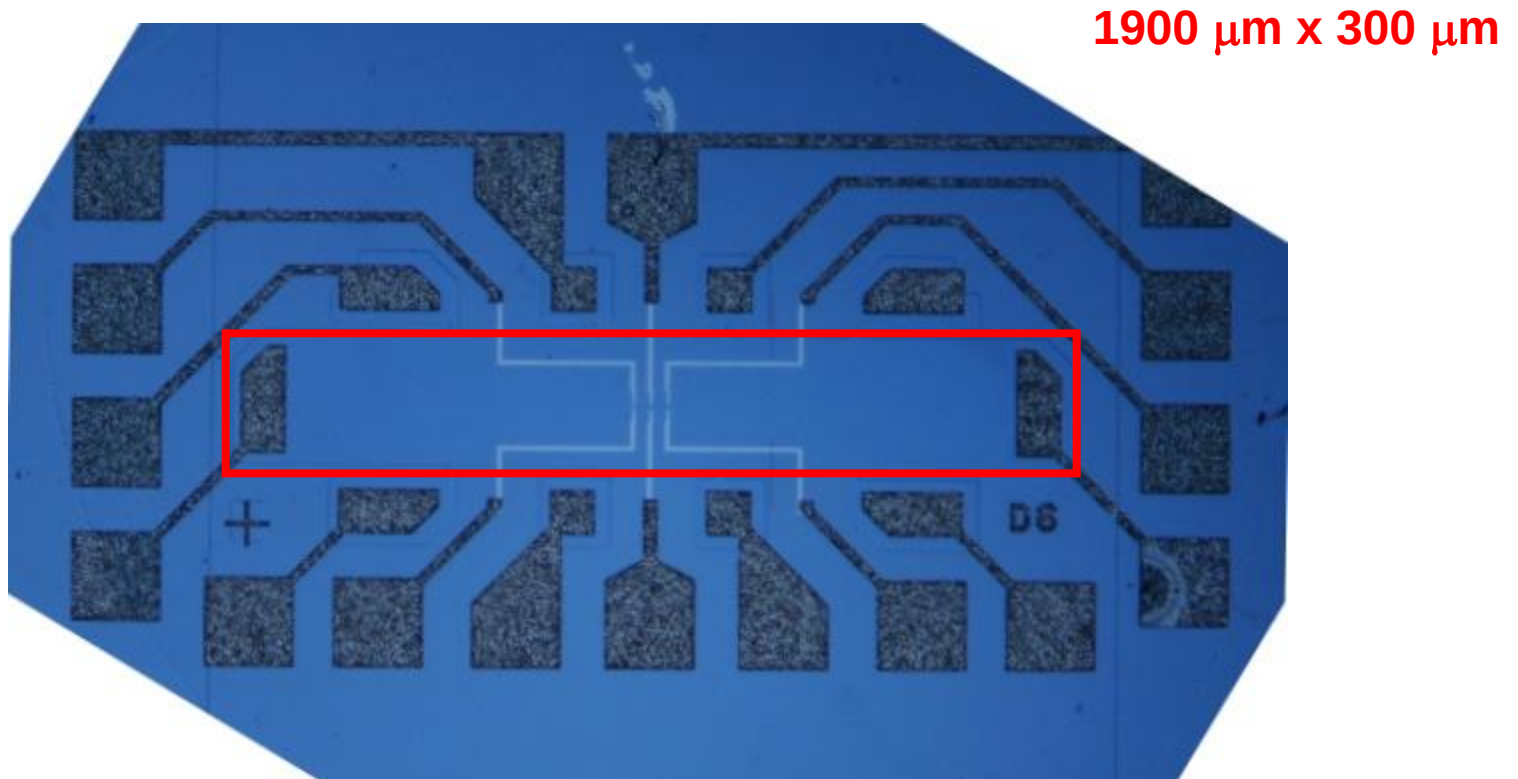
NEST

Tuning fork and sample holder

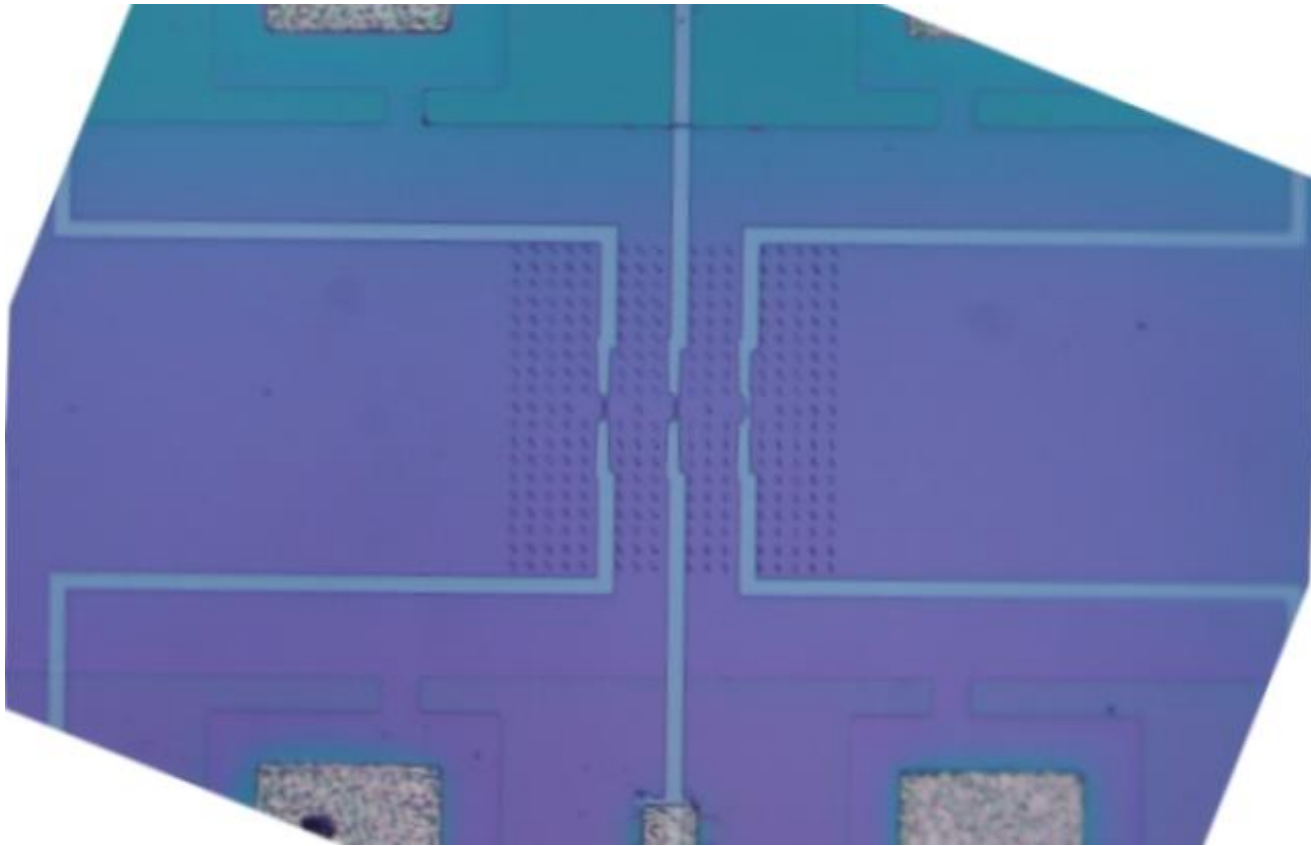


- Basics of Scanning Gate Microscopy (SGM)
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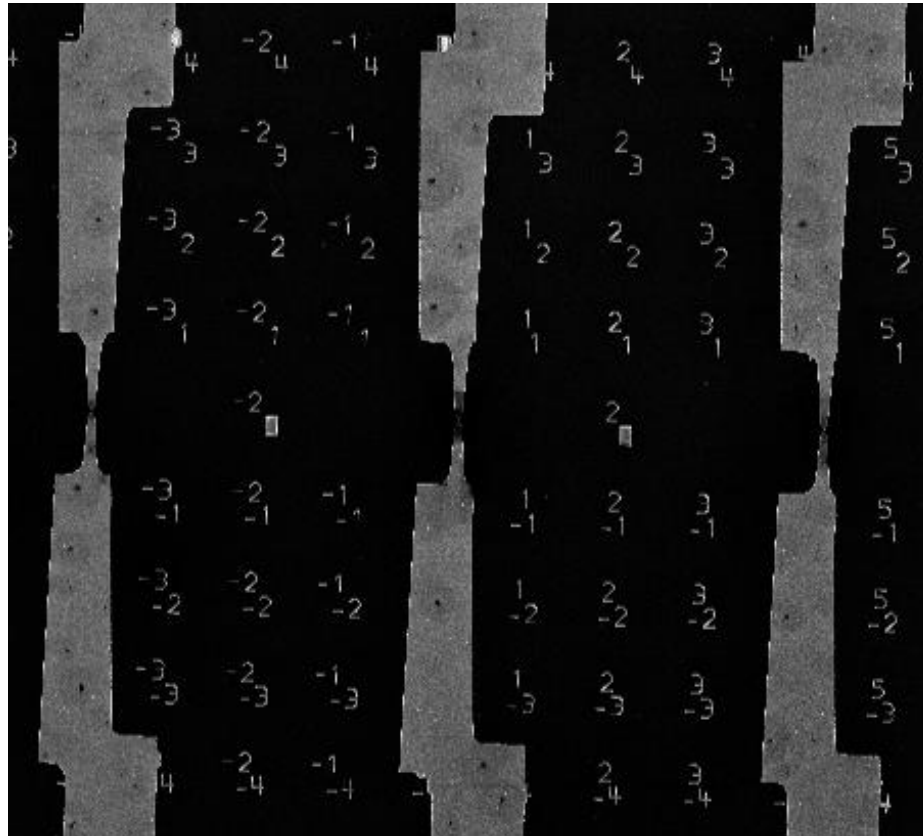
Hall-bar samples



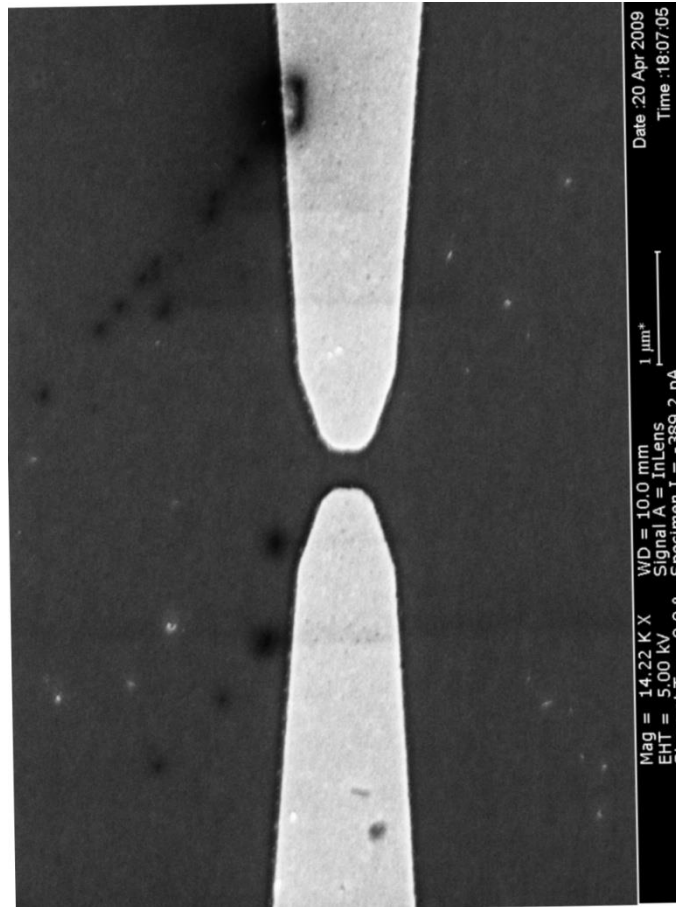
Hall-bar samples



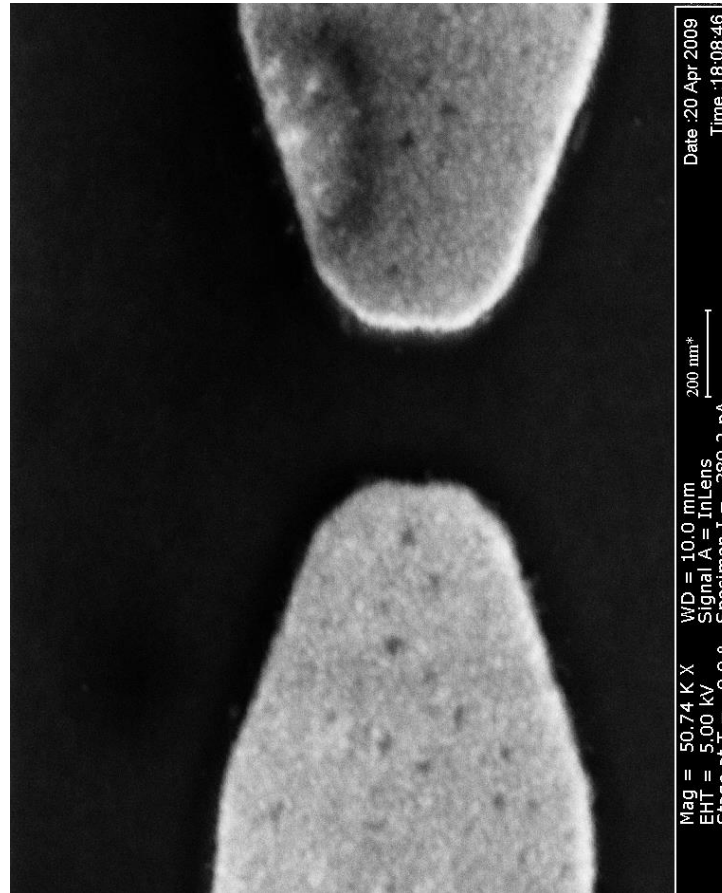
Hall-bar samples



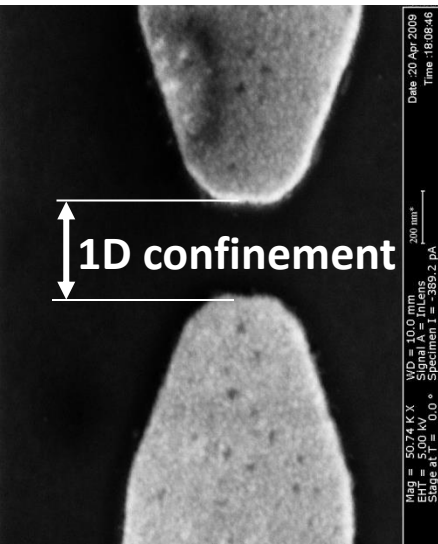
Hall-bar samples



Hall-bar samples

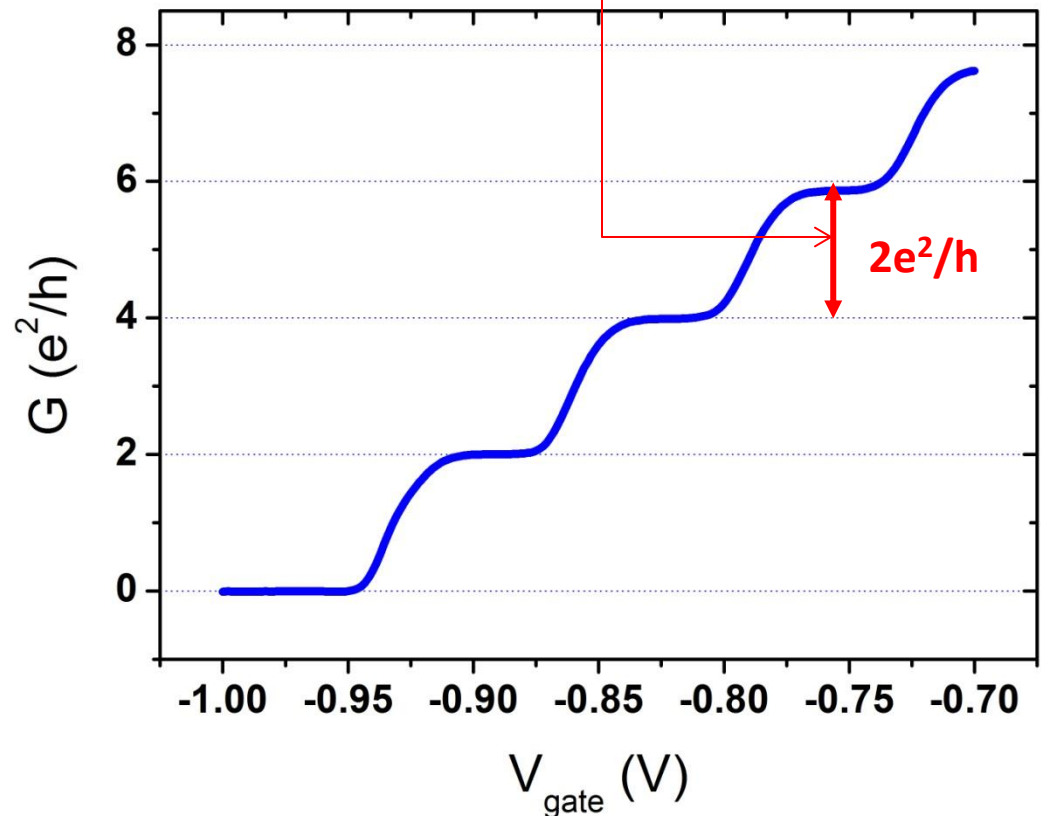


Conductance quantization in QPCs



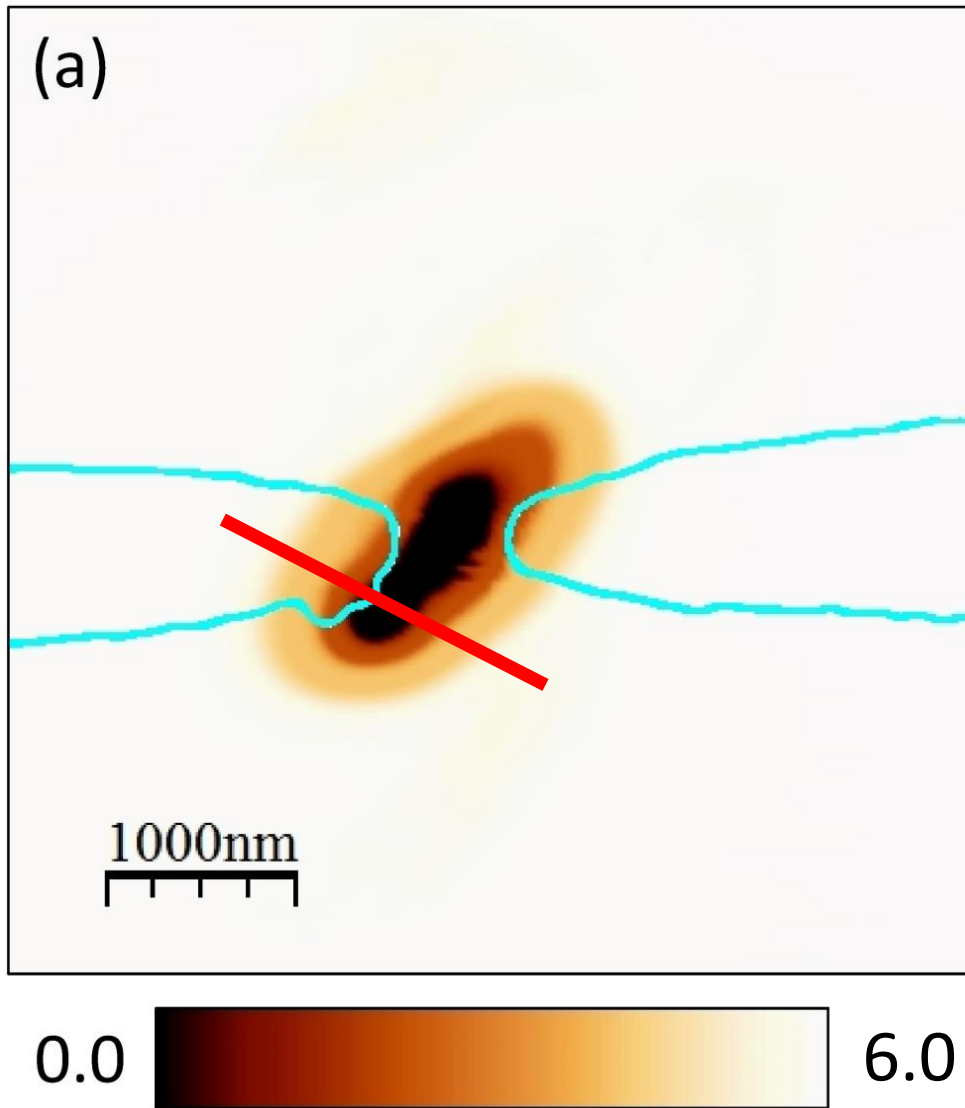
In 1D systems the current is carried by a finite number of modes (arising from confined subbands) . Each mode contributes two quantum of conductance.

