

Josephson diode effect in high-mobility InSb nanoflags

Bianca Turini

NEST, Istituto Nanoscienze-CNR and Scuola Normale Superiore, Piazza San Silvestro, Pisa, Italy

National Enterprise for nanoScience and nanoTechnology



NEST

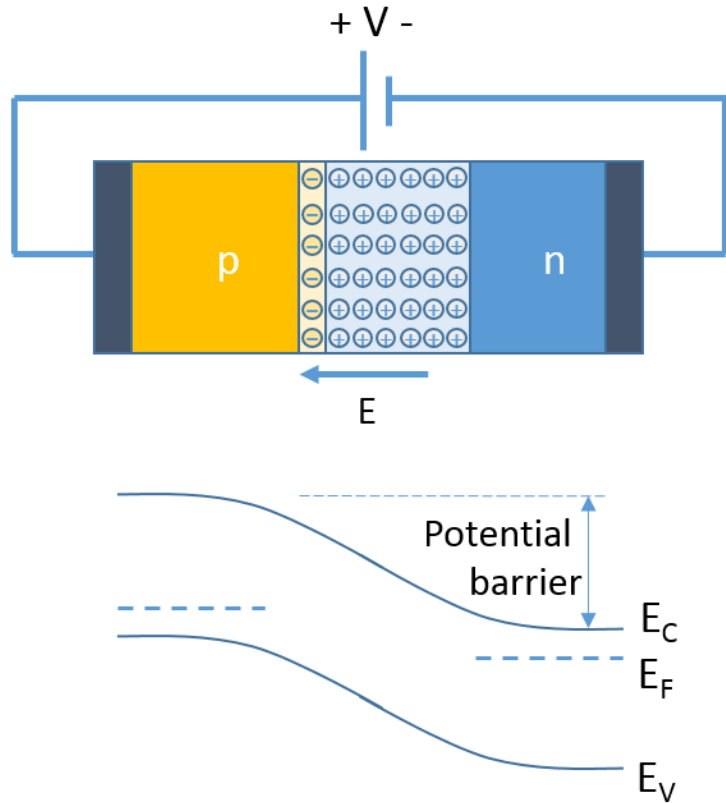
Outline of the talk

- ❖ Non-reciprocity in condensed matter systems
- ❖ InSb nanoflags for advanced devices
- ❖ Nanoflag-based Josephson junctions
- ❖ Josephson diode effect in InSb nanoflags

Outline of the talk

- ❖ **Non-reciprocity in condensed matter systems**
- ❖ InSb nanoflags for advanced devices
- ❖ Nanoflag-based Josephson junctions
- ❖ Josephson diode effect in InSb nanoflags

Non-reciprocity: a familiar concept



The p-n junction is at the basis of classical electronics.

Magneto-chiral anisotropy:

$$R = R_0(1 + \gamma_{MCA} \hat{e}_z \vec{B} \times \vec{I})$$

- Non-linear effect
- TRS-breaking required
- Elusive in CM systems

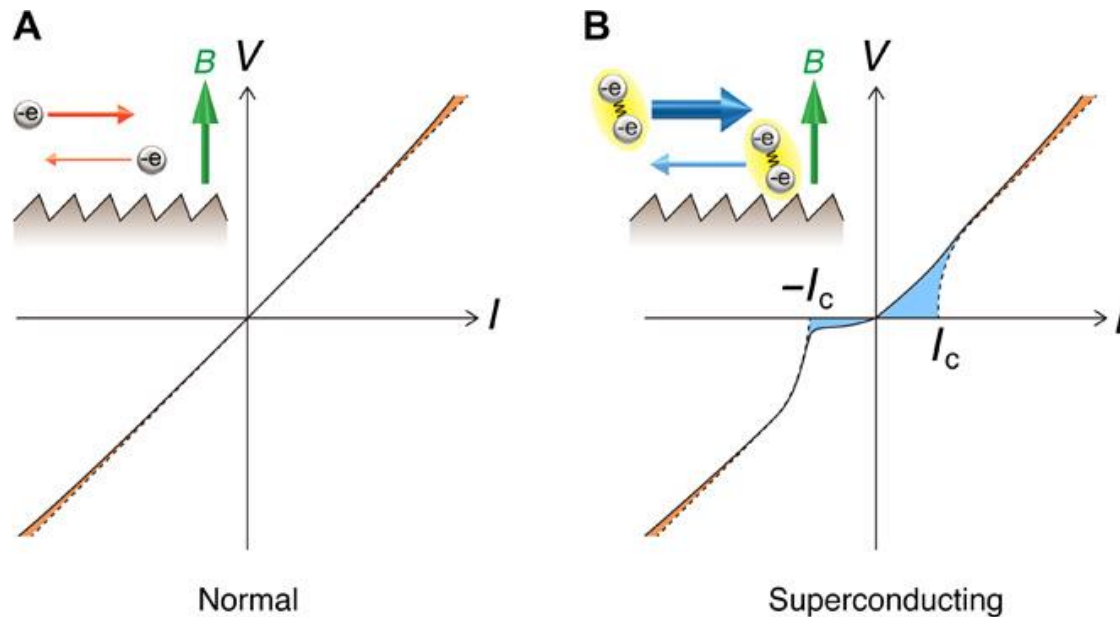
$$\gamma_{MCA} \left(\frac{E_{SOI}}{E_G} \right) \sim 10^{-3} - 10^{-2} \text{ T}^{-1} \text{ A}^{-1}$$

MCA in superconductors

- Superconducting order defines a new energy scale:

$$E_G \gg \Delta \sim \text{meV}$$

- MCA is strongly enhanced (10^5) in the resistive state
- What happens to the supercurrent?