First we fix the mode number (QPC setpoint), then we start scanning the biased tip at a fixed height.

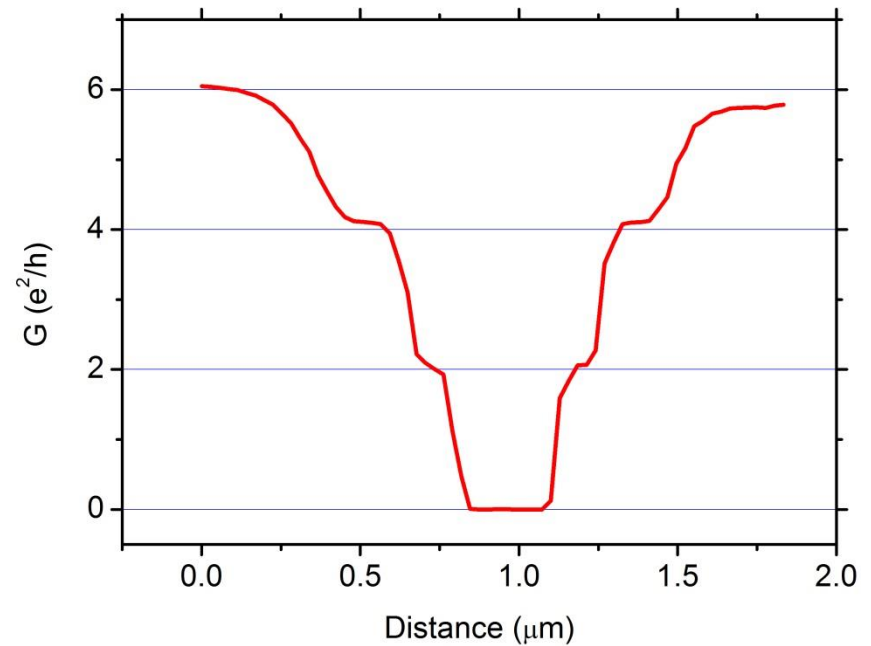
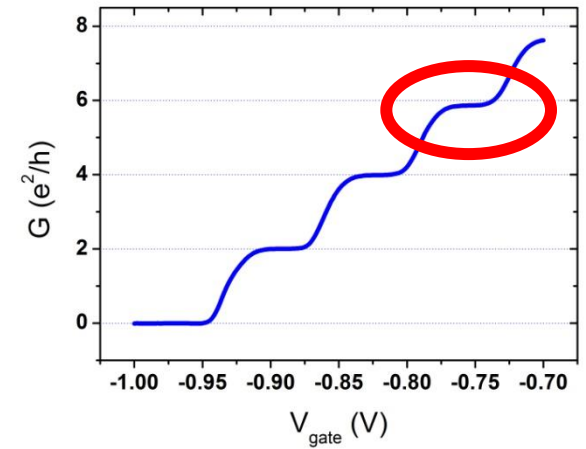


QPC at 3rd plateau

(a)

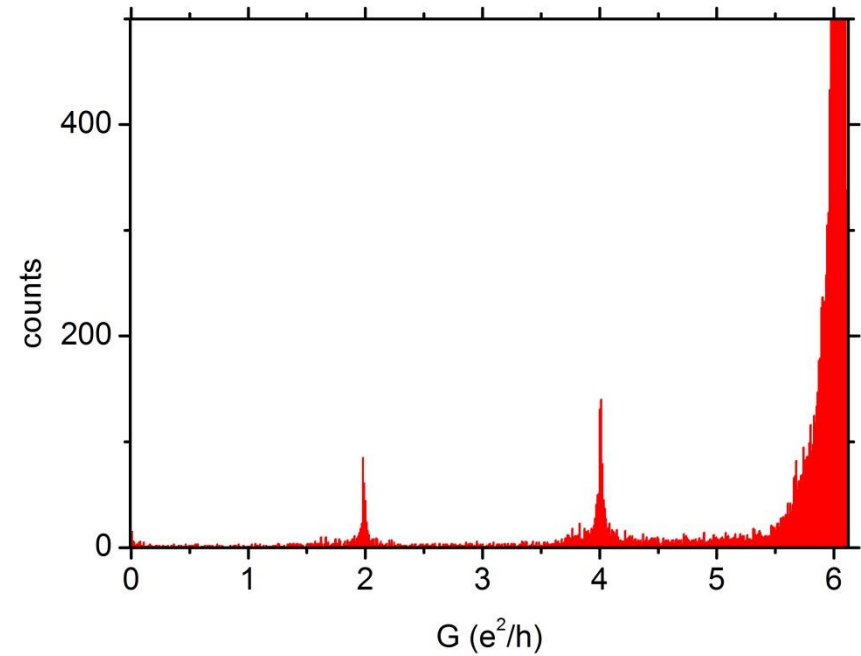
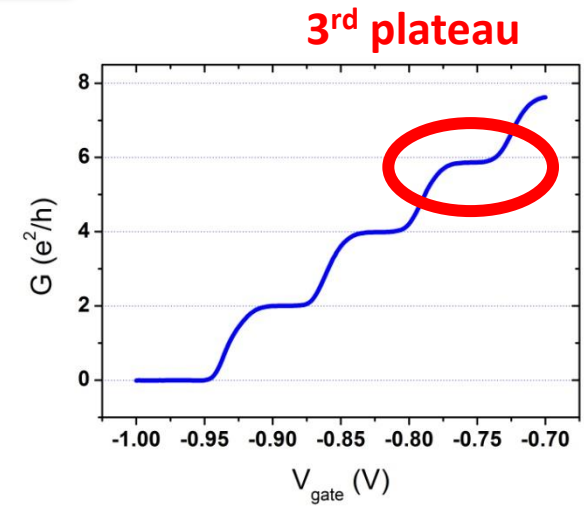
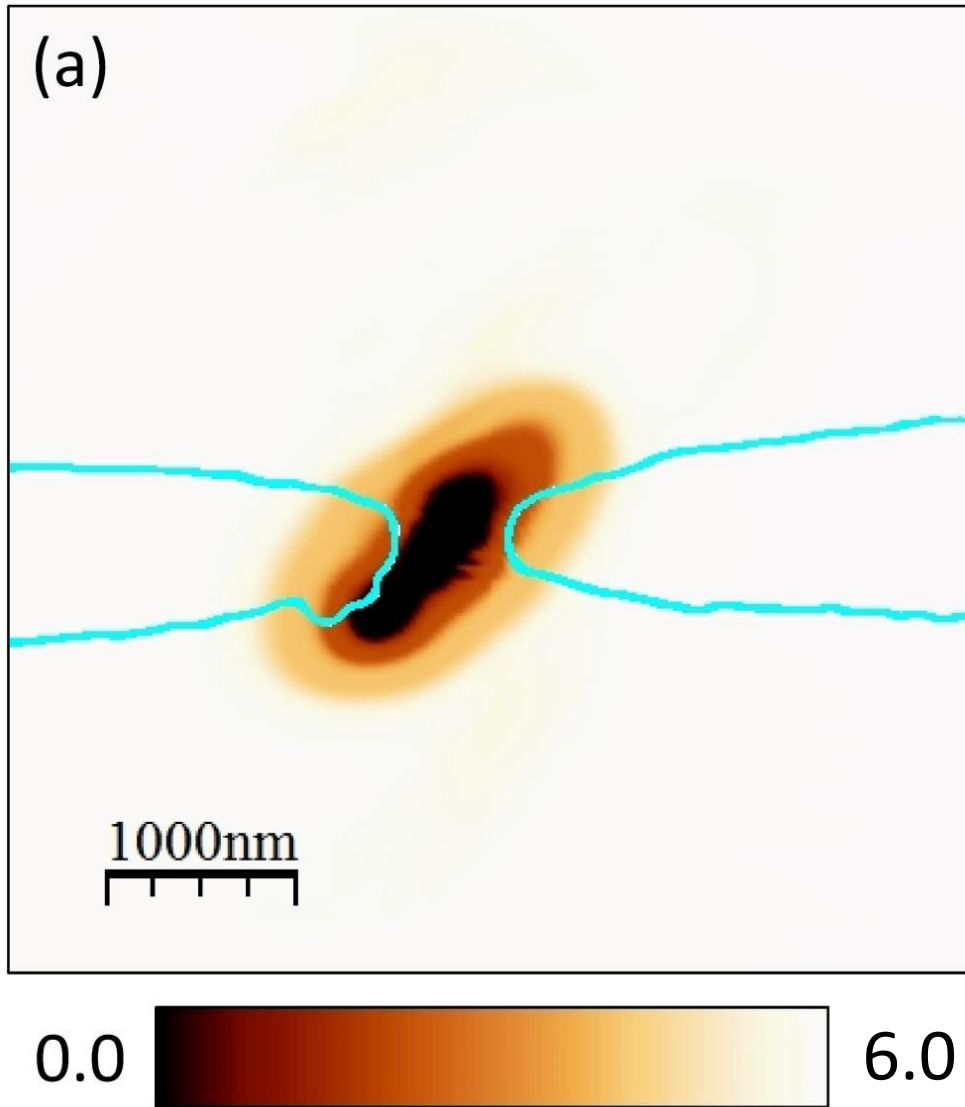


3rd plateau



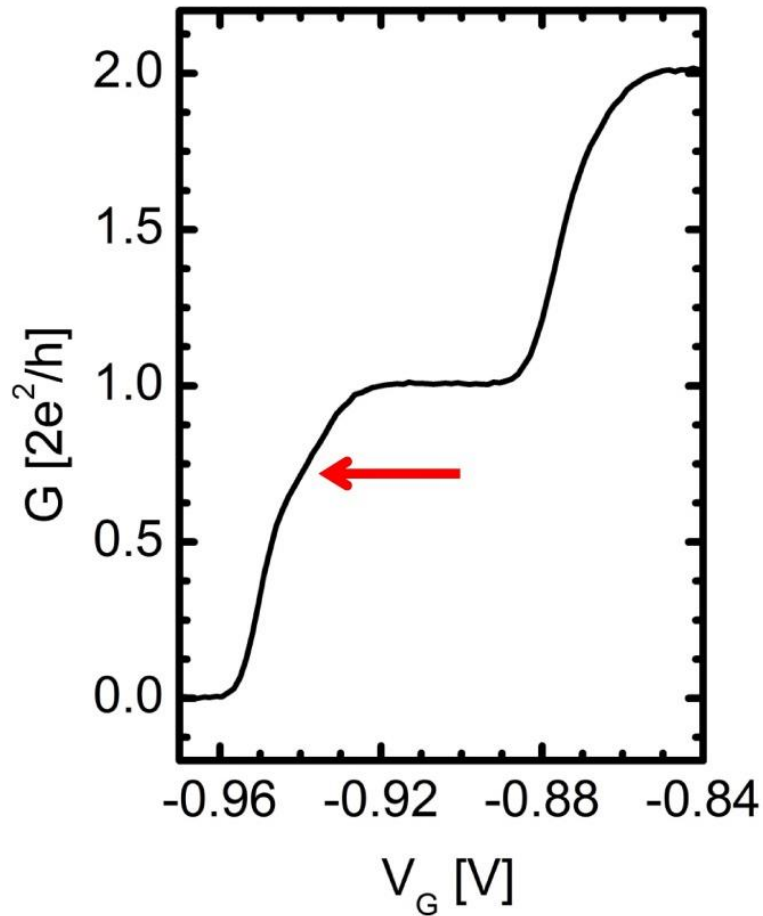
Histogram analysis

(a)



0.7 Anomaly

(b)



Origin still debated
Intrinsic or extrinsic?

- Quantum interference
- Spin polarization
- Kondo effect
- Wigner crystallization

A. Iqbal *et al.*, arXiv:1311.6303

0.7 Anomaly

LETTER

doi:10.1038/nature12421

Microscopic origin of the '0.7-anomaly' in quantum point contacts

Florian Bauer¹
Werner Wegscheider¹

LETTER

doi:10.1038/nature12491

Odd and even Kondo effects from emergent localization in quantum point contacts

M. J. Iqbal¹
Yigal Meir¹

Scanning gate control over conductance anomalies in a quantum point contact

B. Brun¹, F. Martins², S. Faniel², B. Hackens², A. Cavanna⁴, C. Ulysse⁴, A. Ouerghi⁴,
U. Gennser⁴, D. Mailly⁴, S. Huant¹, V. Bayot^{1,2}, M. Sanquer³ and H. Sellier^{1*}

¹*Institut Néel, CNRS et Université Joseph Fourier, 25 rue des Martyrs, F-38042 Grenoble, France*

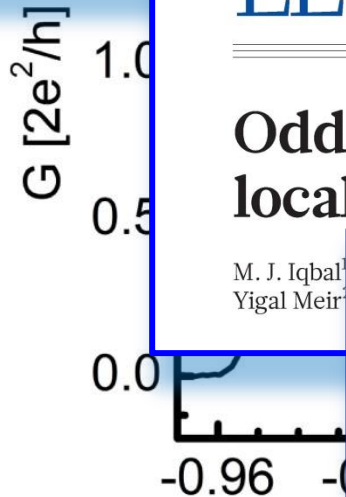
²*IMCN/NAPS, Université catholique de Louvain, B-1348 Louvain-la-Neuve, Belgium*

³*SPSMS, UMR-E CEA / UJF-Grenoble 1, INAC, 17 rue des Martyrs, F-38054 Grenoble, France*

⁴*Laboratoire de Photonique et de Nanostructures CNRS, Route de Nozay, F-91460 Marcoussis, France*

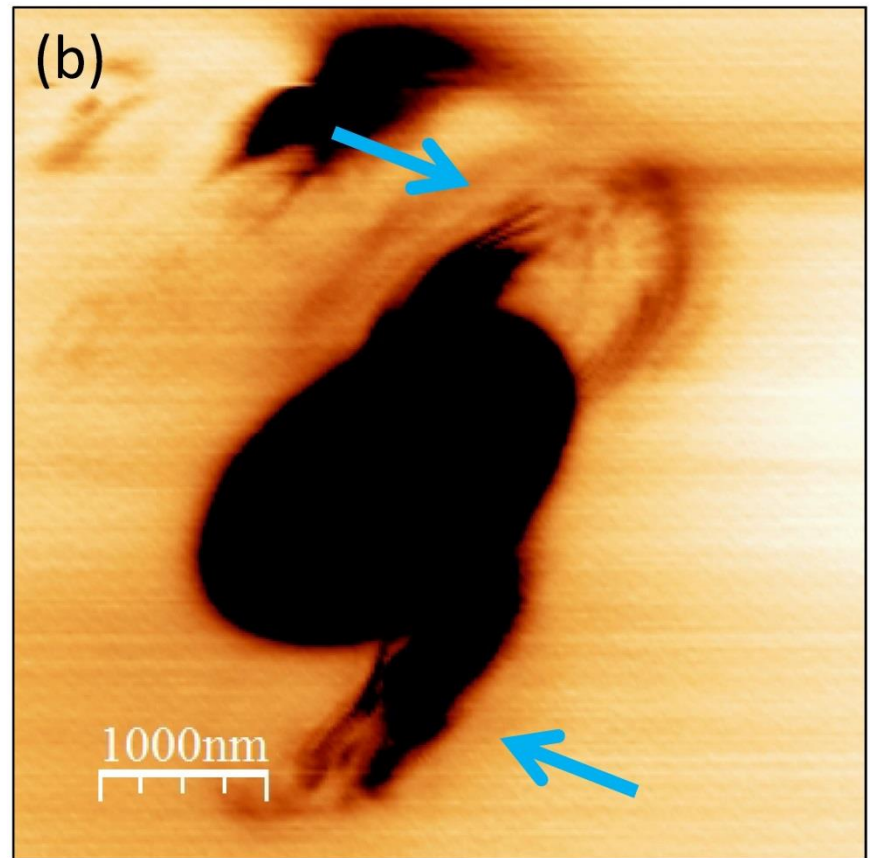
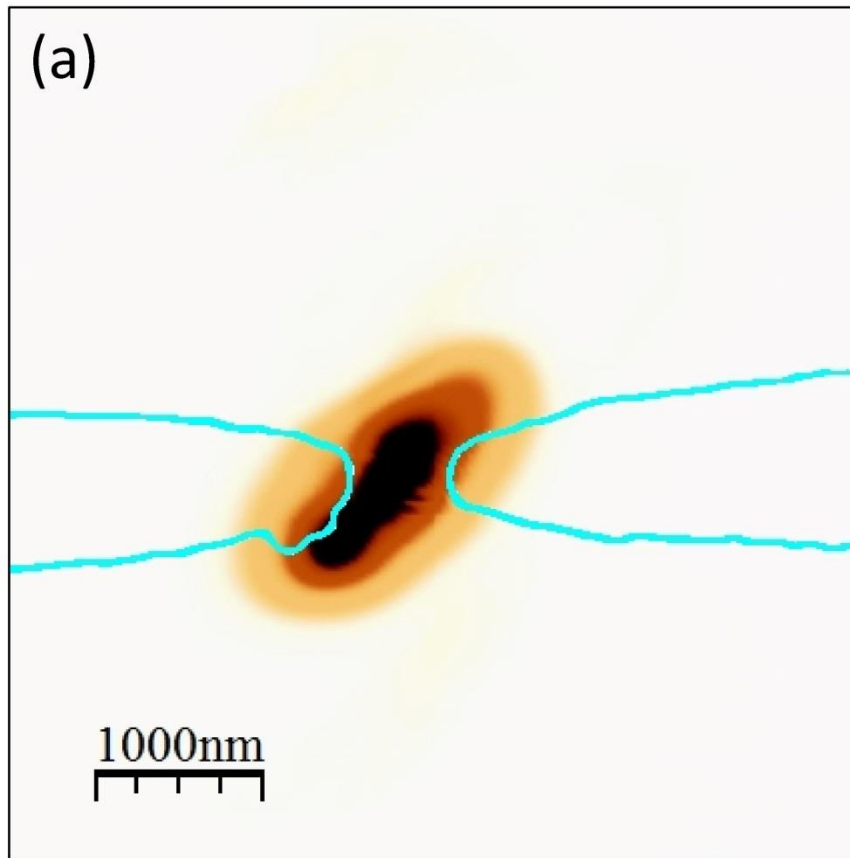
*Electronic address: hermann.sellier@grenoble.cnrs.fr

(Dated: August 1, 2013)



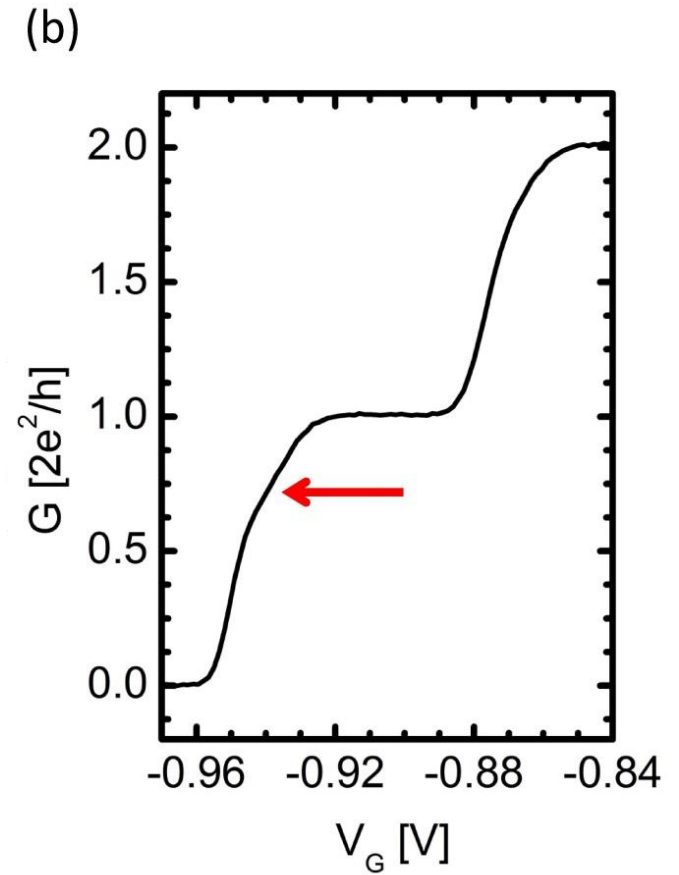
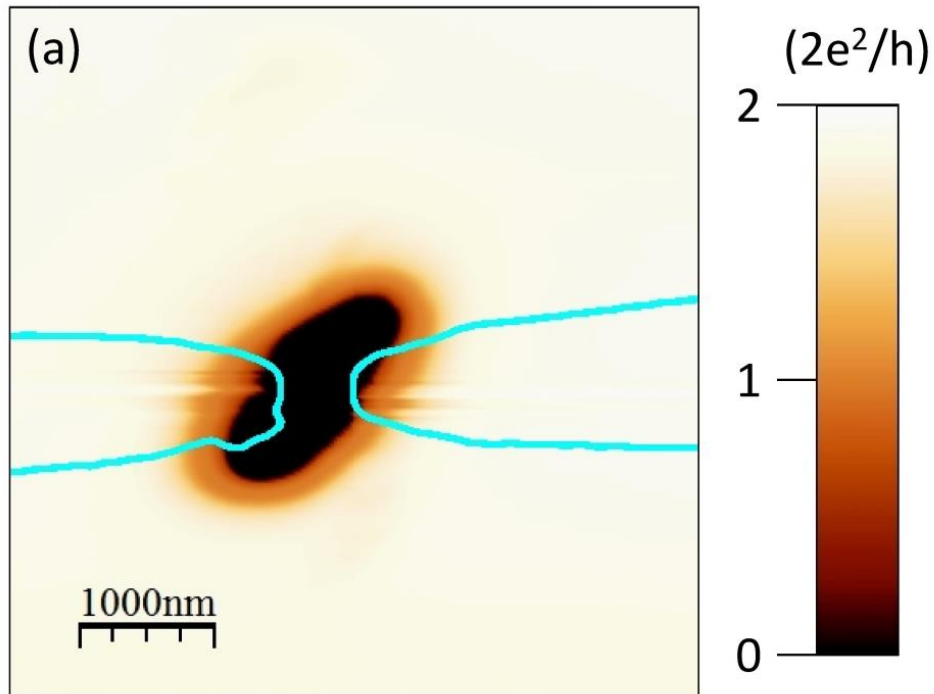
A. Iqbal et al., arXiv:1311.6303

Device A: QPC with localized impurities



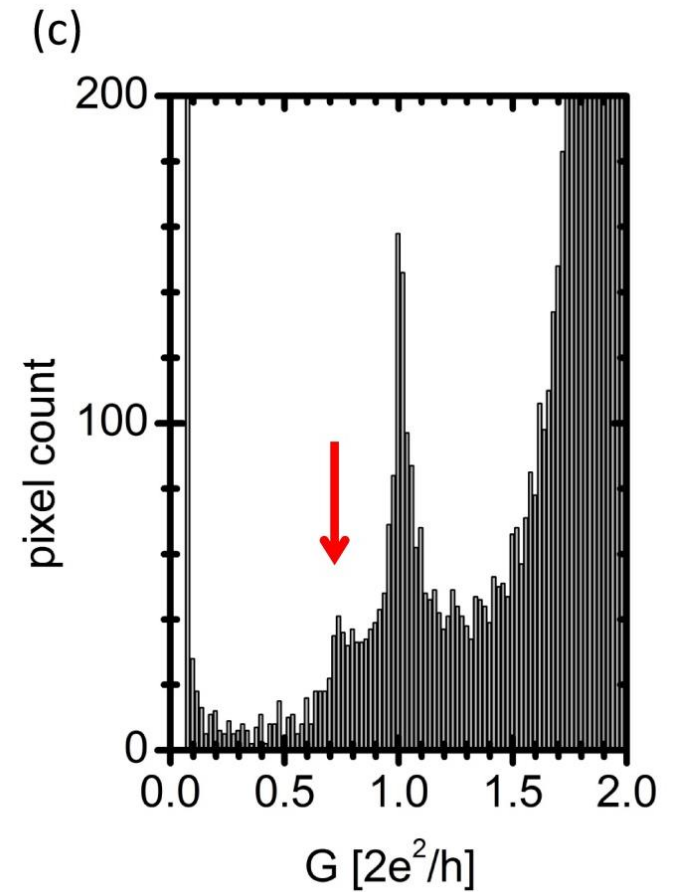
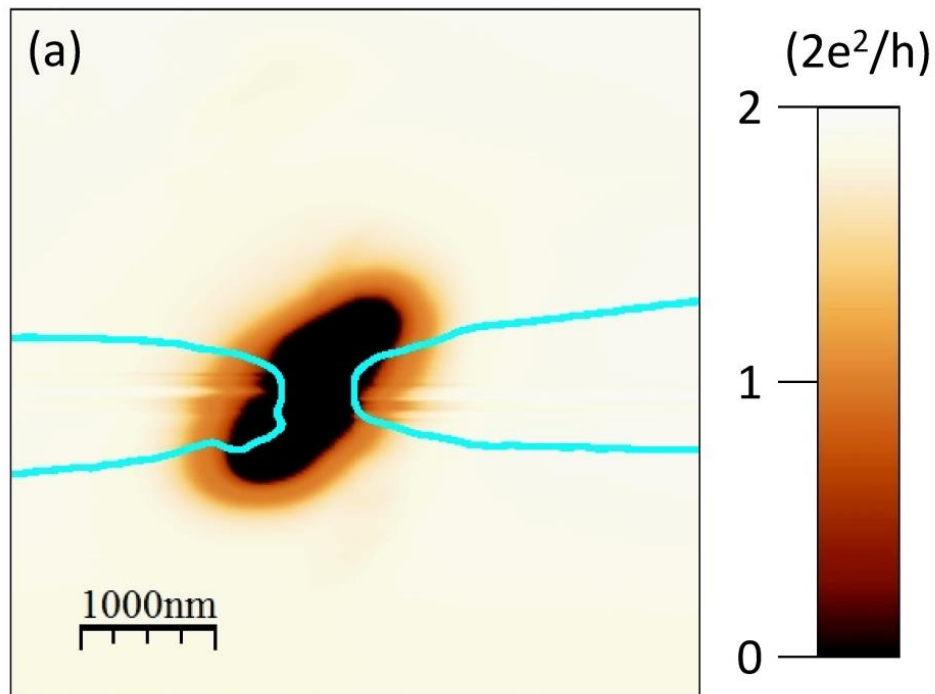
A. Iagallo *et al.*, arXiv:1311.6303

0.7 Anomaly in Device A



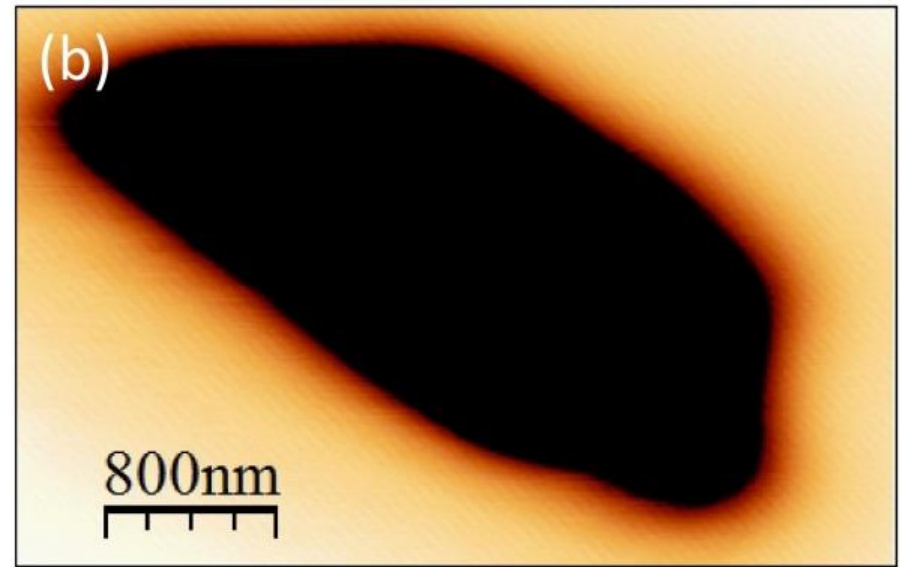
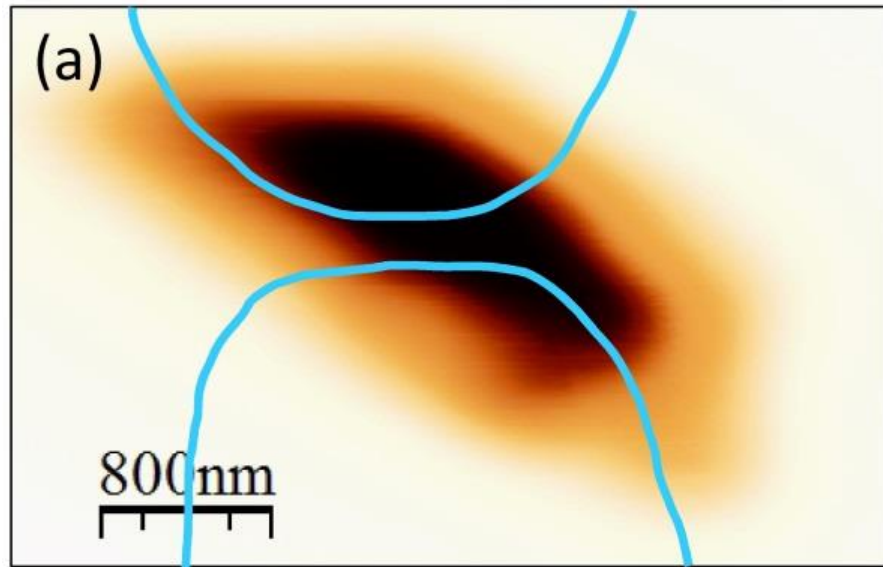
A. Iqbal *et al.*, arXiv:1311.6303

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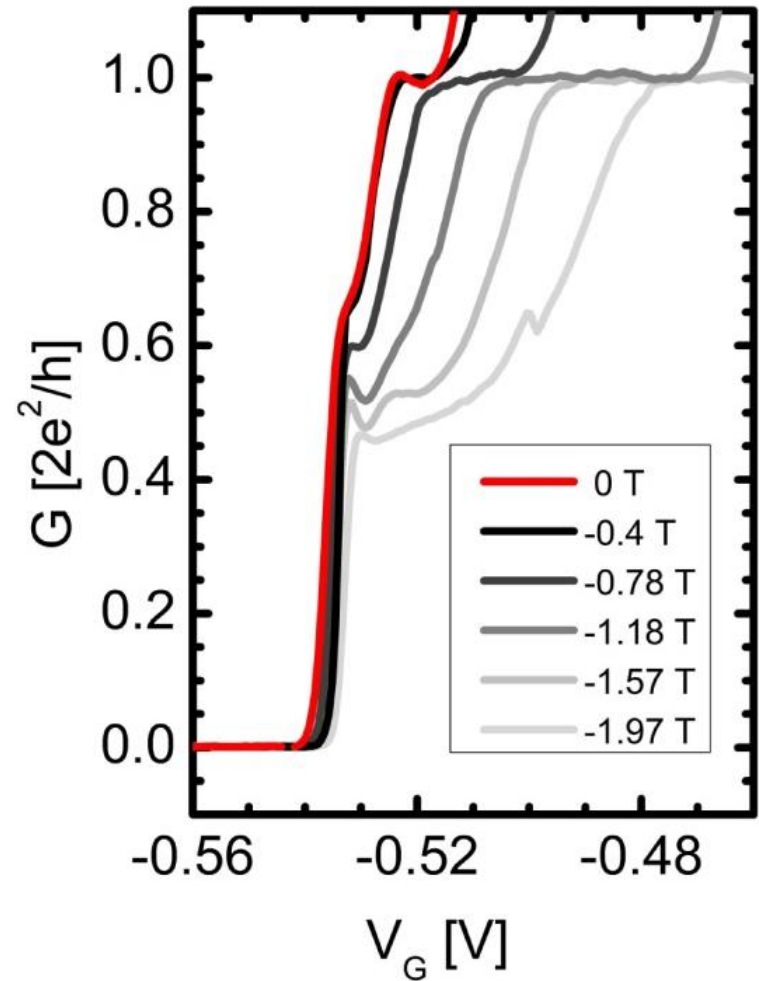
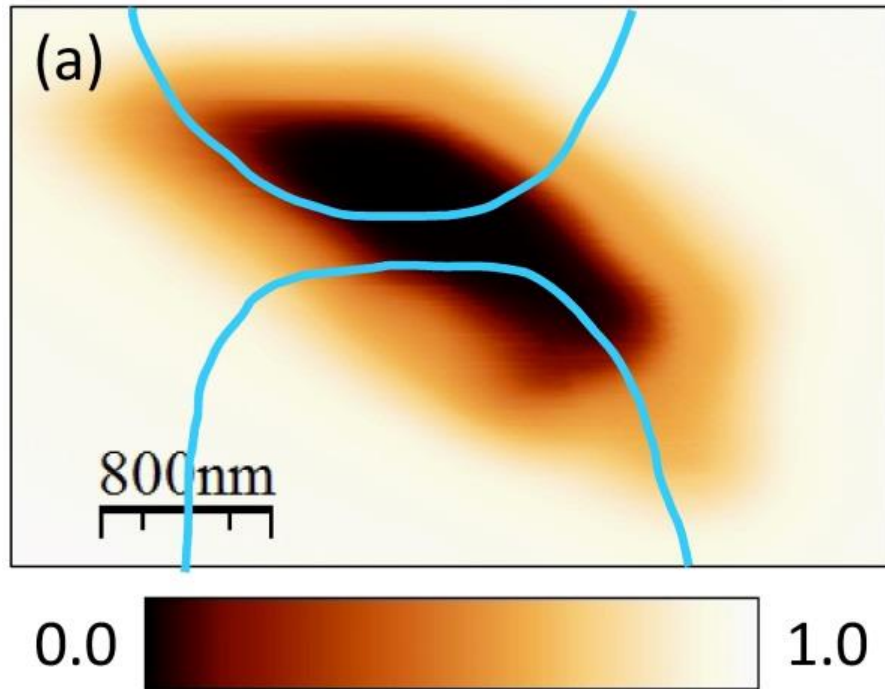
A. Iqbal *et al.*, arXiv:1311.6303

Device B: QPC without localized impurities



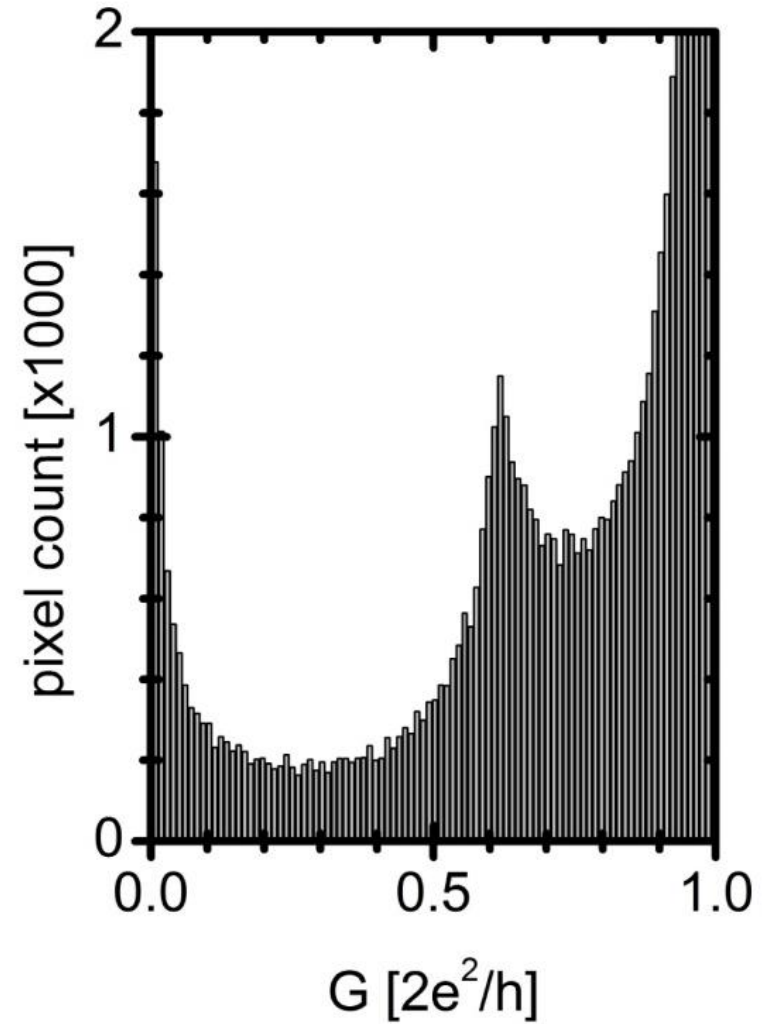
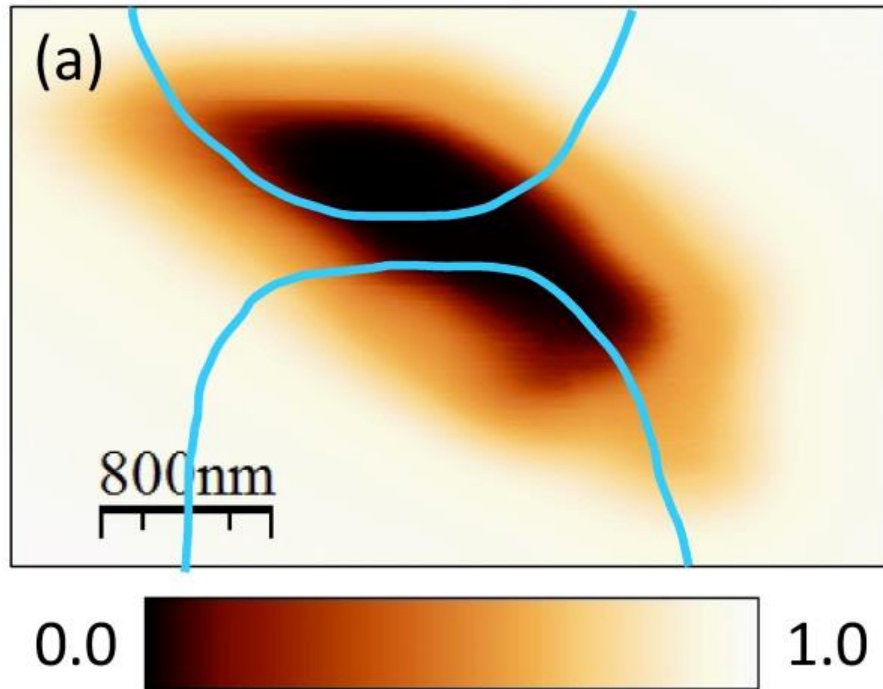
A. Iagallo *et al.*, arXiv:1311.6303

0.7 Anomaly in Device B



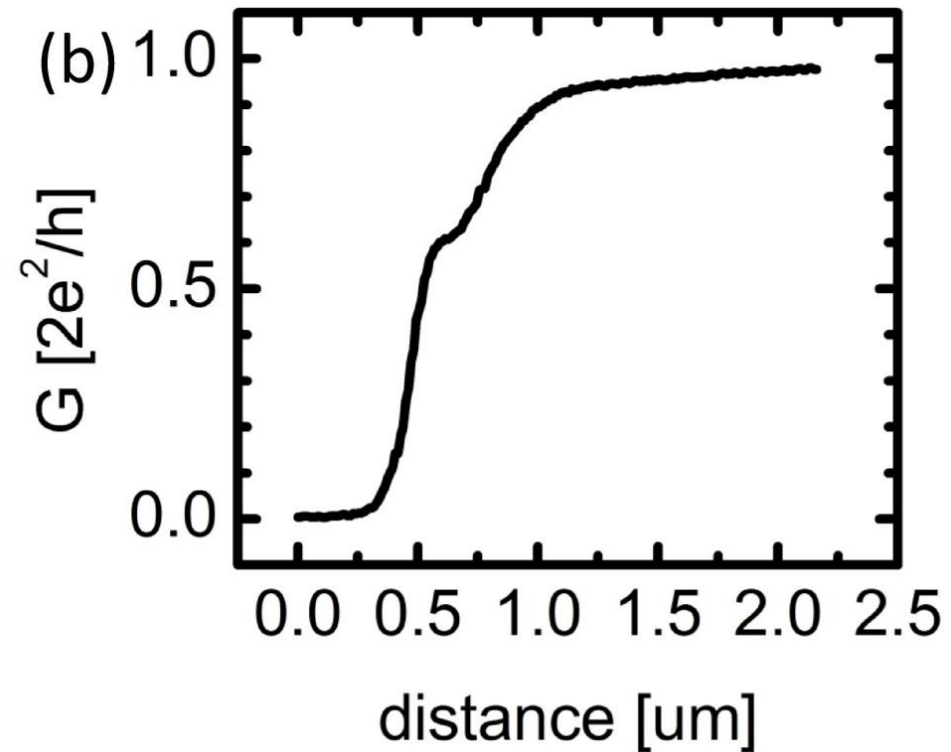
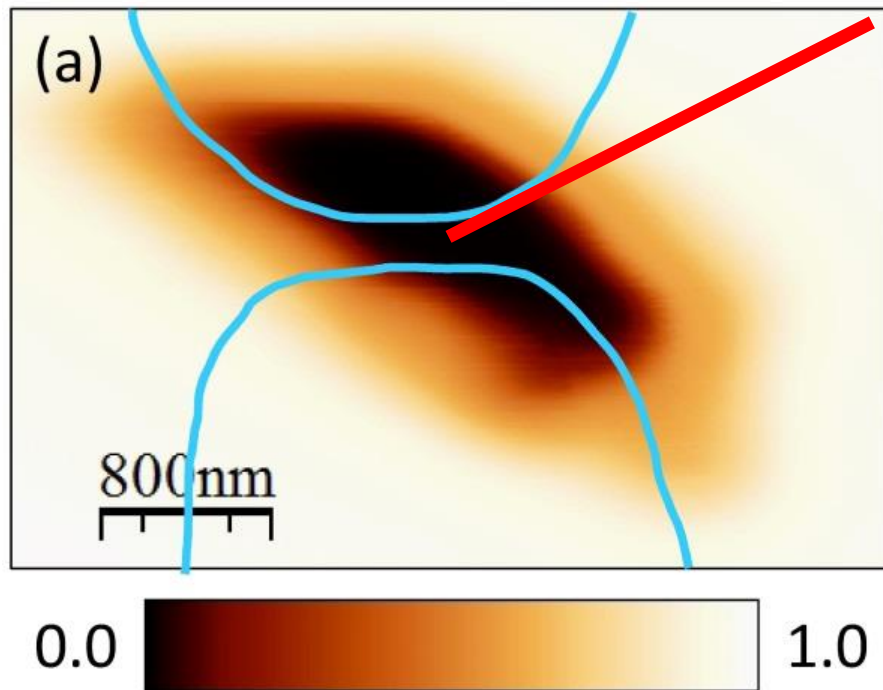
A. Iqbal *et al.*, arXiv:1311.6303