SUPERCURRENT DIODE EFFECT

Article

Observation of superconducting diode effect

<https://doi.org/10.1038/s41586-020-2590-4>

Received: 14 March 2020

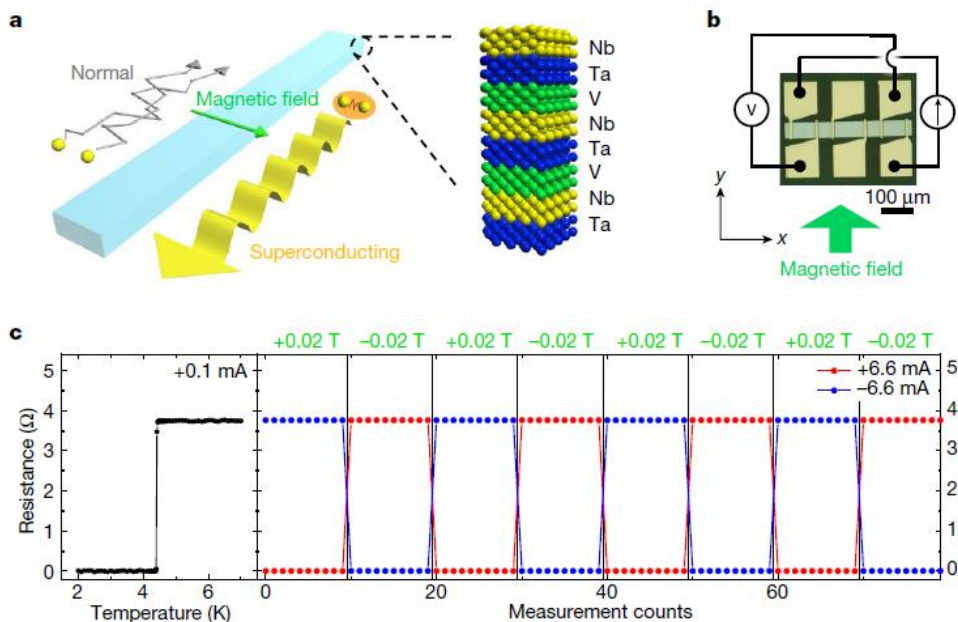
Accepted: 23 June 2020

Published online: 19 August 2020

Check for updates

Fuyuki Ando¹, Yuta Miyasaka¹, Tian Li¹, Jun Ishizuka², Tomonori Arakawa^{3,4}, Yoichi Shiota¹, Takahiro Moriyama¹, Youichi Yanase² & Teruo Ono^{1,4}✉

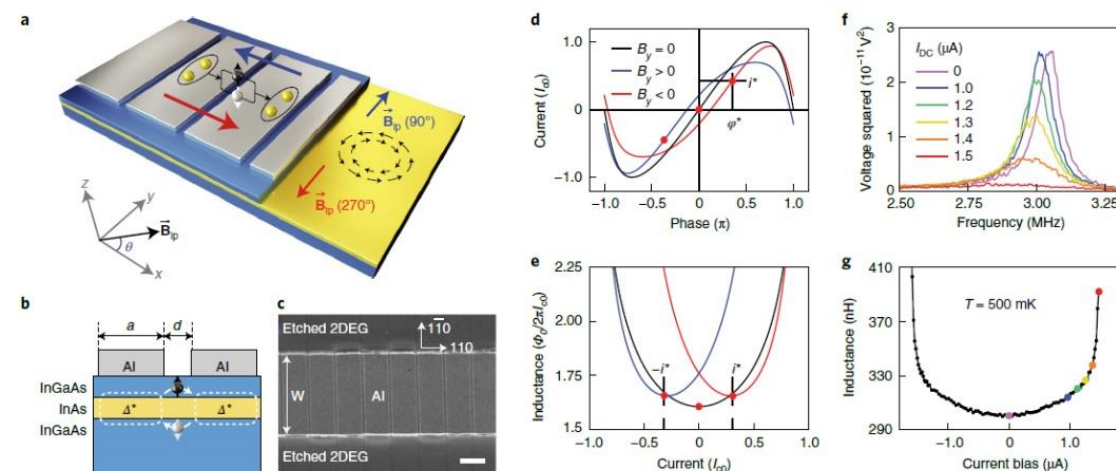
Nonlinear optical and electrical effects associated with a lack of spatial inversion symmetry allow direction-selective propagation and transport of quantum particles, such as photons¹ and electrons^{2–9}. The most common example of such nonreciprocal



Check for updates

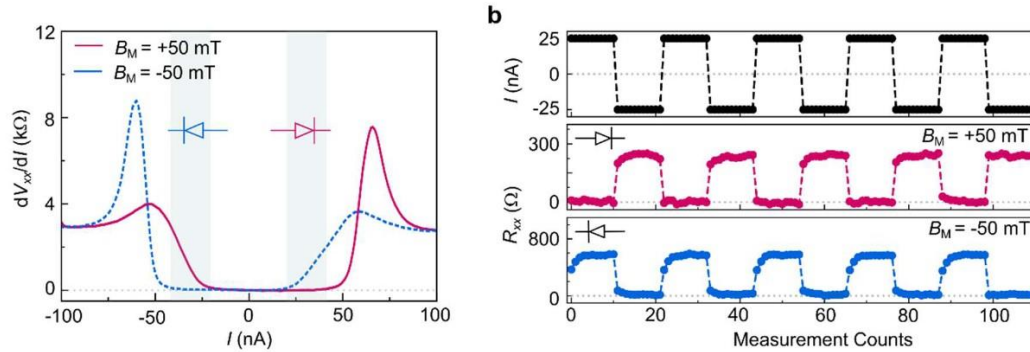
Supercurrent rectification and magnetochiral effects in symmetric Josephson junctions

Christian Baumgartner^{1,8}, Lorenz Fuchs^{1,8}, Andreas Costa², Simon Reinhardt³, Sergei Gronin^{3,4}, Geoffrey C. Gardner^{3,4}, Tyler Lindemann^{4,5}, Michael J. Manfra^{3,4,5,6,7}, Paulo E. Faria Junior², Denis Kochan², Jaroslav Fabian², Nicola Paradiso¹✉ and Christoph Strunk¹