0.7 Anomaly in Device B



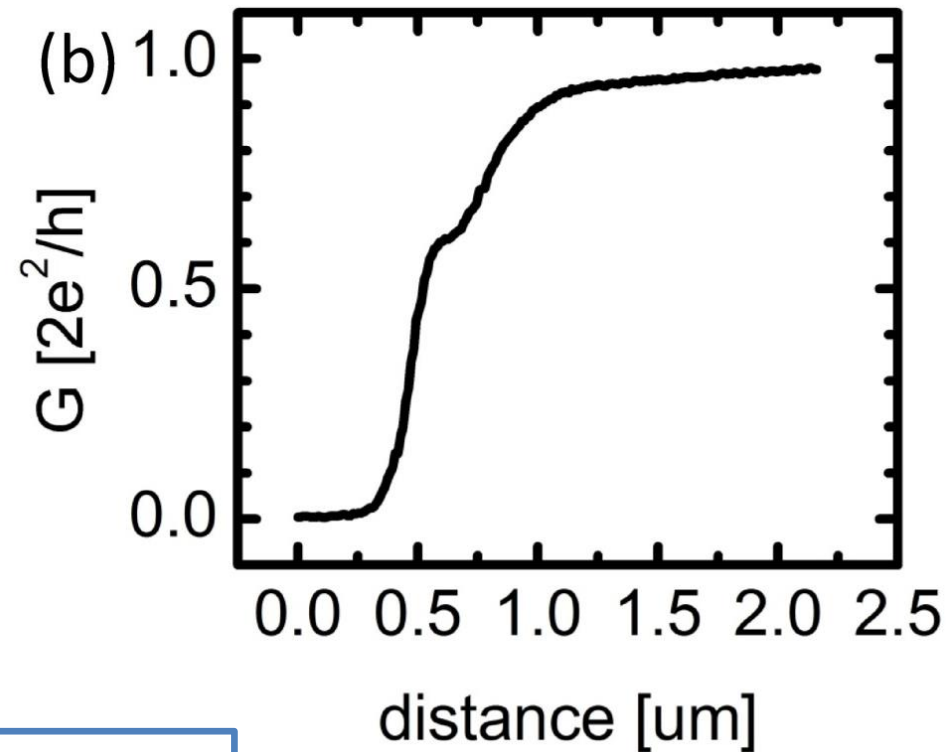
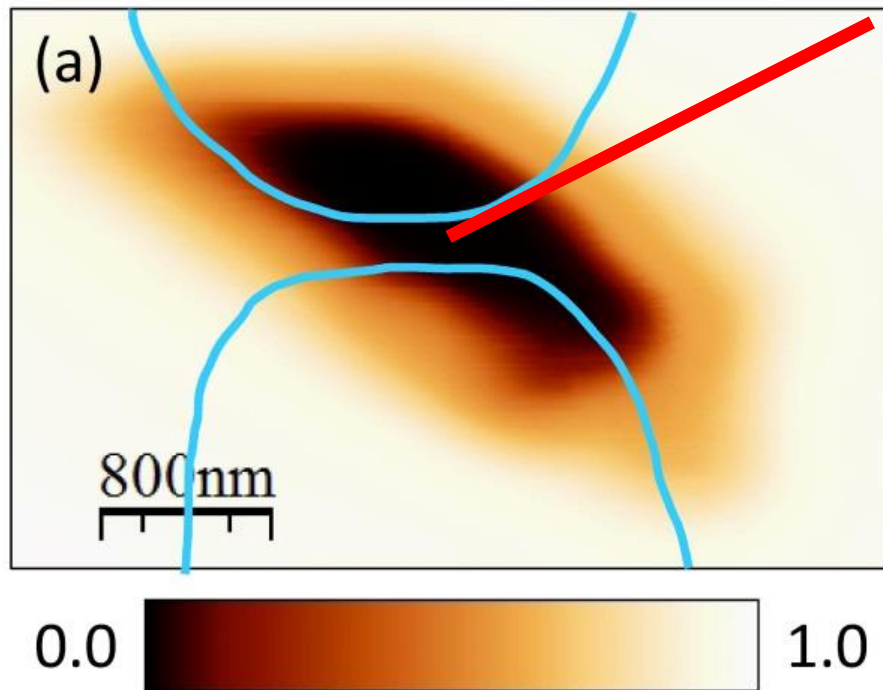
A. Iagallo *et al.*, arXiv:1311.6303

0.7 Anomaly in Device B



A. Iagallo *et al.*, arXiv:1311.6303

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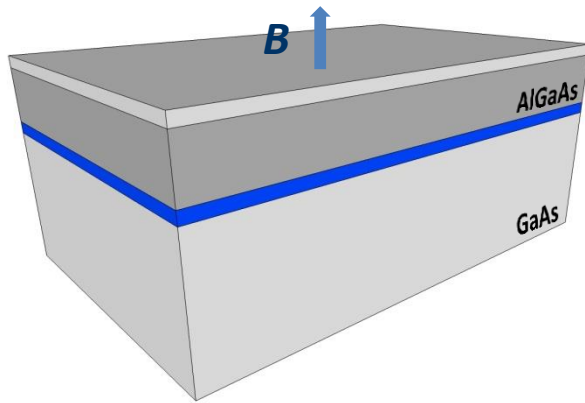


The 0.7 anomaly is observed irrespective of the presence of localized defects and is therefore a fundamental property

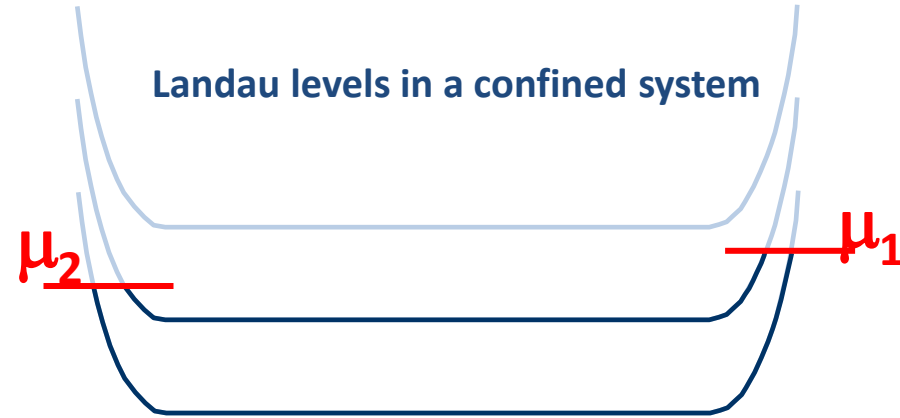
A. Iqbal *et al.*, arXiv:1311.6303

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The non-interacting picture of the QH effect

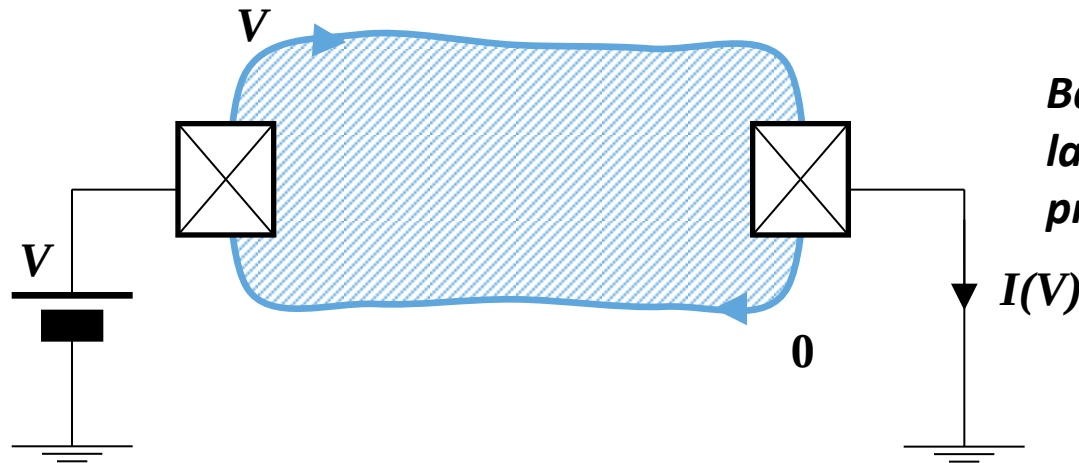


2DES
in high field



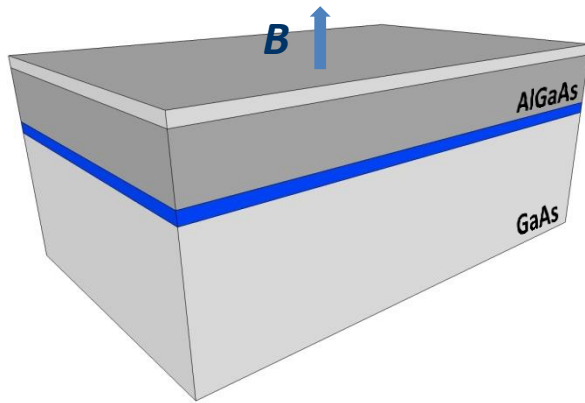
- Edge state picture:
current is carried by chiral 1D channels

$$G \equiv \frac{dI}{dV} = \nu \frac{e^2}{h}$$

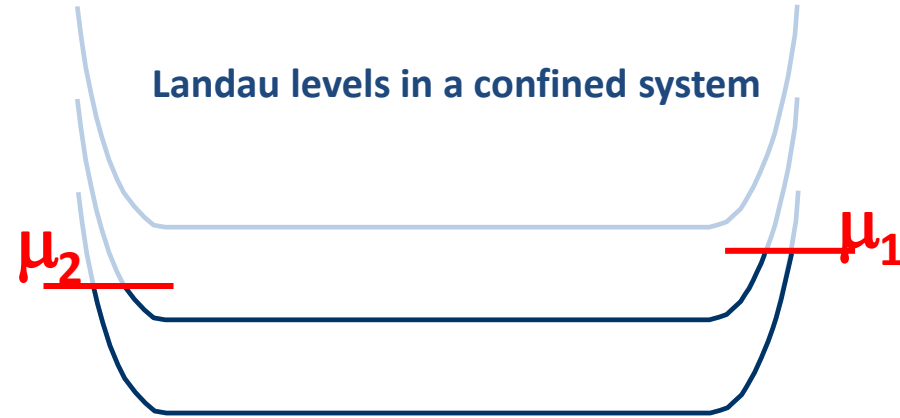


Backscattering is suppressed due to the large spatial separation between counter-propagating channels

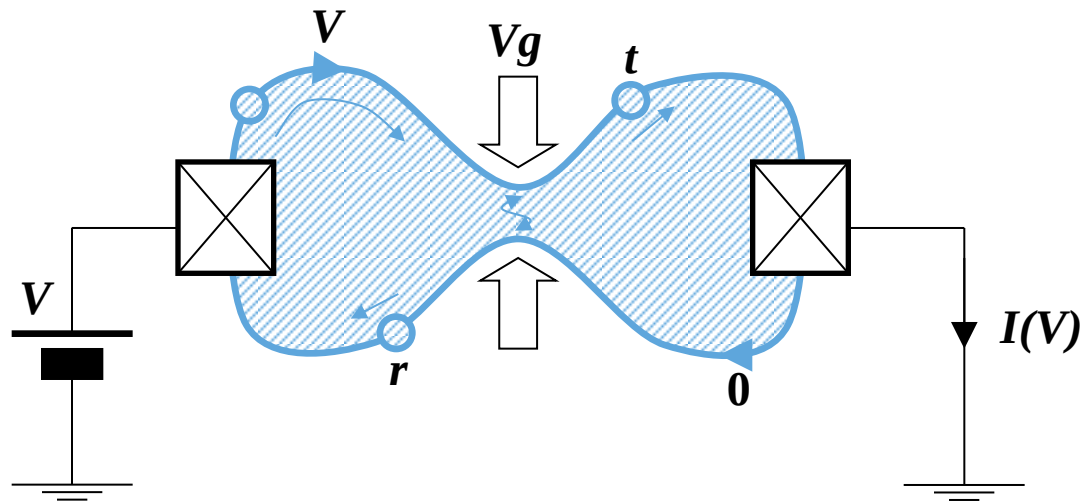
The non-interacting picture of the QH effect



2DES
in high field



- Edge state picture:
current is carried by chiral 1D channels



With a QPC we can intentionally induce backscattering, which provides us information about the edge properties

Roddaro et al.: PRL **90** (2003) 046805

Roddaro et al.: PRL **93** (2004) 046801

Roddaro et al.: PRL **95** (2005) 156804

Roddaro, Paradiso et al.: PRL **103** (2009) 016802

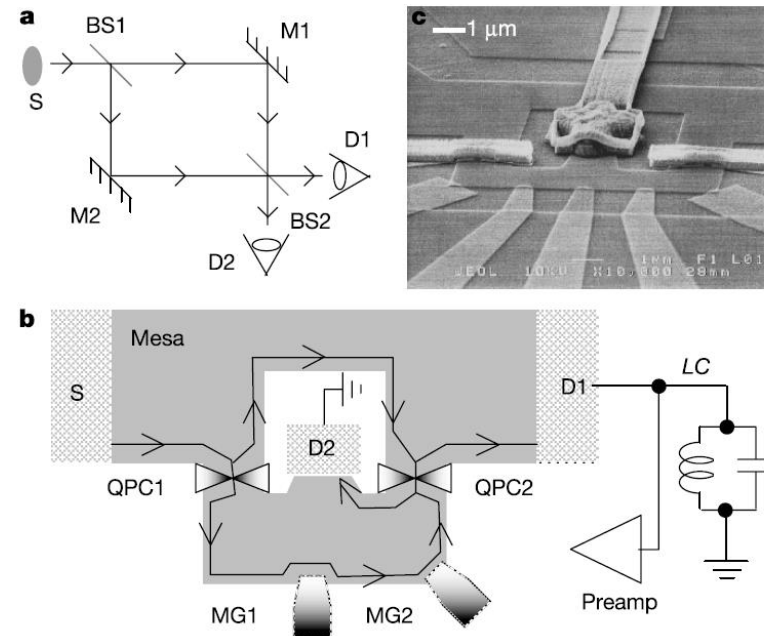
Edge channel-based interferometers

The very large coherence length has been exploited to implement complex interferometers as the electronic Mach-Zehnder.

Puzzle: so far, MZI only work with electron-like excitations. **The interference of fractional quasi-particles is inexplicably still elusive**

An electronic Mach-Zehnder interferometer

Yang Ji, Yunchul Chung, D. Sprinzak, M. Heiblum, D. Mahalu & Hadas Shtrikman



Ji *et al.*: Nature **422**, 415 (2003)

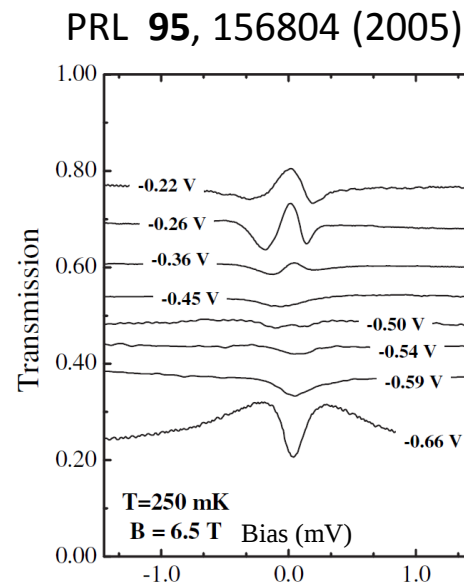
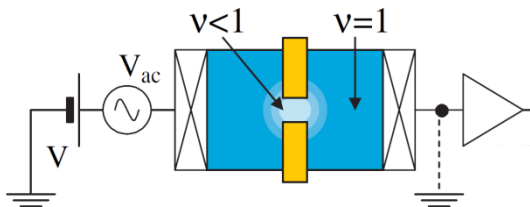
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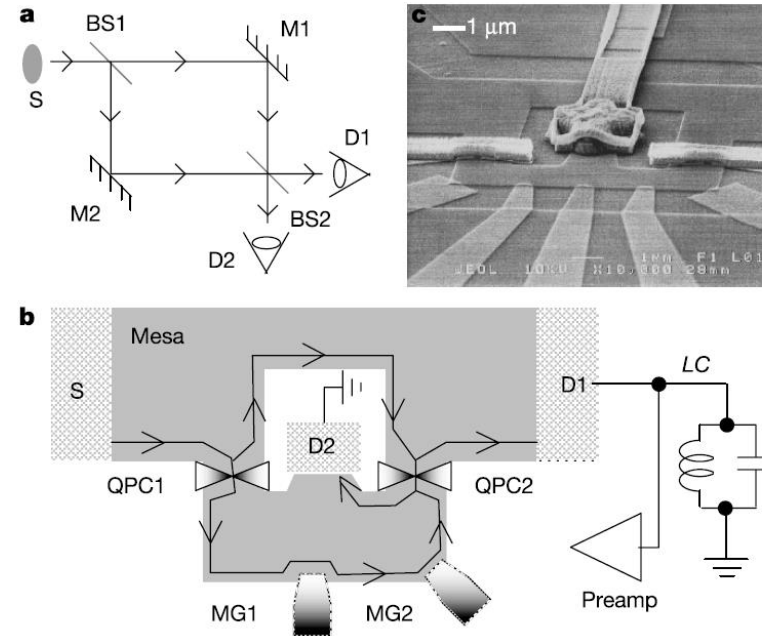
Role of the inner edge structure?

Roddaro *et al.*: experiments on QPCs revealed signatures of **fractional components** in “simple” integer channels



An electronic Mach-Zehnder interferometer

Yang Ji, Yunchul Chung, D. Sprinzak, M. Heiblum, D. Mahalu & Hadas Shtrikman



Ji *et al.*: Nature **422**, 415 (2003)

Need for **spatially** resolved measurements

Non-interacting VS interacting picture

- The self consistent potential due to e-e interactions modifies the edge structure
- For any realistic potential the density goes smoothly to zero.