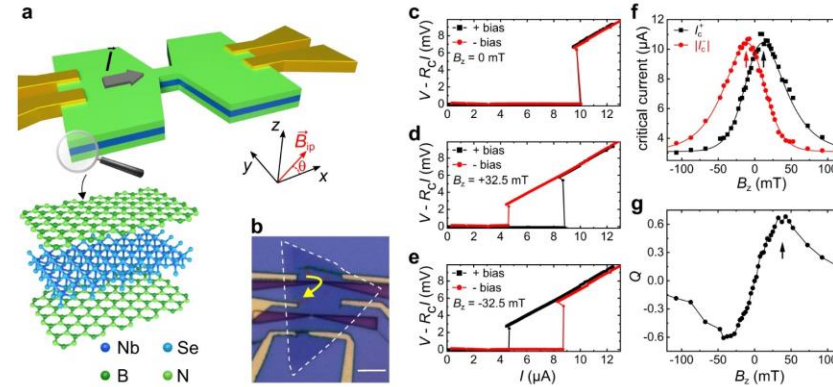
SDE in different systems

Twisted bilayer graphene



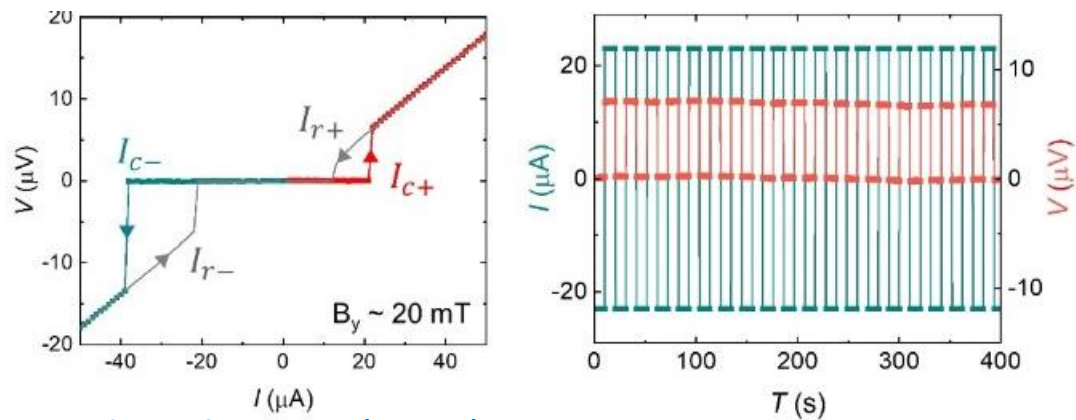
Diez-Merida et al., arXiv (2021)

Van der Waals materials

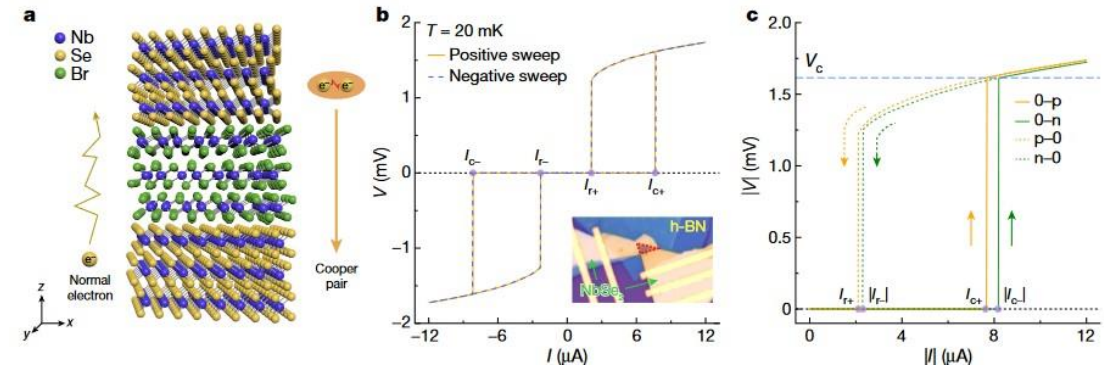


Bauriedl et al., *Nat Commun* **13**, 4266 (2022)

Topological semimetal (NiTe₂)



Pal et al., arXiv (2021)

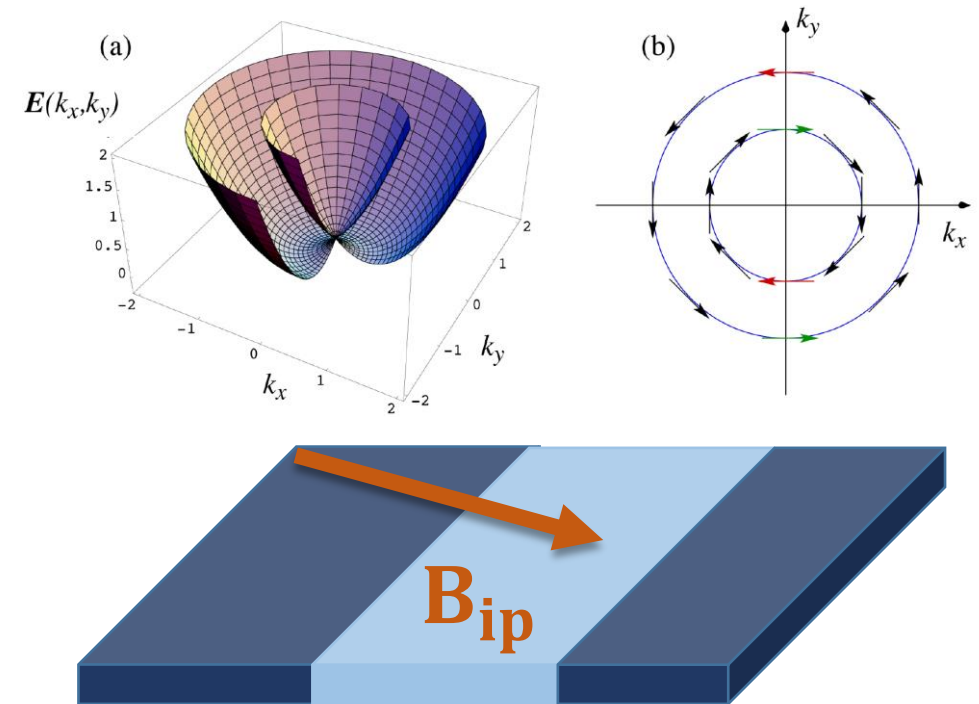


Wu et al., *Nature* **604**, 653–656 (2022)

Ingredients for intrinsic SDE

- Time-reversal breaking mechanism
- Broken inversion symmetry
- Robust superconducting phase

SNS junction + SOI + Zeeman field



Ideal candidate:
strong SOI and large effective g-factor

Outline of the talk

- ❖ Non-reciprocity in condensed matter systems
- ❖ **InSb nanoflags for advanced devices**
- ❖ Nanoflag-based Josephson junctions
- ❖ Josephson diode effect in InSb nanoflags