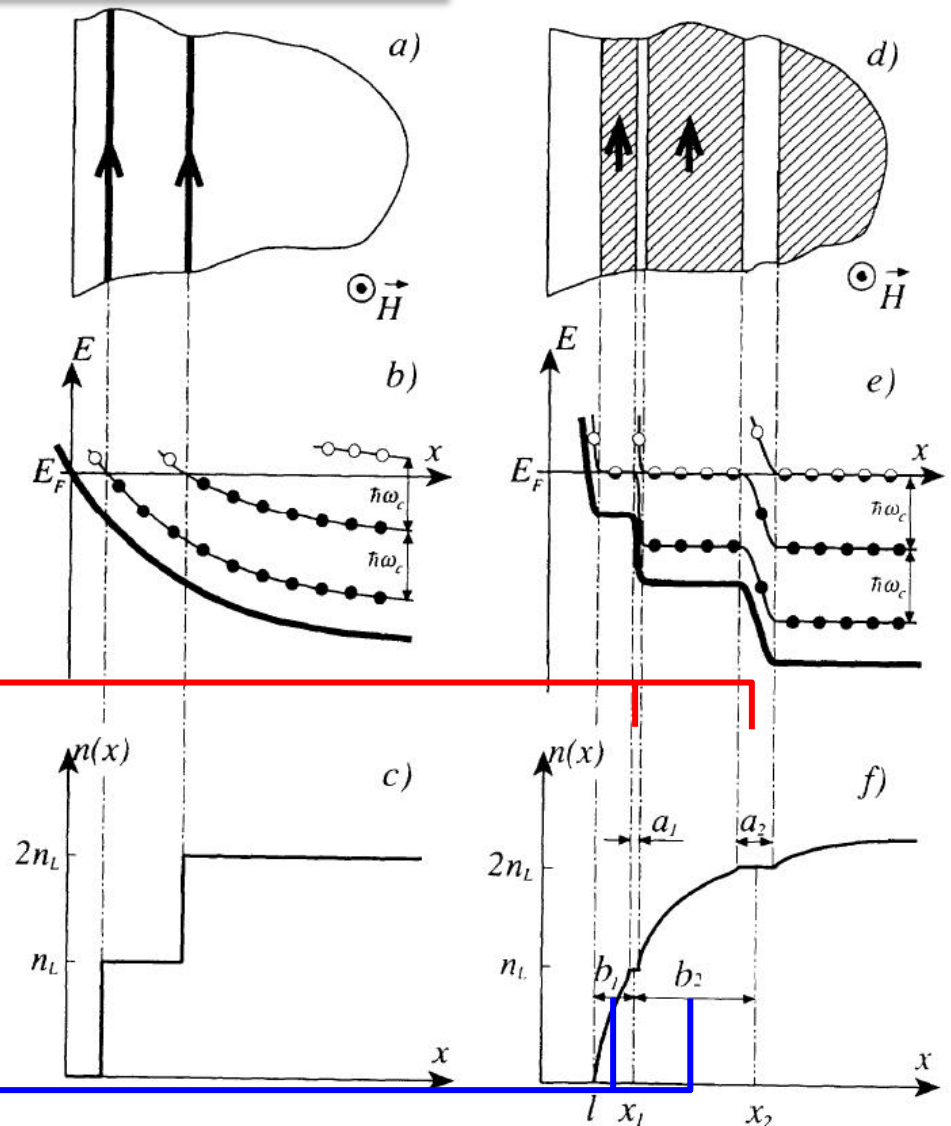
- Alternating compressible and incompressible stripes arise at the sample edge

Incompressible stripes:

- The electron density is constant
- The potential has a jump

Compressible stripes:

- The electron density has a jump
- The potential is constant



D. B. Chklovskii *et al.*:
PRB **46** (1992) 4026.

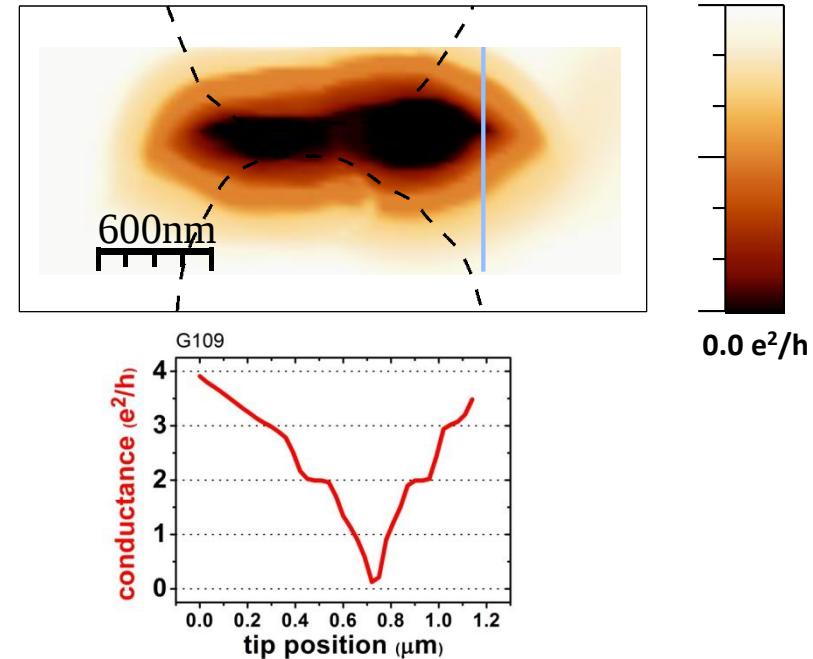
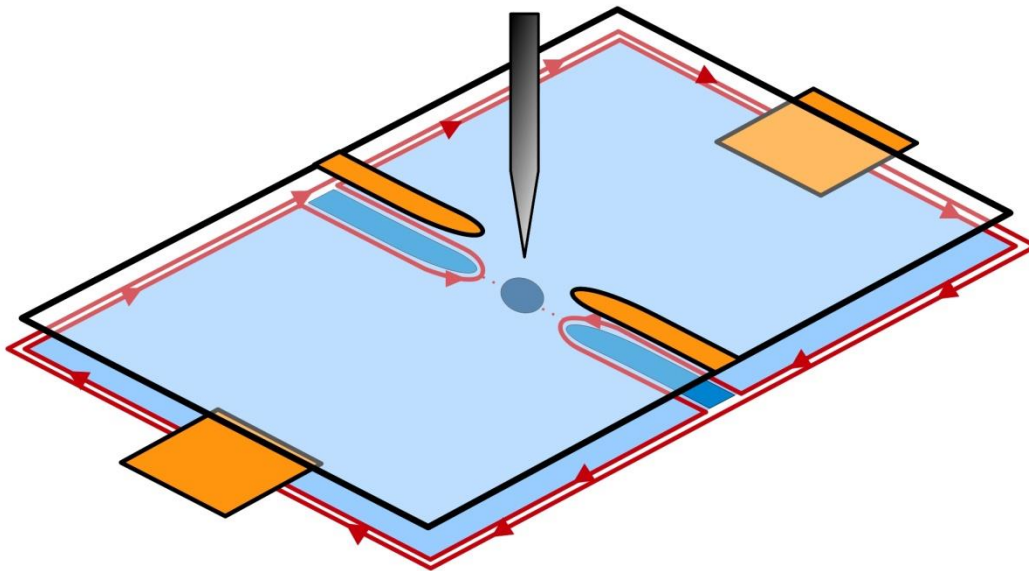
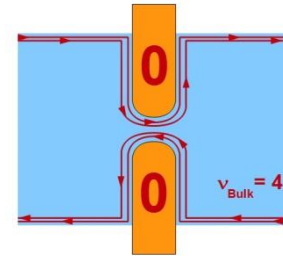
National Enterprise for nanoScience and nanoTechnology

SGM Group

NEST

Edge channel tomography by SGM

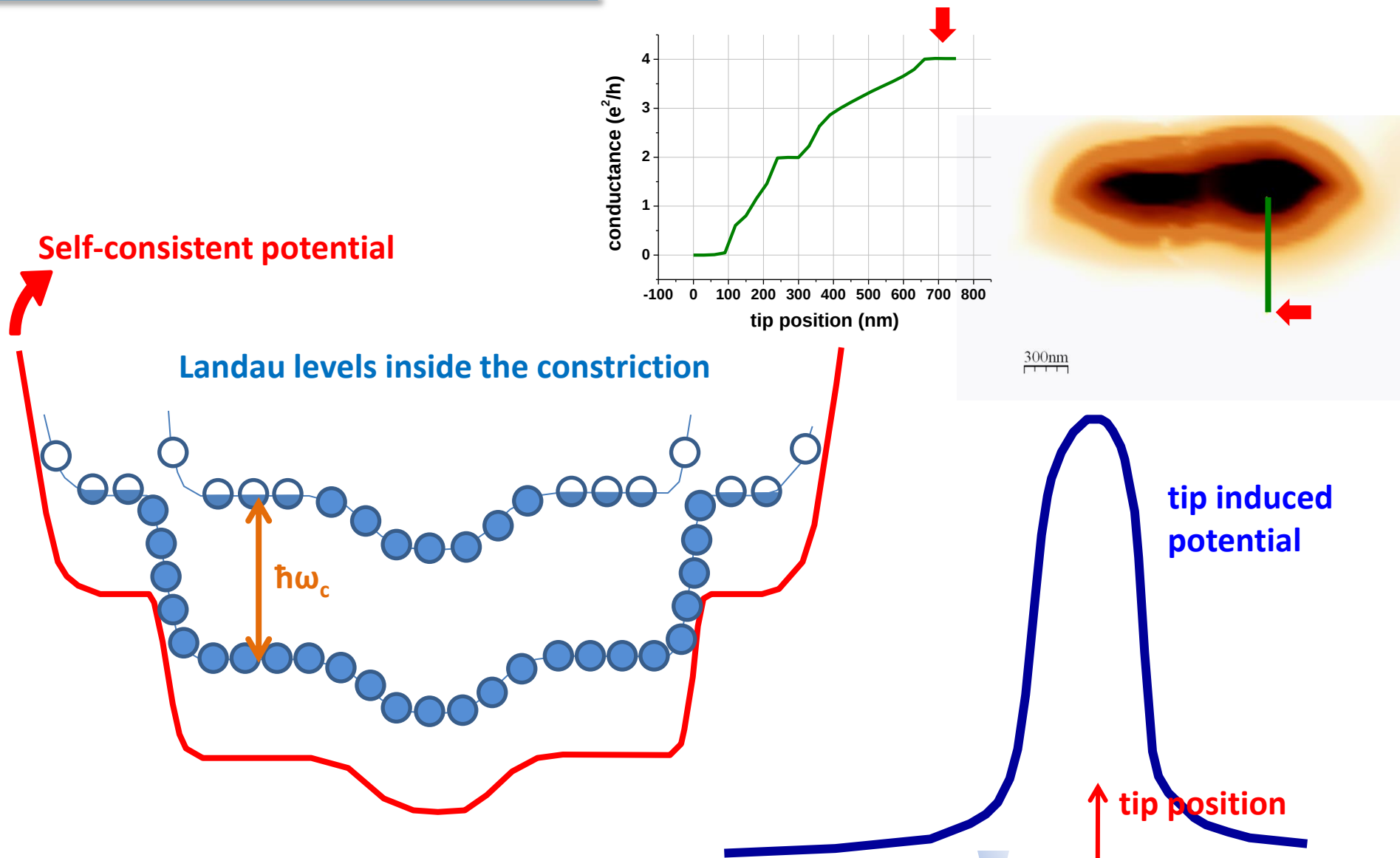
SGM technique: we **select** individual channels from the edge of a quantized 2DEG, we **send** them to the constriction and make them **backscatter** with the biased **SGM tip**.



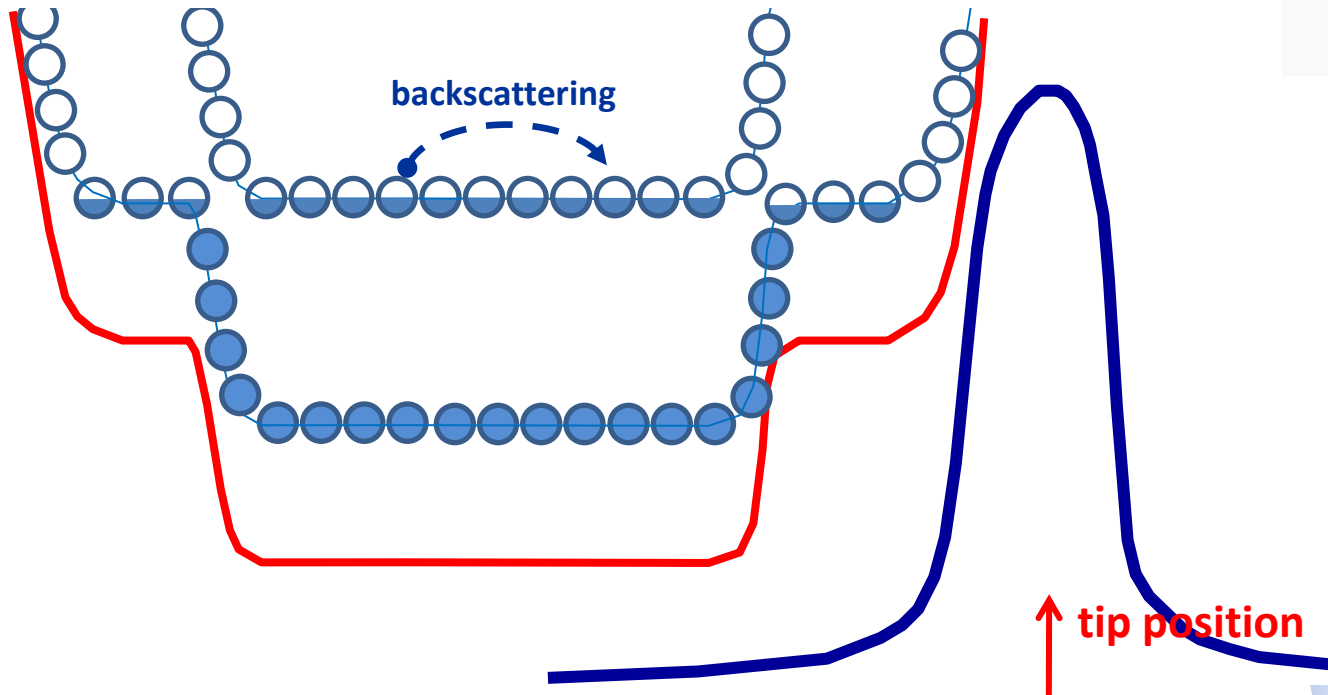
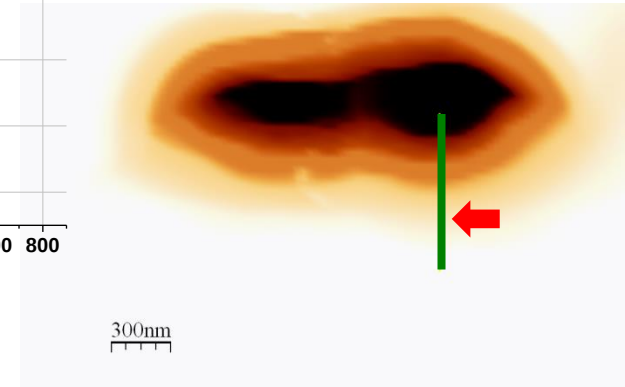
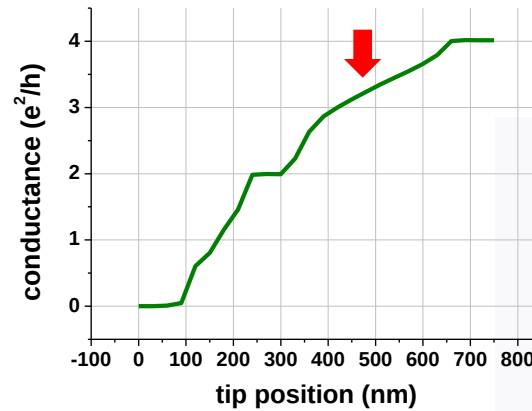
- Bulk filling factor $\nu=4$
- $B = 3.04 \text{ T}$
- 2 spin-degenerate edge channels
- gate-region filling factors $g_1 = g_2 = 0$

N. Paradiso *et al.*, *Physica E* 42 (2010) 1038.

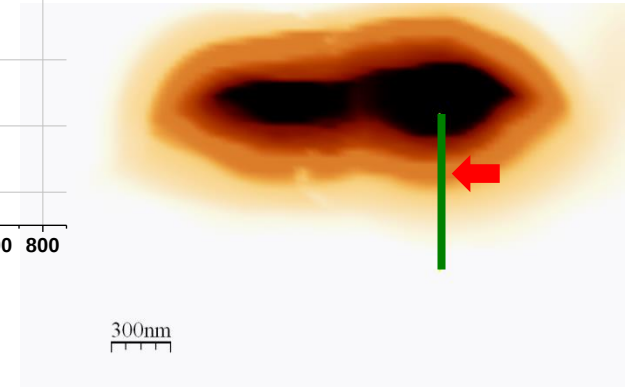
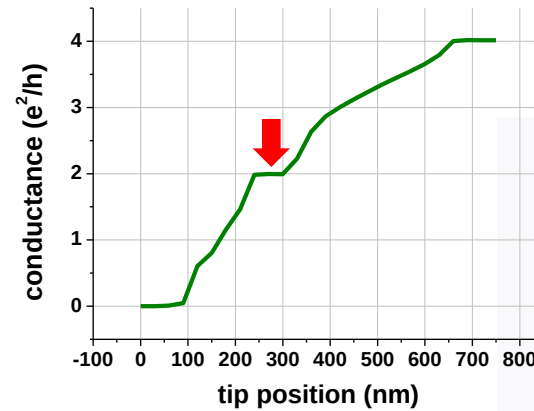
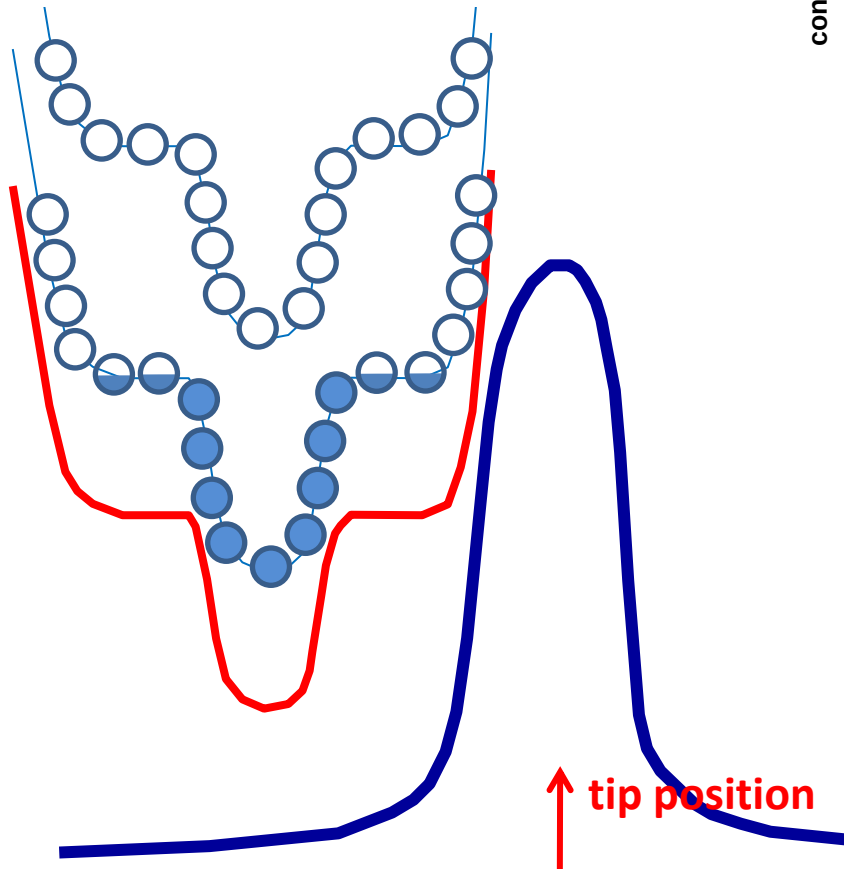
How we probe incompressible stripes