InSb: a convenient material

$$E_G = 0.23 \text{ eV}$$

→ mid-IR range devices

$$m^* \sim 0.018m_e$$

high-speed electronics

$$\mu_{bulk} = 7.7 \times 10^4 \text{ cm}^2/(\text{Vs})$$

→

$$g_{bulk}^* \sim 50$$

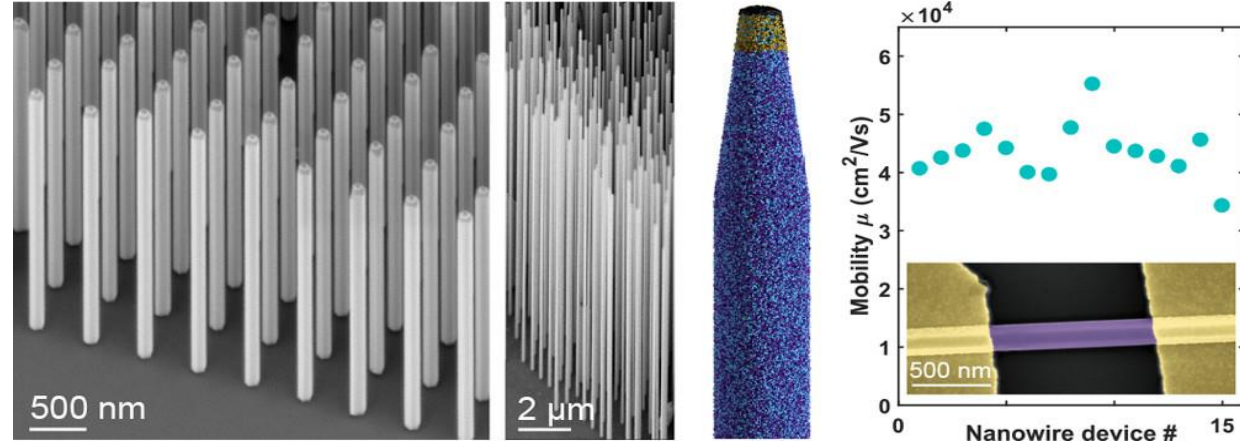
→

spintronics

not only for searching Majorana zero modes!

InSb nanostructures

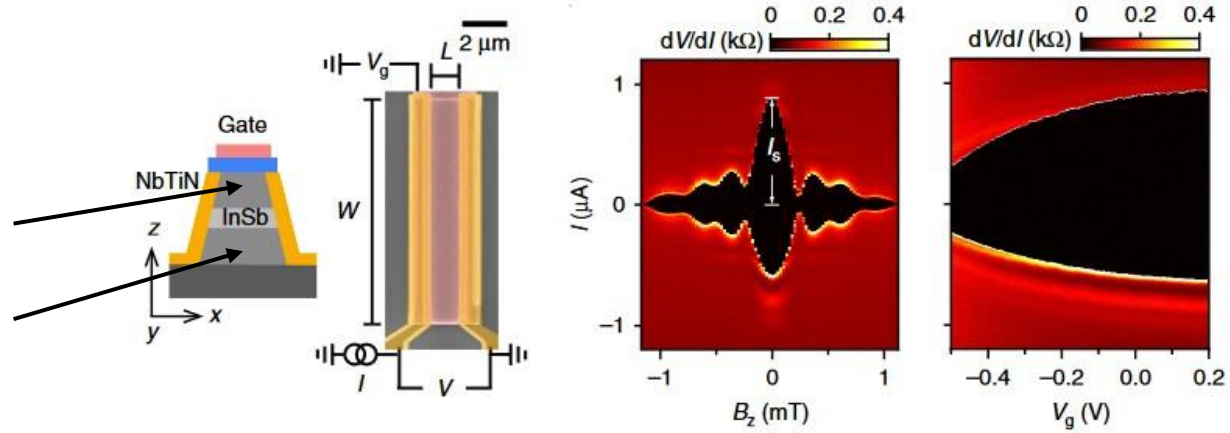
- InSb nanowires:



Nano Lett. 2019, 19, 6, 3575–3582

- InSb quantum wells:

Thick buffer layers are required due to lattice mismatch

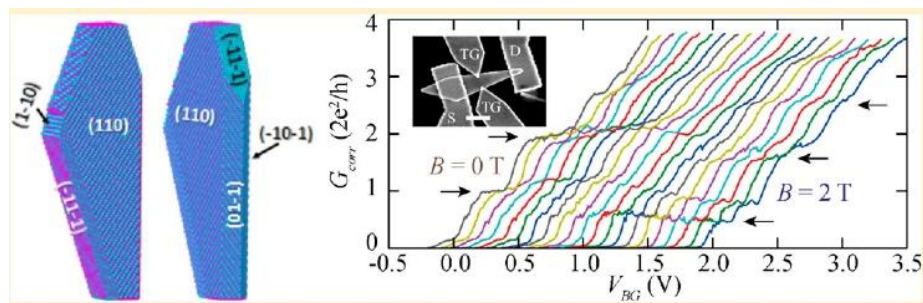


Nat Commun 10, 3764 (2019)

A novel approach: 2D nanoflags

Twin-Induced InSb Nanosails: A Convenient High Mobility Quantum System

María de la Mata,[†] Renaud Leturcq,^{*‡§} Sébastien R. Plissard,^{||} Chloé Rolland,[‡] César Magén,[⊥] Jordi Arbiol,^{*‡#} and Philippe Caroff^{*‡v}

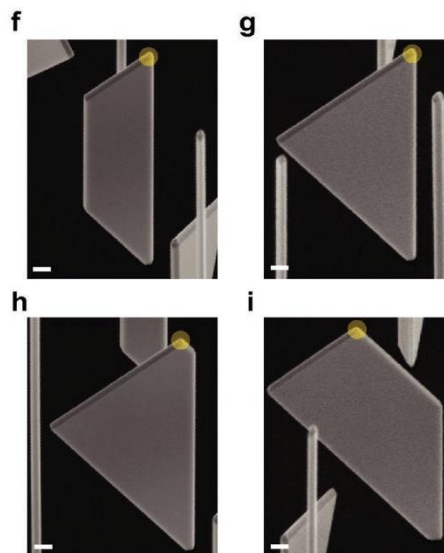


Nano Lett. 16 (2016) 825

Bottom-Up Grown 2D InSb Nanostructures

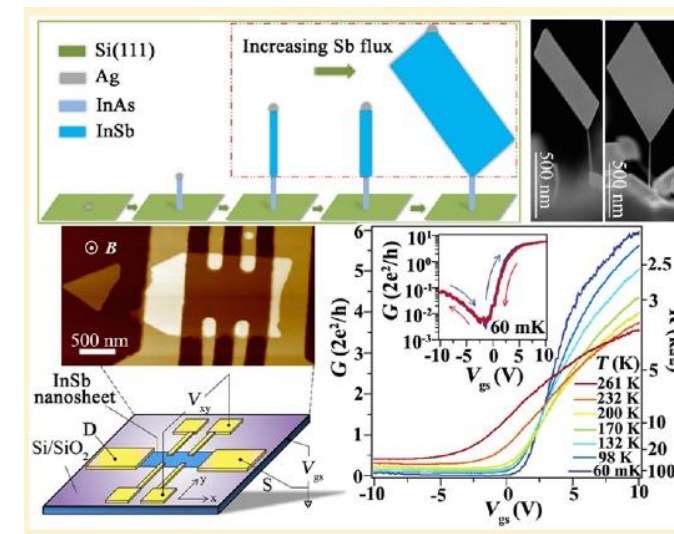
Sasa Gazibegovic,^{*} Ghada Badawy,^{*} Thijs L. J. Buckers, Philipp Leubner, Jie Shen, Folkert K. de Vries, Sebastian Koelling, Leo P. Kouwenhoven, Marcel A. Verheijen, and Erik P. A. M. Bakkers

Adv. Mater. 31 (2019) 1808181



Free-Standing Two-Dimensional Single-Crystalline InSb Nanosheets

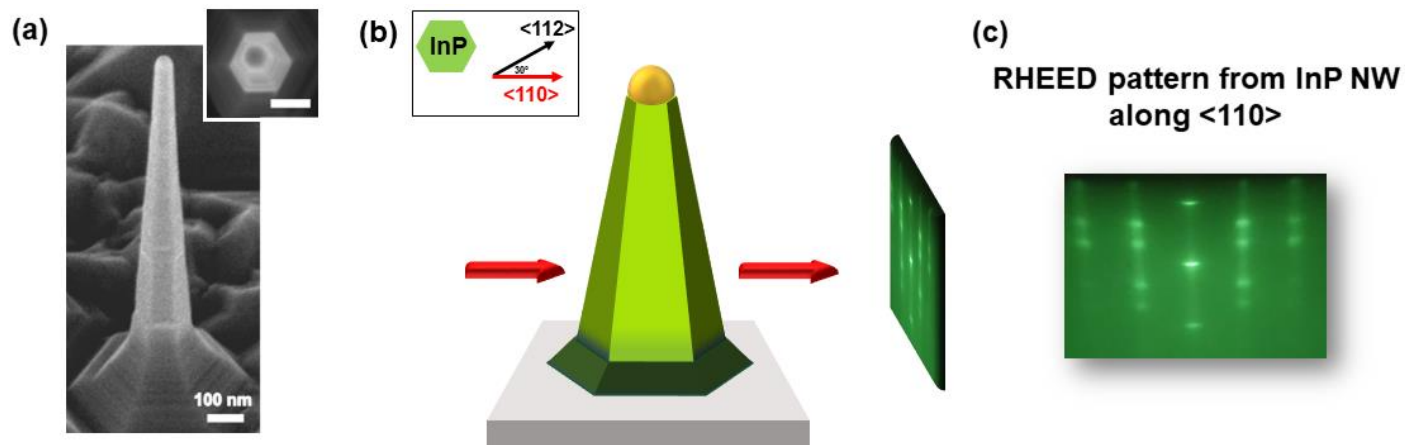
D. Pan,[†] D. X. Fan,[‡] N. Kang,[‡] J. H. Zhi,[‡] X. Z. Yu,[†] H. Q. Xu,^{*‡} and J. H. Zhao^{*‡}



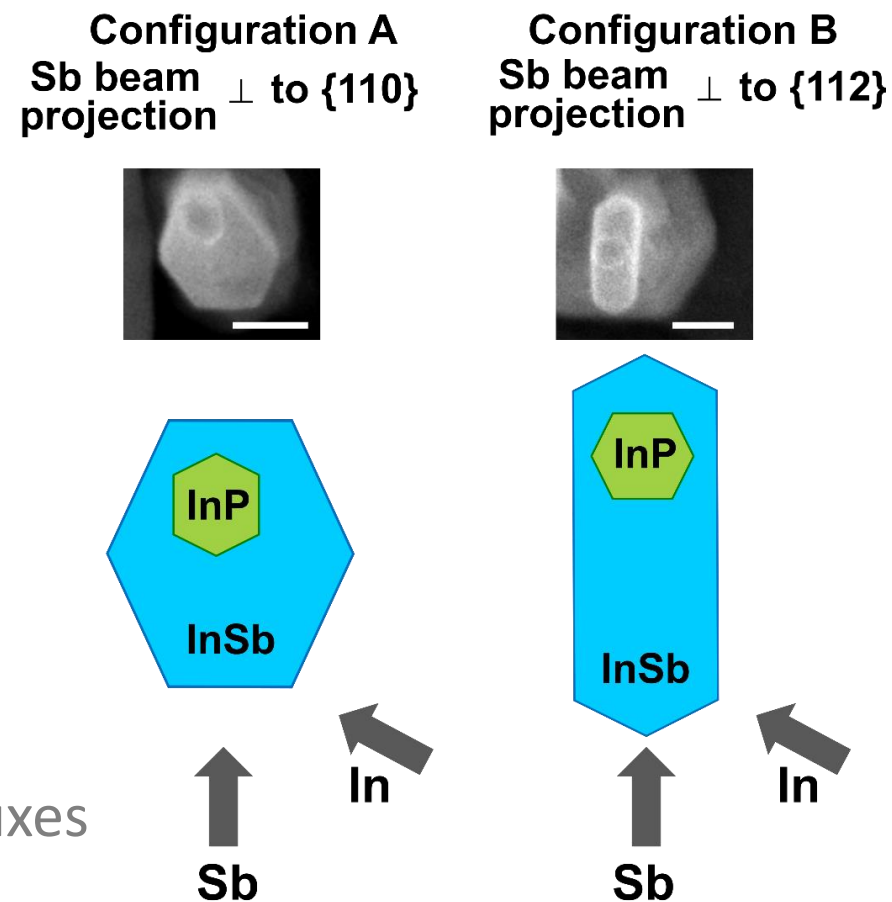
Nano Lett. 16 (2016) 834

From nanowires (1D) to nanoflags (2D)