How we probe incompressible stripes



How we probe incompressible stripes

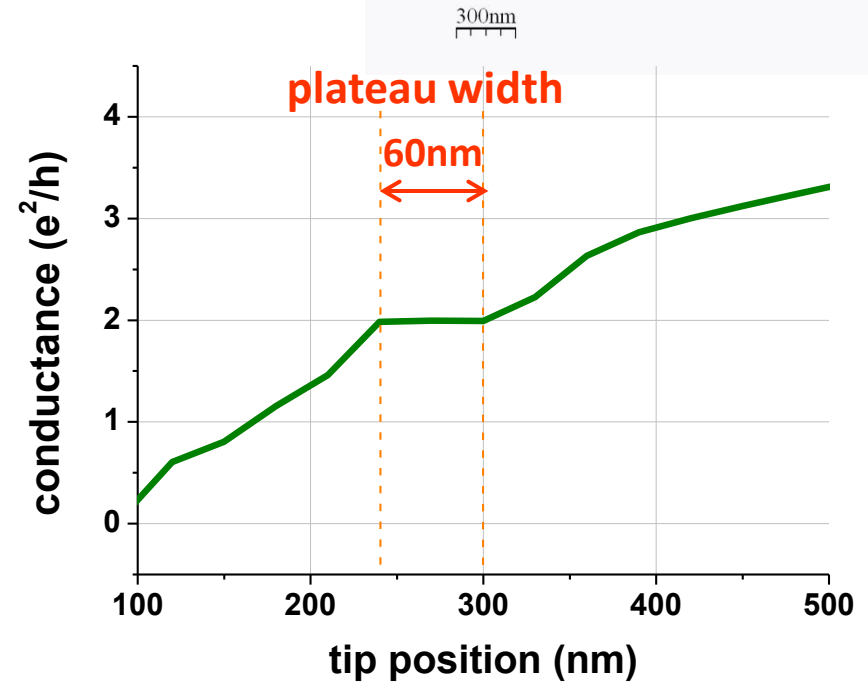
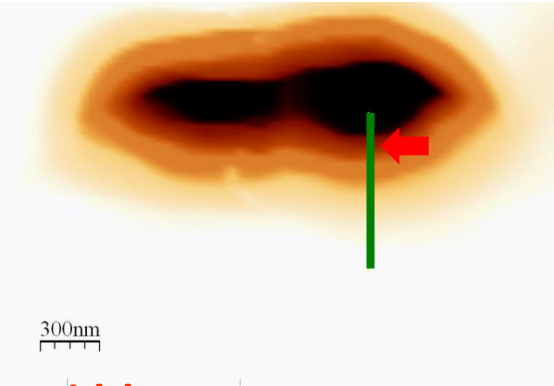
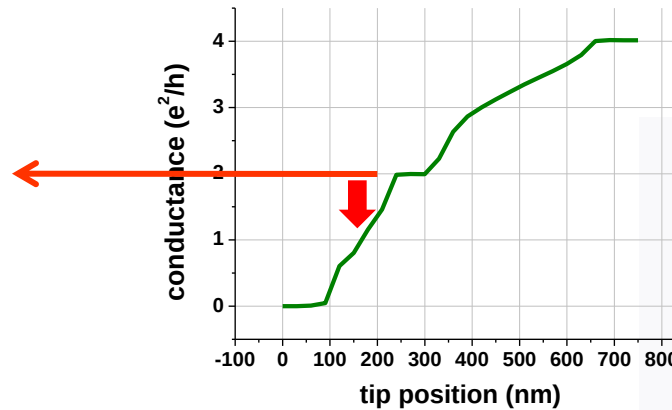
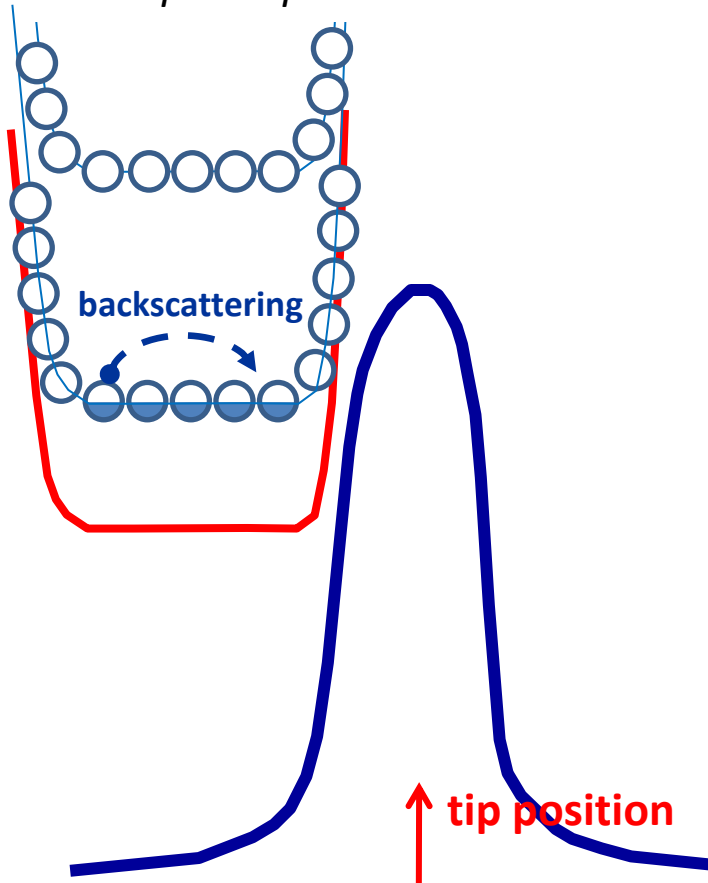


How we probe incompressible stripes

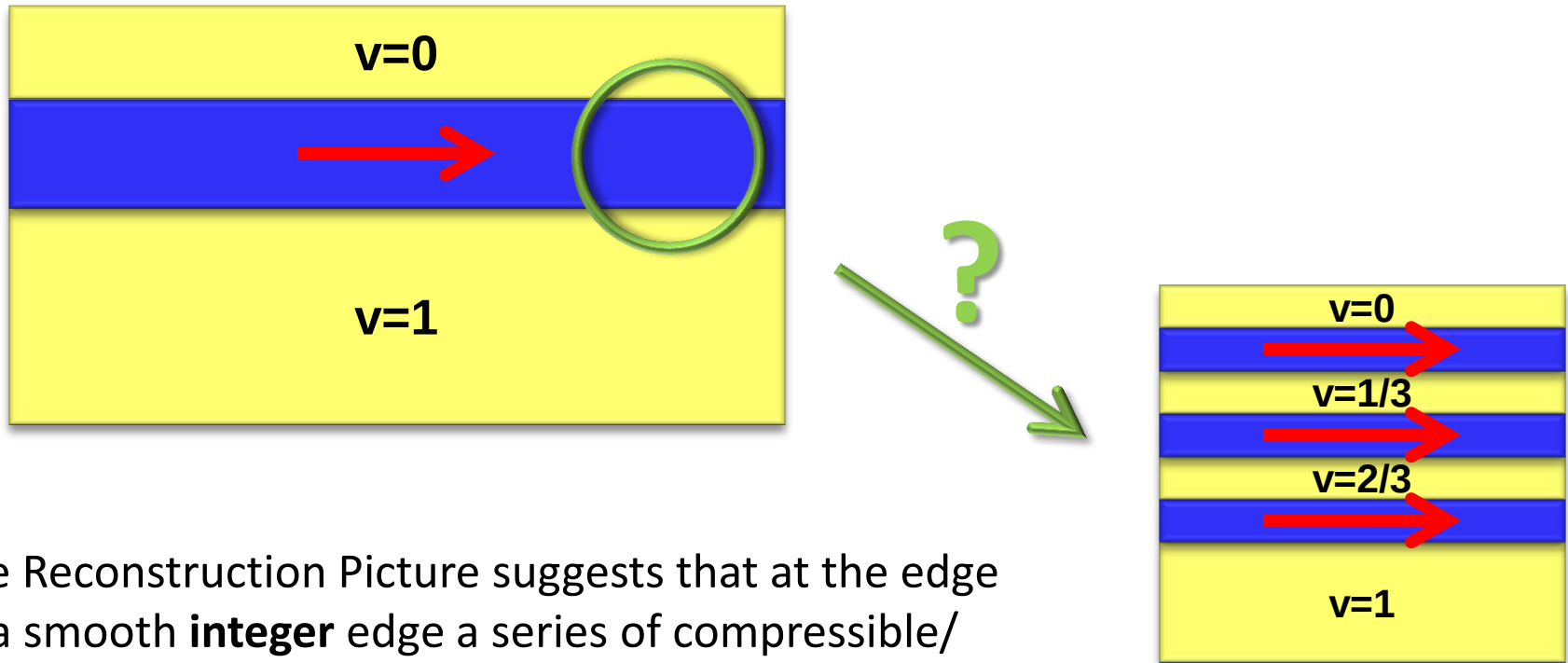
Energy gap: $\hbar\omega = 5.7$ meV

Plateau width: 60 nm

Incompr. stripe width: ≈ 30 nm

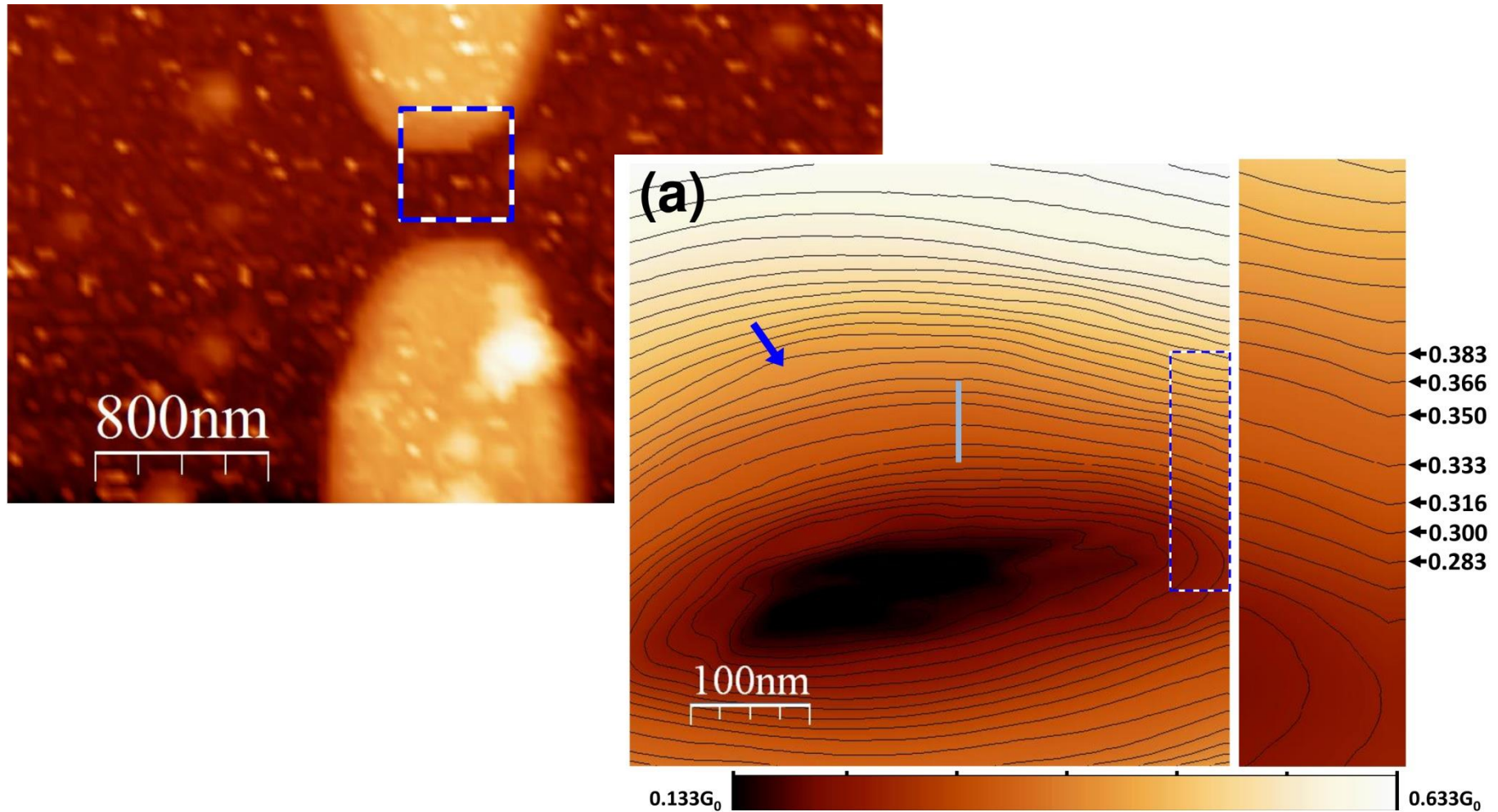


Imaging fractional structures in integer channels ($\nu=1$)



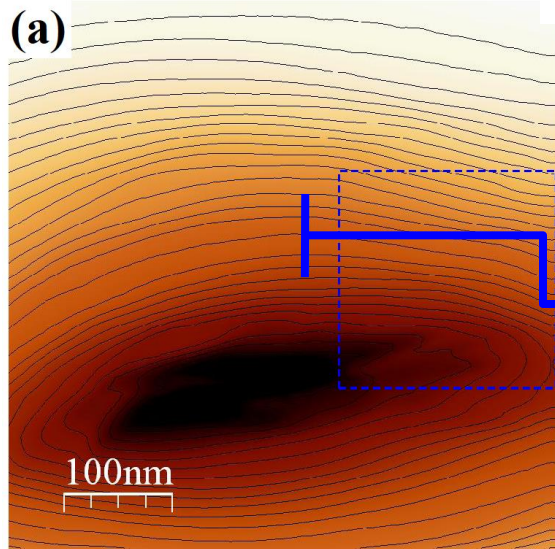
The Reconstruction Picture suggests that at the edge of a smooth **integer** edge a series of compressible/**incompressible fractional stripes** can occur.

Imaging fractional structures in integer channels ($\nu=1$)

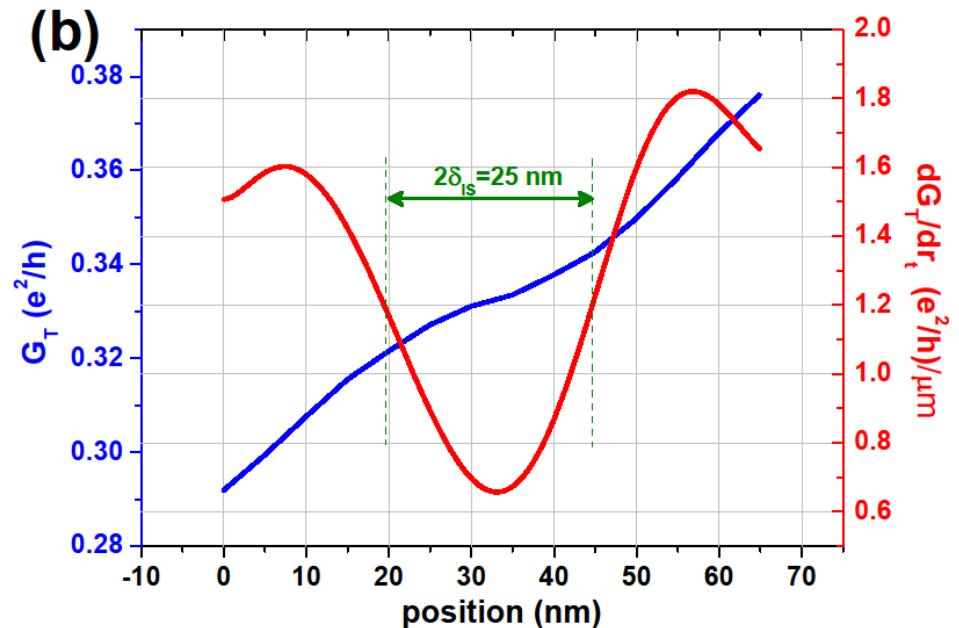
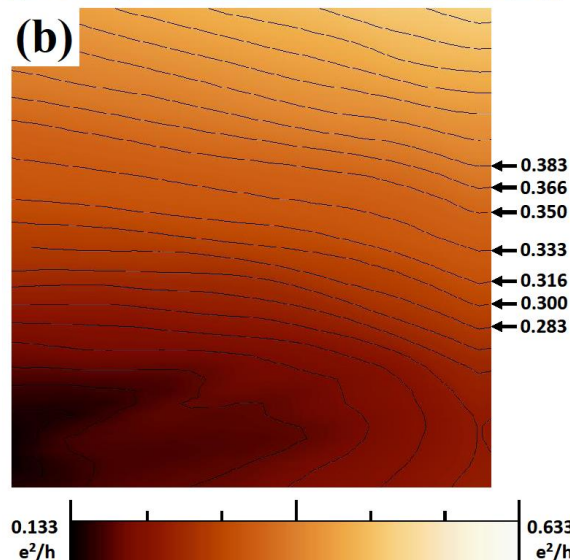


N. Paradiso *et al.* Phys. Rev. Lett. **108**, 246801 (2012)

Imaging fractional structures in integer channels ($\nu=1$)

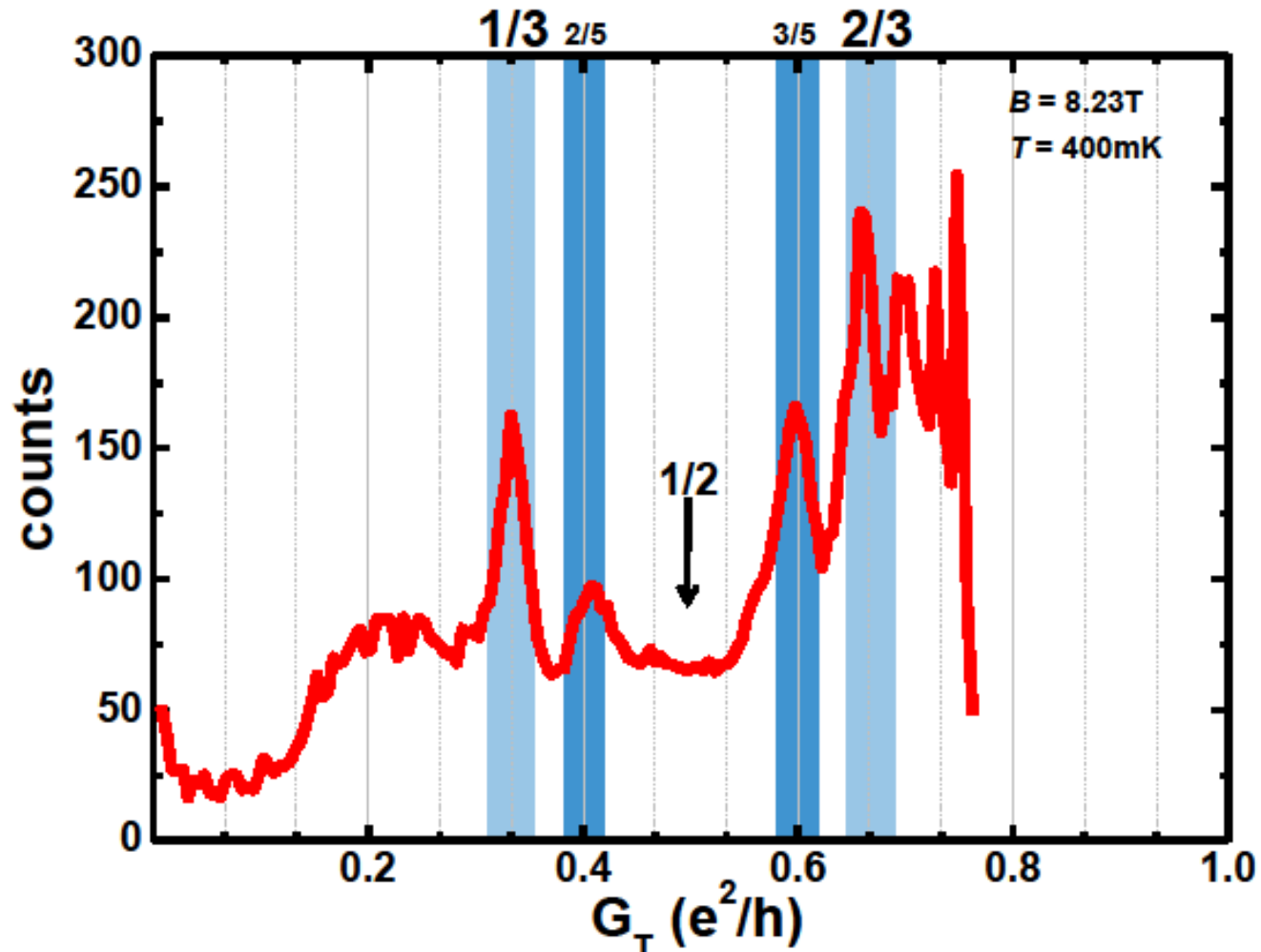


$$\delta_{IS} \sim 12 \text{ nm}$$



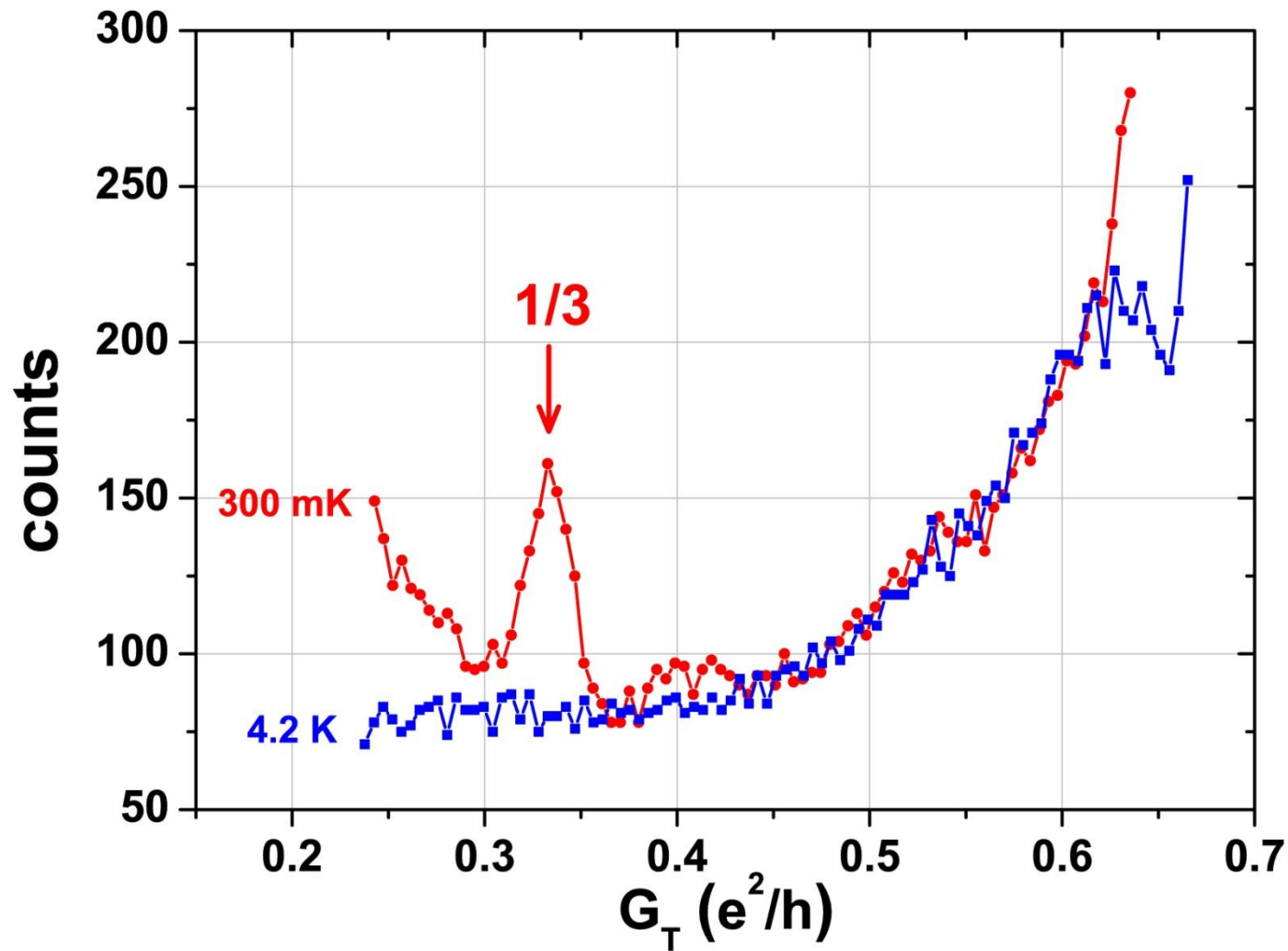
N. Paradiso *et al.* Phys. Rev. Lett. 108, 246801 (2012)