tapered InP nanowires are used as *stems*



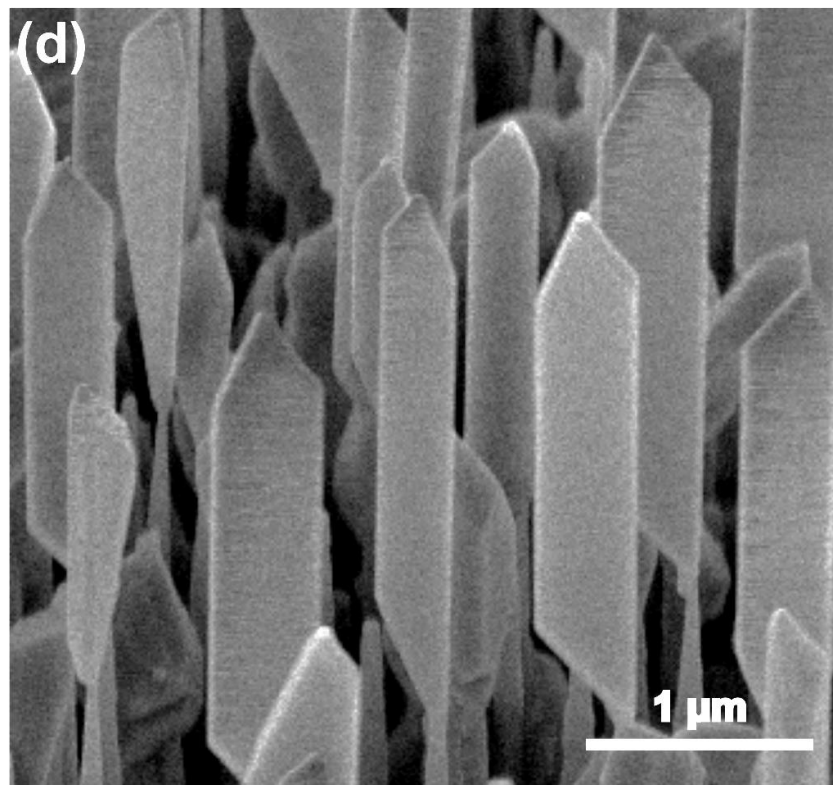
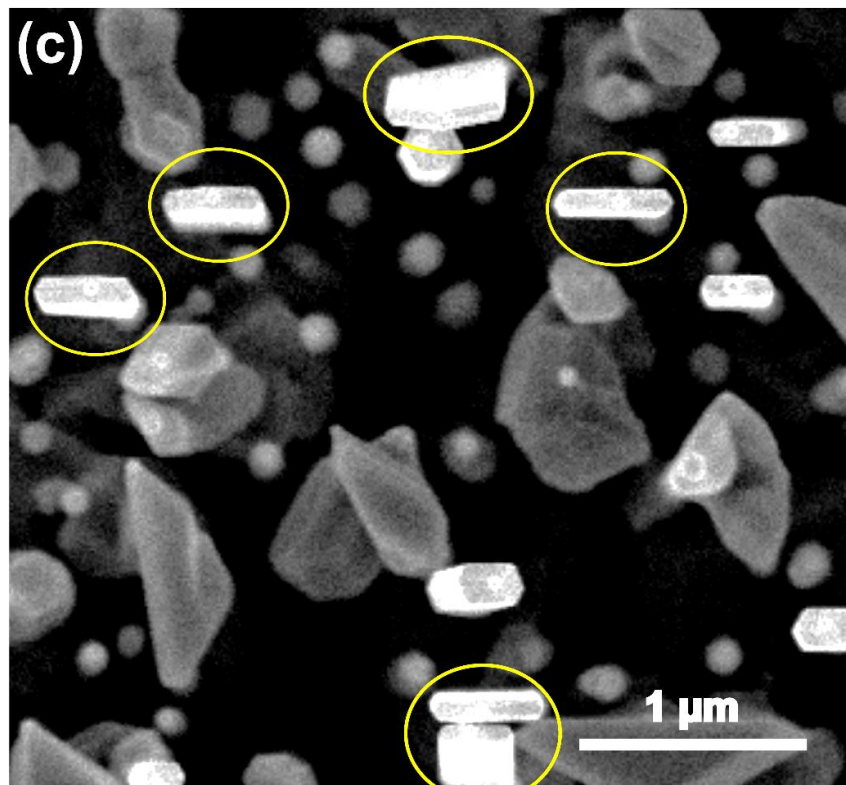
the 2D shape is obtained with directional fluxes



Growth of InSb nanoflags via CBE



Isha Verma

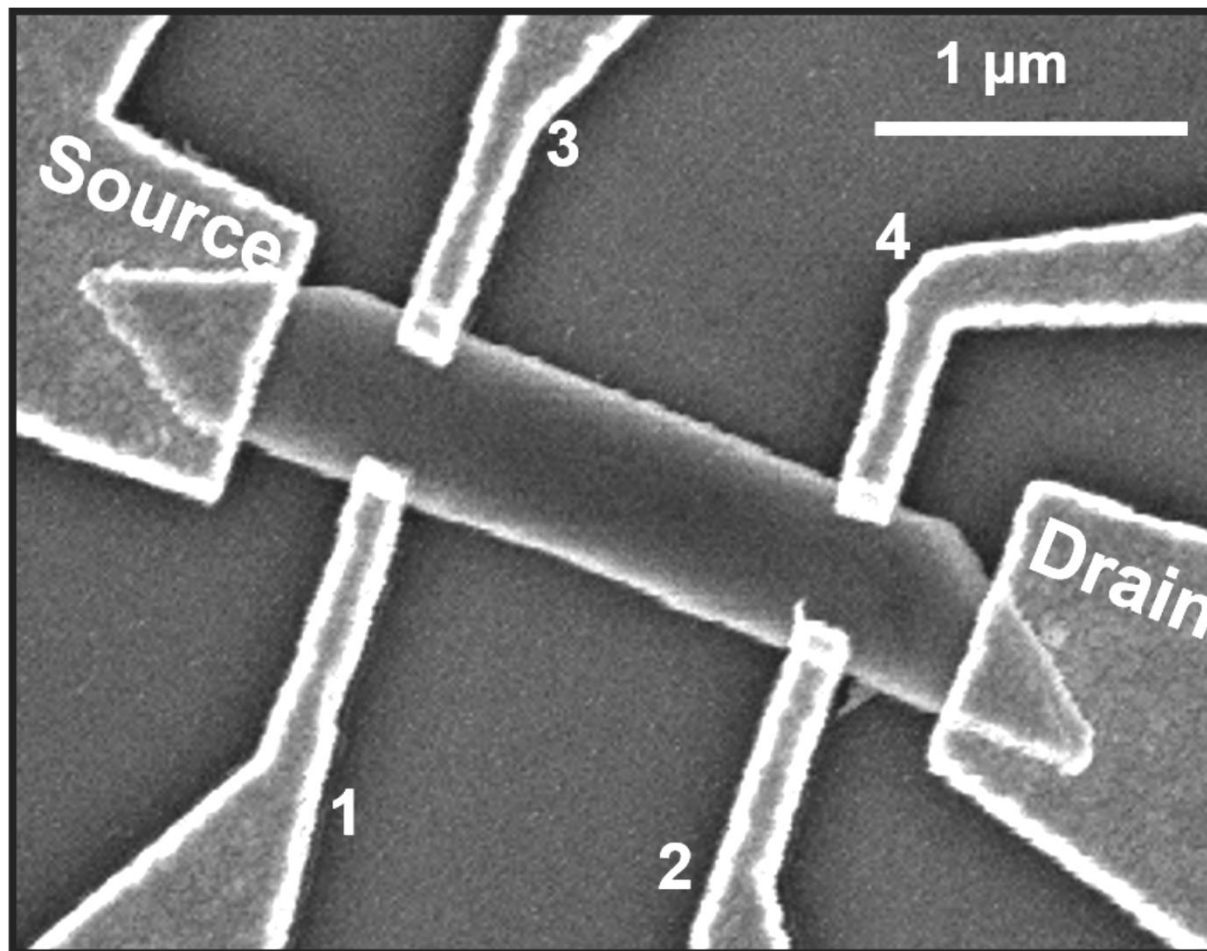


- ZB lattice
- defect-free crystal

Nanoflags:

- $t \sim 100 \text{ nm}$
- $W \sim 500 \text{ nm}$
- $L \sim 2 \mu\text{m}$

Nanoflag in Hall bar geometry



Sample geometry:

- $t \sim 100$ nm
- $W \sim 325$ nm
- $L \sim 1.5$ μm

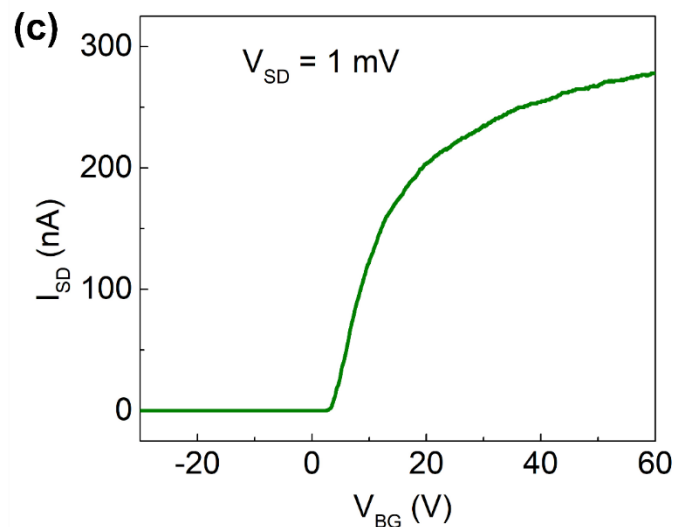
Leads:

Ti/Au 10/190 nm

Substrate:

Si/SiO₂

InSb NF characterization @ T= 4.2 K



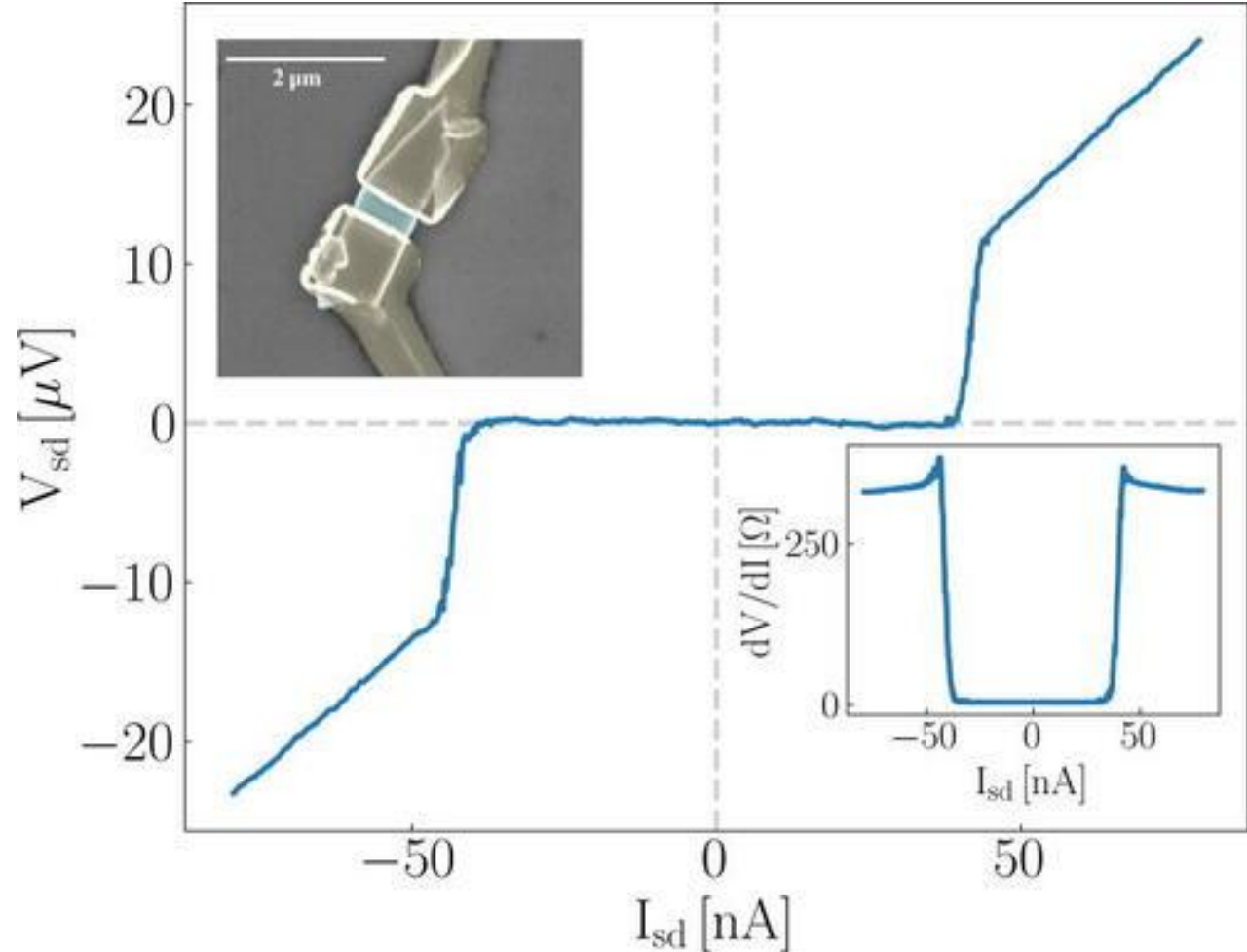
Field-effect :

n-type conduction

$$\mu_{FE} = 2.8 \times 10^4 \text{ cm}^2/\text{Vs}$$

Outline of the talk

- ❖ Non-reciprocity in condensed matter systems
- ❖ InSb nanoflags for advanced devices
- ❖ **Nanoflag-based Josephson junctions**
- ❖ Josephson diode effect in InSb nanoflags