Imaging fractional structures in integer channels ($\nu=1$)



N. Paradiso *et al.* Phys. Rev. Lett. 108, 246801 (2012)

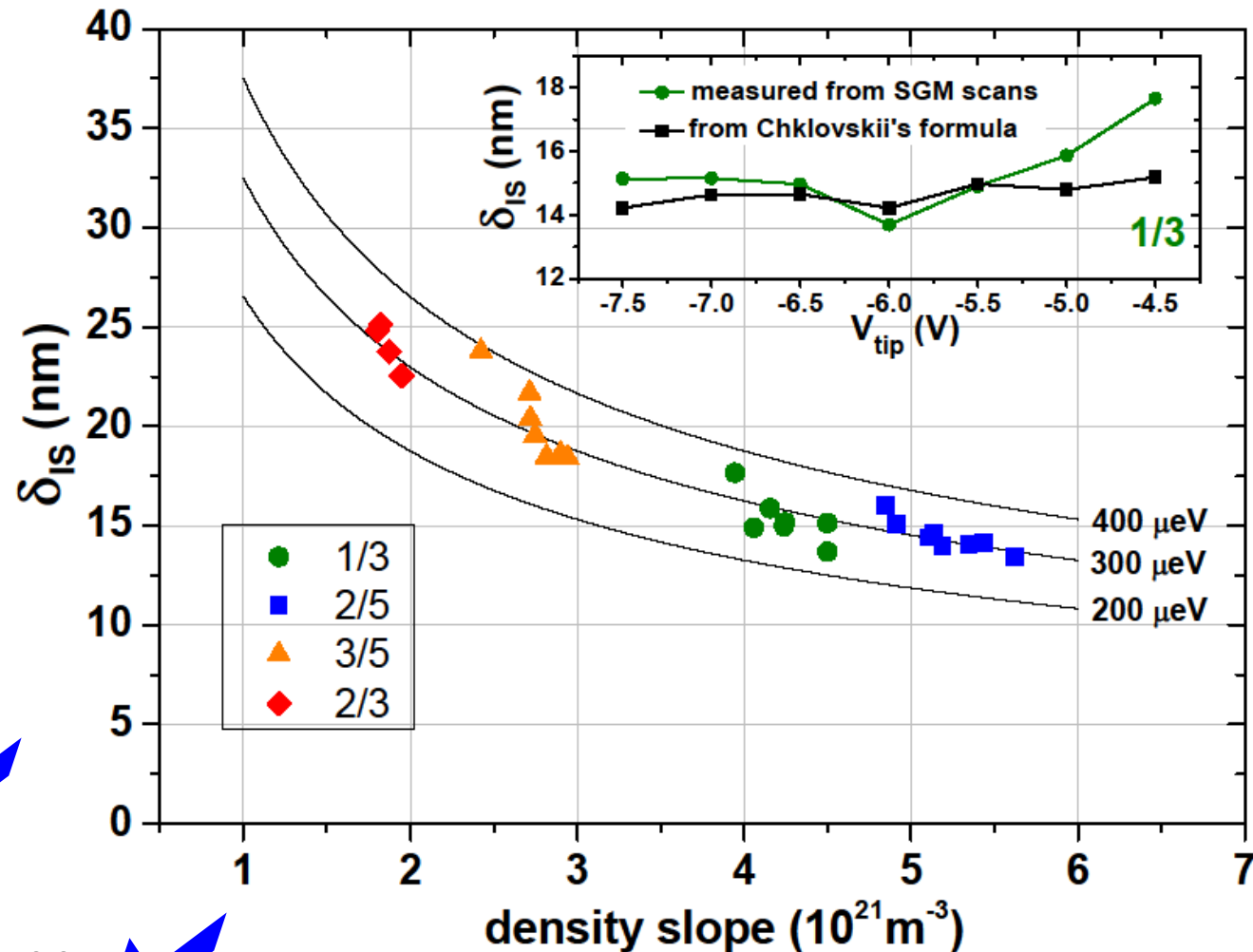
Temperature dependence of 1/3 peak in histogram



N. Paradiso *et al.* Phys. Rev. Lett. **108**, 246801 (2012)

Fractional edge reconstruction

The IS width values (colored dots) obtained from SGM images compare well with the reconstruction picture predictions (black lines)



Inner edge structure
demonstrated and imaged

Quantitative test of the IS width
dependence on the density slope

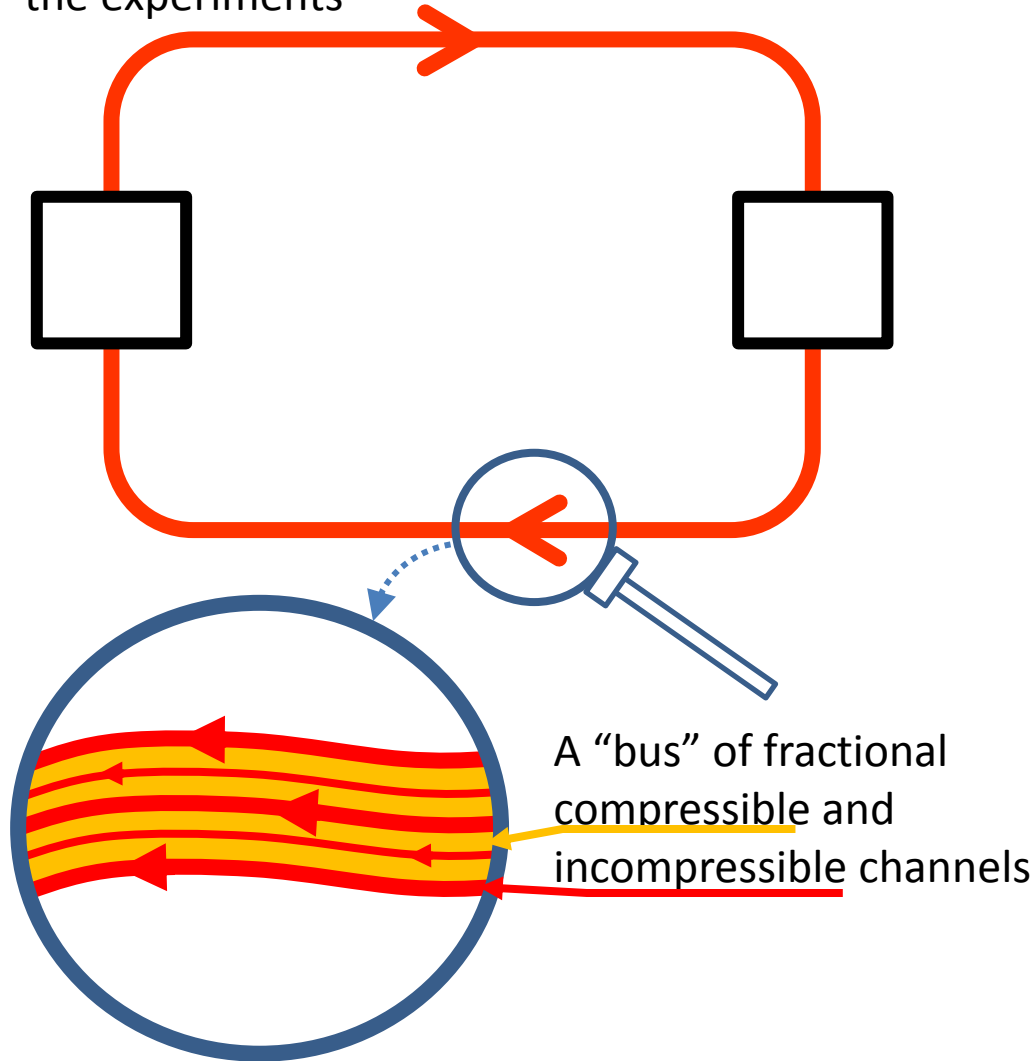
N. Paradiso *et al.* Phys. Rev. Lett. 108, 246801 (2012)

- Basics of Scanning Gate Microscopy (SGM)
- Quantum Point Contact w/o magnetic field
- QPC in the quantum Hall regime
- **Edge channel equilibration**



Can we exploit the non-trivial edge structure?

The picture of a QH device emerging from the experiments



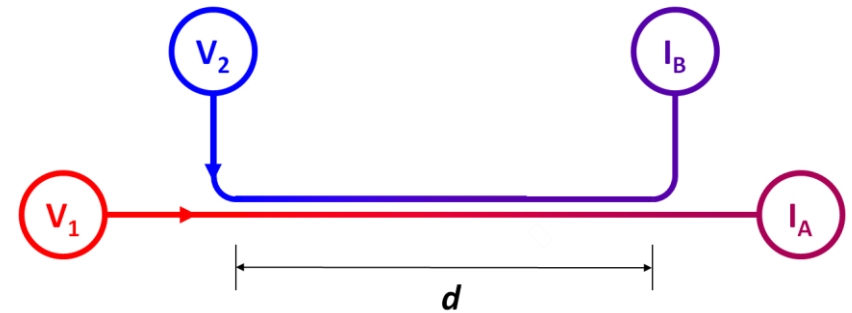
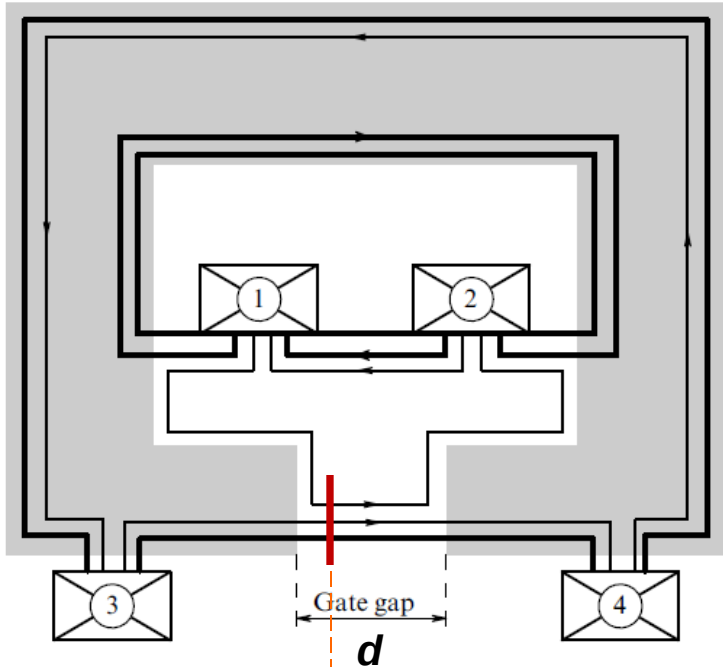
Is it possible to study and image the microscopic details of the inter-channel scattering?

Studying the inter-channel equilibration

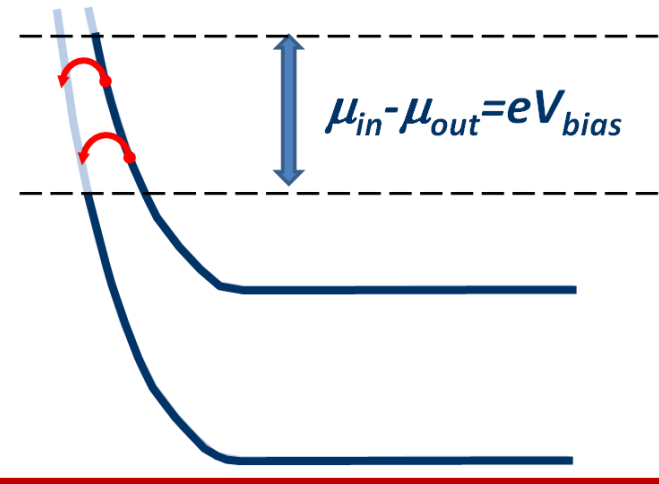
Edge states in the regimes of integer and fractional quantum Hall effects

E V Deviatov

Physics – Uspekhi **50** (2) 197–218 (2007)



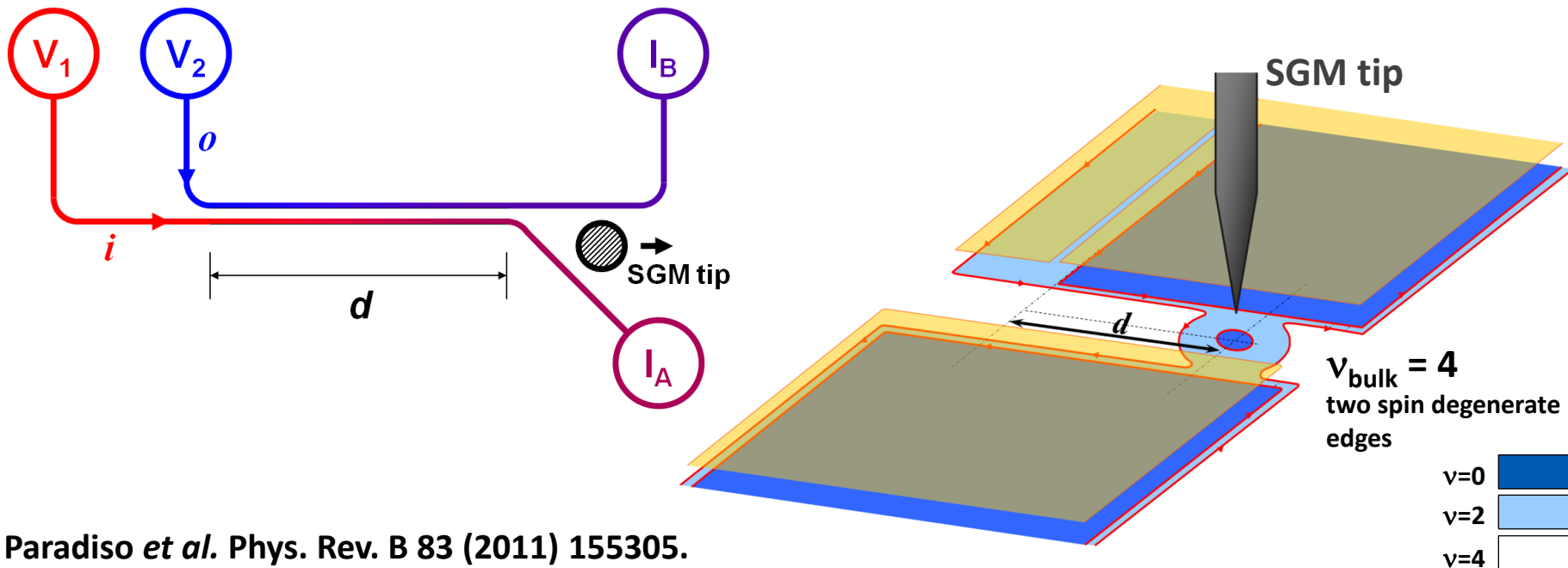
devices with fixed interaction length d :
elusive determination of **the microscopic details of the equilibration mechanisms**



The opportunity of the Scanning Gate Microscopy

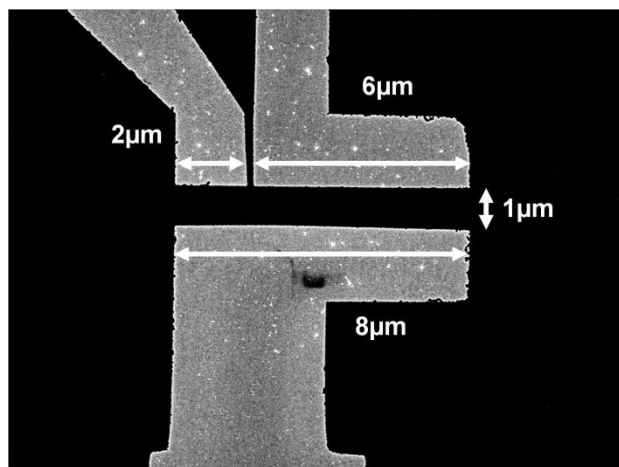
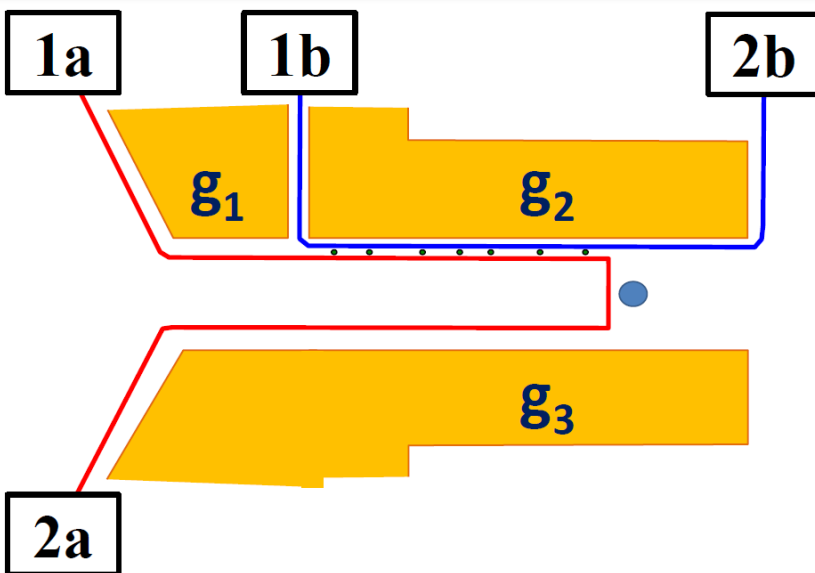
Our technique allows to selectively control the channel trajectory

Our idea: exploit the mobile depletion spot induced by the SGM to **continuously tune d**

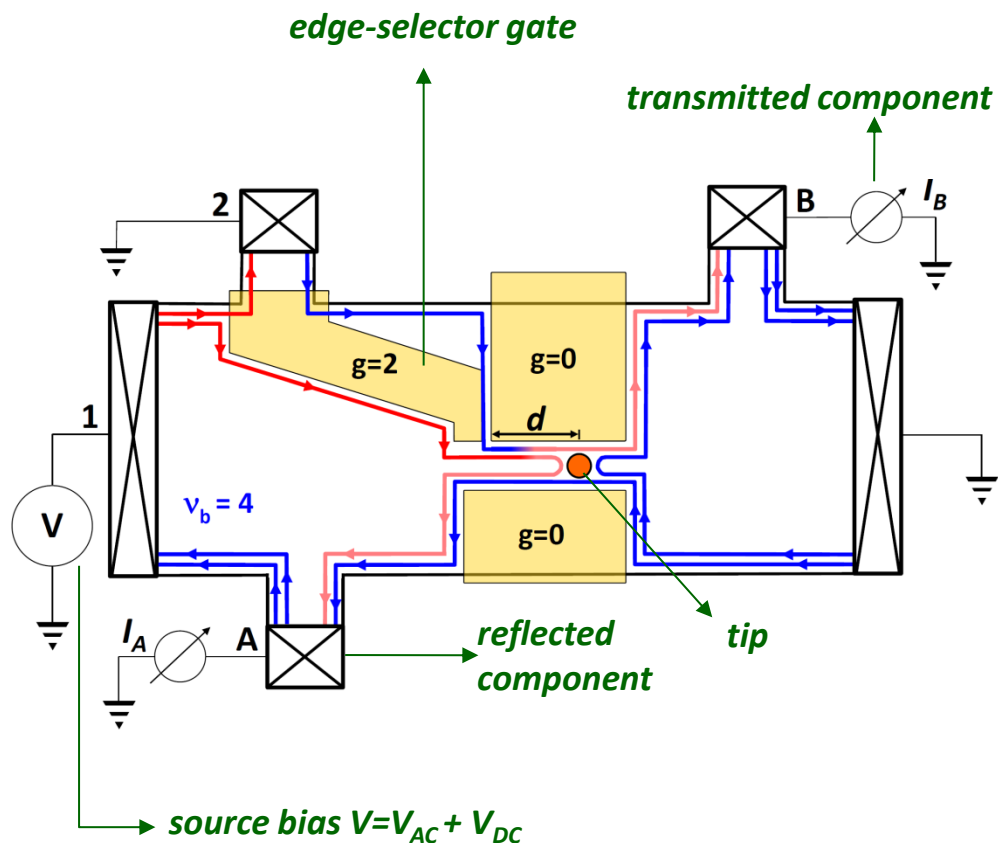


N. Paradiso *et al.* Phys. Rev. B 83 (2011) 155305.

Experimental setup



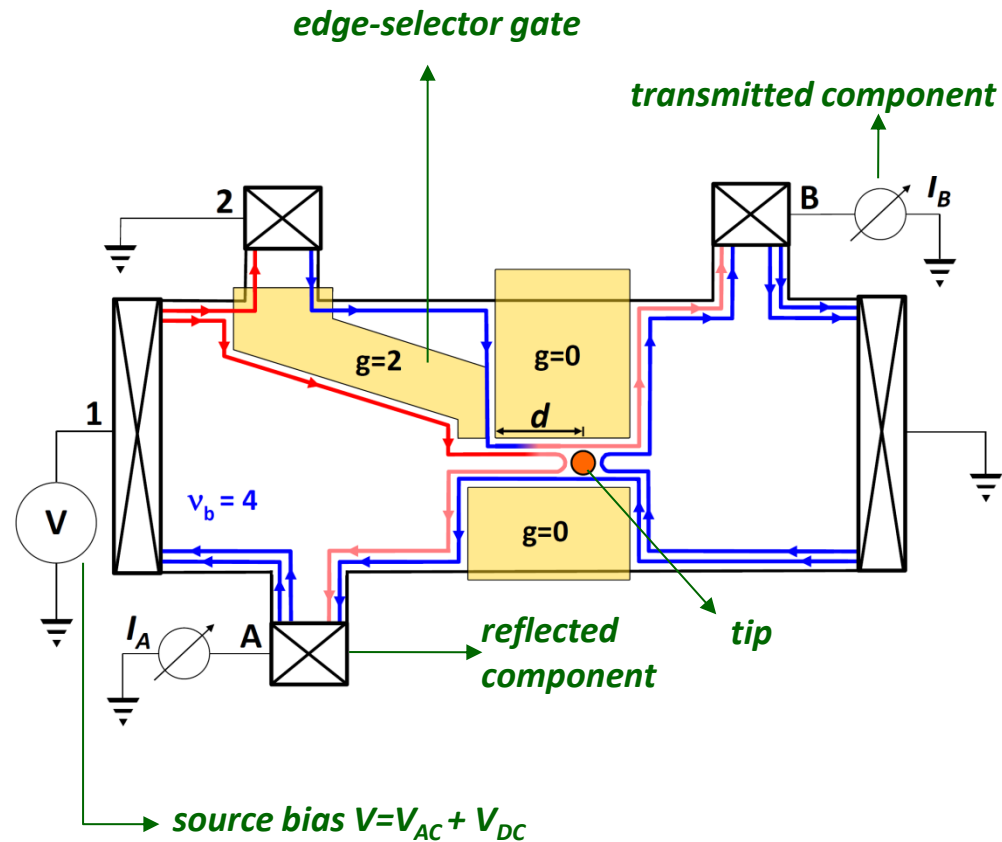
SEM micrograph of the device



Scheme of the electronic setup

Experimental setup

	No eq.	Full eq.
A	$2 e^2/h$	$1 e^2/h$
B	$0 e^2/h$	$1 e^2/h$

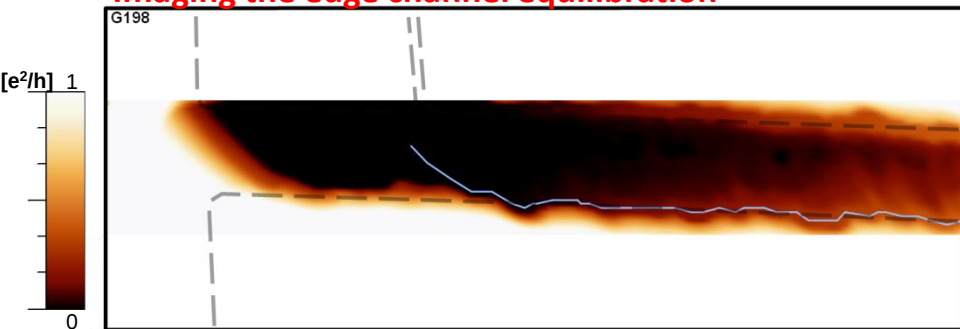


Scheme of the electronic setup

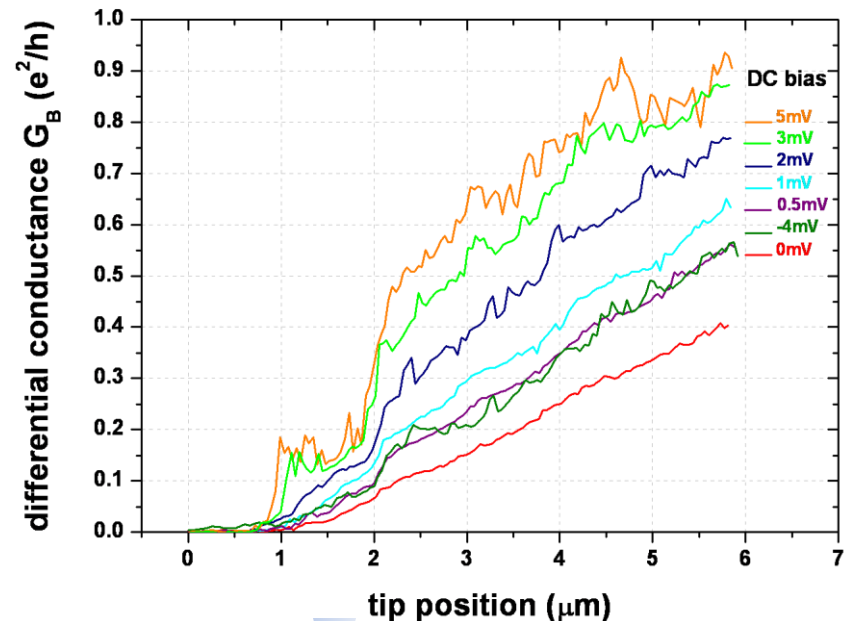
Imaging the inter-channel equilibration

The profiles of $G_B(d)$ along the trajectory show a strict dependence on the local details

Imaging the edge channel equilibration



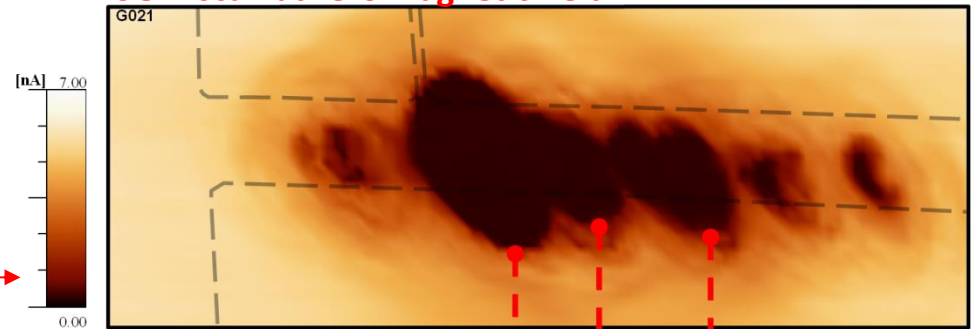
Source bias: $V_{AC}=50\mu V$, $V_{DC}=0mV$



Imaging the inter-channel equilibration

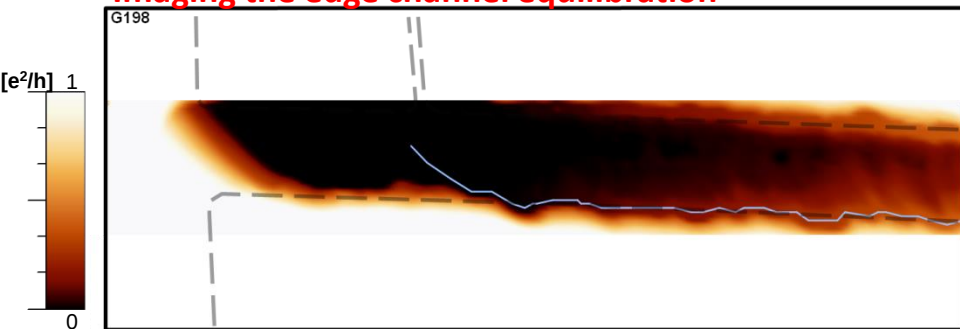
We can directly image the potential induced by the most important defects by means of a scan at zero magnetic field

SGM scan at zero magnetic field

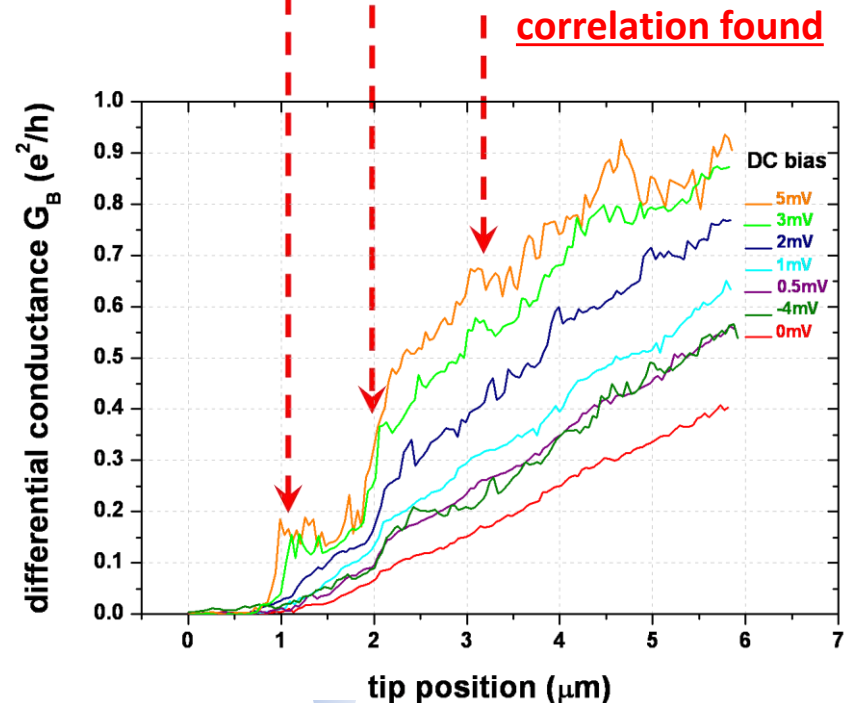


The profiles of $G_B(d)$ along the trajectory show a strict dependence on the local details

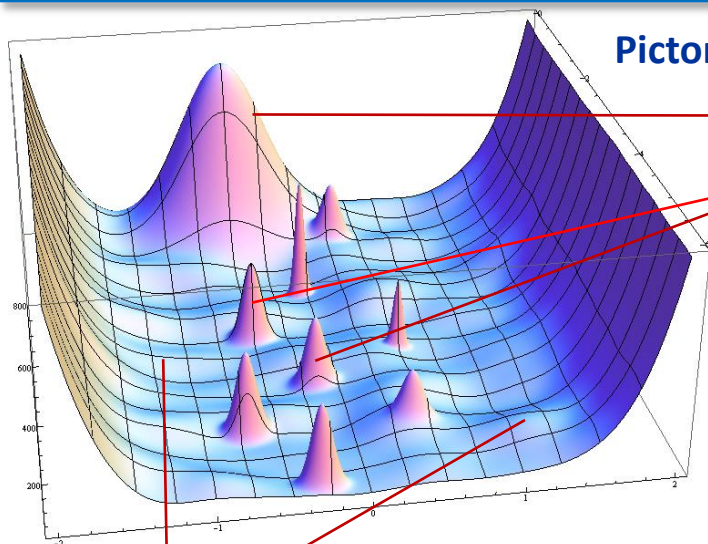
Imaging the edge channel equilibration



Source bias: $V_{AC}=50\mu V$, $V_{DC}=0mV$



Tight binding simulations



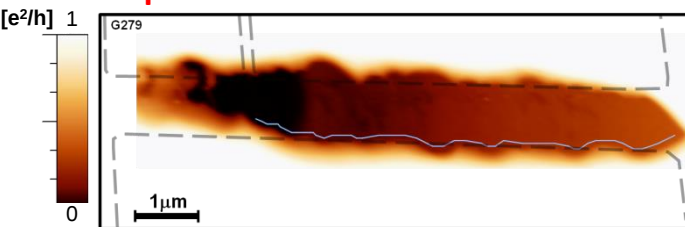
Pictorial model for the disorder potential

• tip potential

• “big impurities” potential

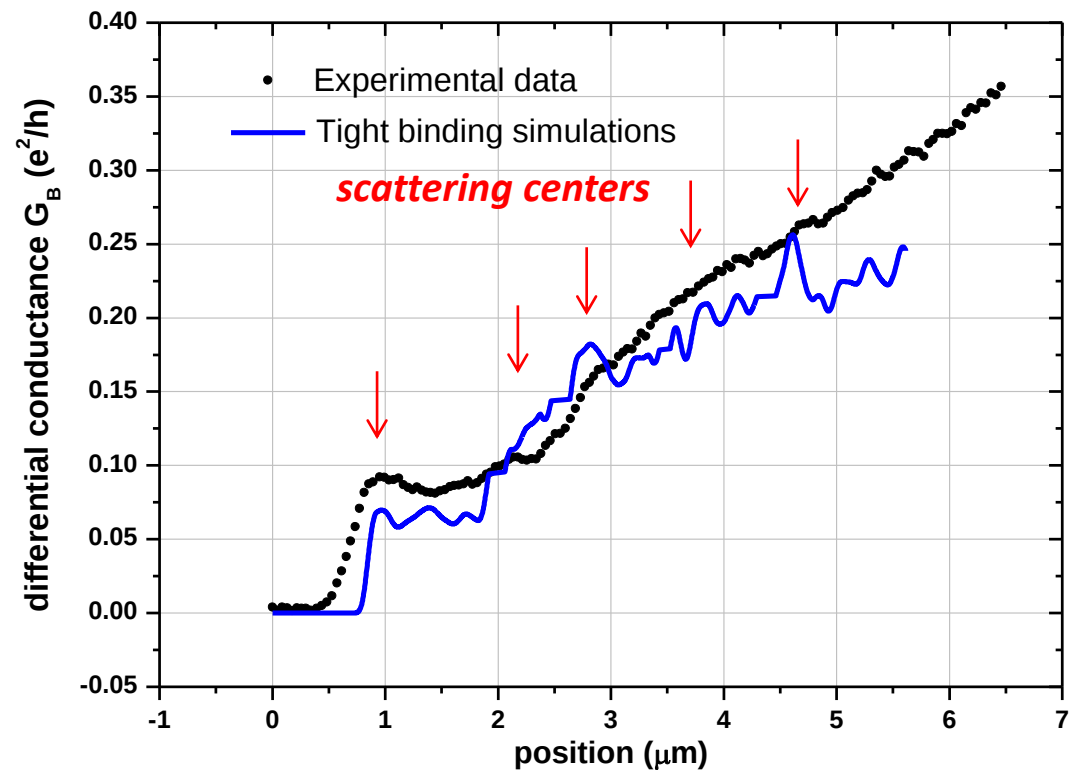
• background potential

SGM map of the inter-channel equilibration in another device



Simulations made by the theoretical group of
Scuola Normale Superiore (Pisa, Italy)

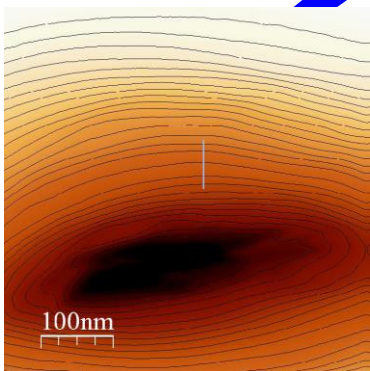
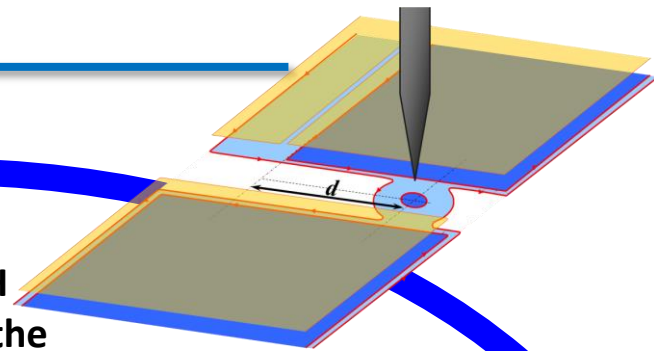
D. Venturelli, F. Taddei, V. Giovannetti and R. Fazio



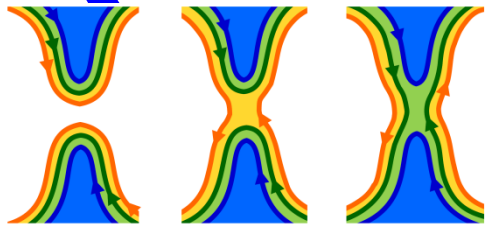
Summary

SGM technique in the QH regime

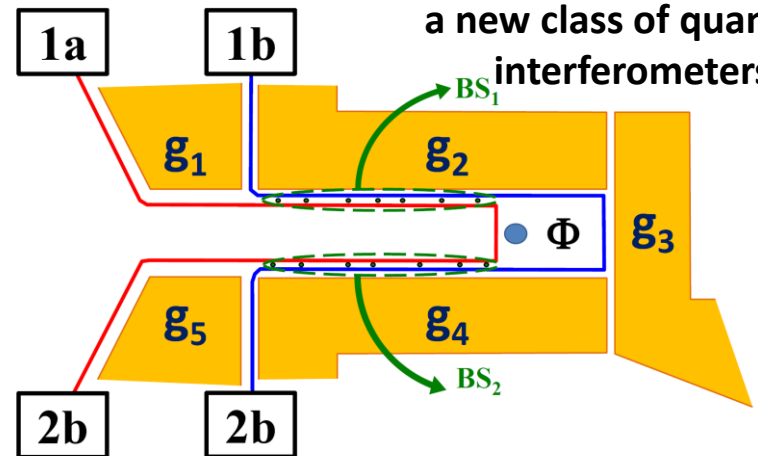
size-tunable QH circuits: study of the channel mixing



Edge channel tomography: imaging of fractional stripes



a new class of quantum interferometers



Future directions:
Interference of fractional
quasi-particles ?

Conclusions

-  We explore the use of Scanning Gate Microscopy to study one-dimensional systems
-  The 0.7 anomaly is observed irrespective of the presence of localized defects and is therefore a fundamental property
-  Control of the edge channel trajectory by SGM allows us to study their structure
-  We observe a fractional substructure in integer QH channels and measured the width of fractional incompressible stripes
-  We built size-tunable QH circuits to directly image the equilibration between imbalanced co-propagating edges