Deposition of superconducting leads
150/10 nm Nb/Ti

↓
Super-normal-super junction

$$T_c = 8.44 \text{ K} \Rightarrow \Delta = 1.28 \text{ meV}$$

□ $\lambda_{MFP} = 500 \text{ nm}$

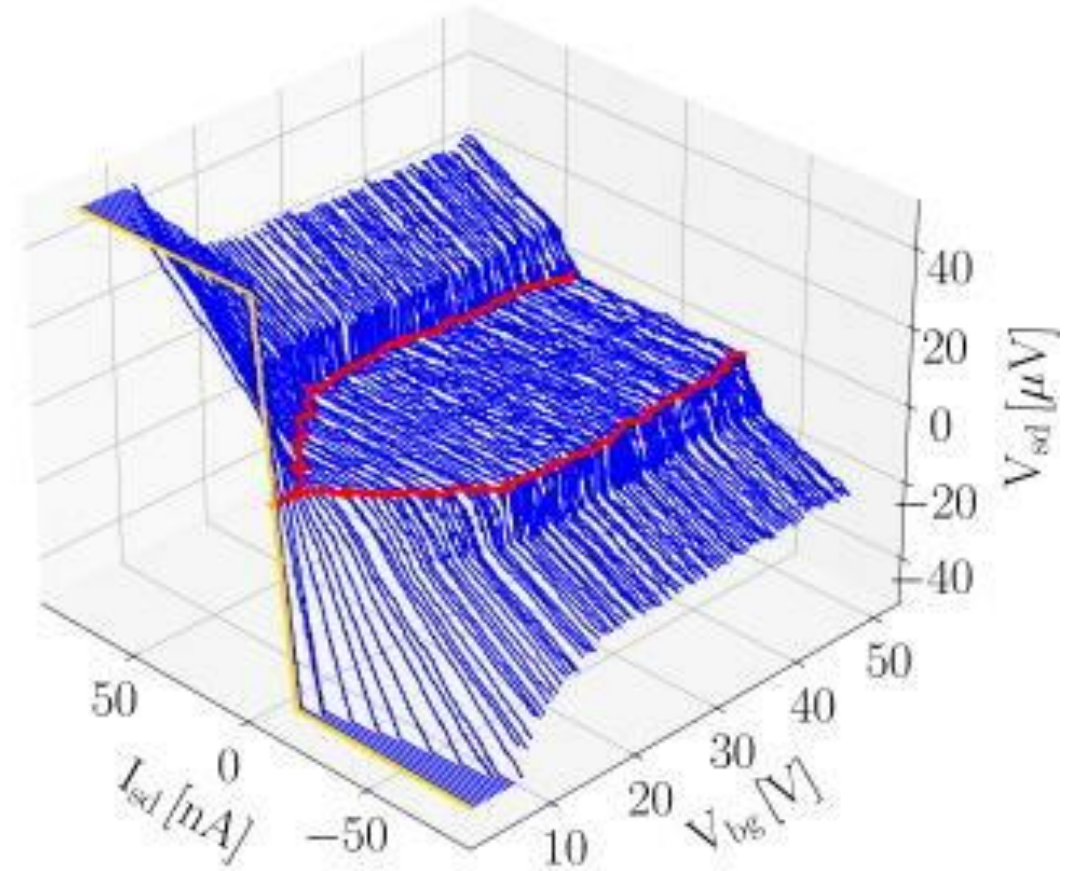
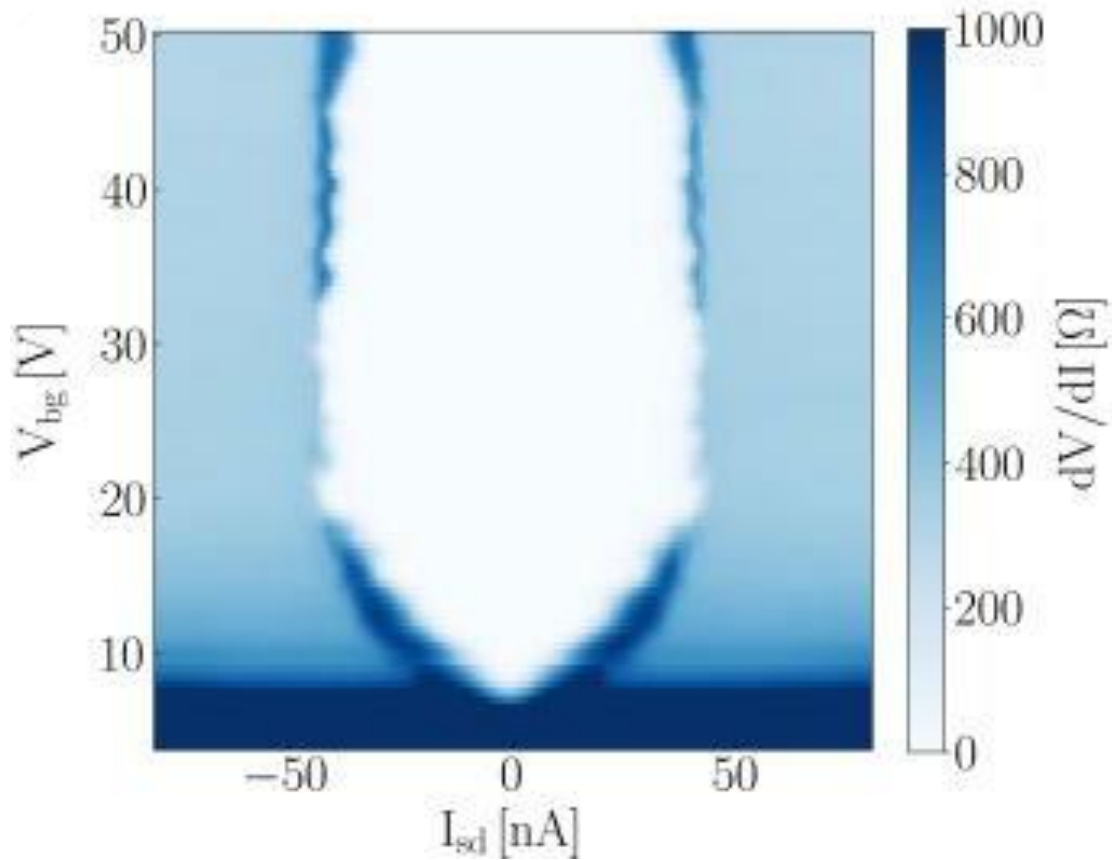
□ $L = 200 \text{ nm}$

□ $\xi_{SC} = \hbar v_F / \Delta \sim 750 \text{ nm}$

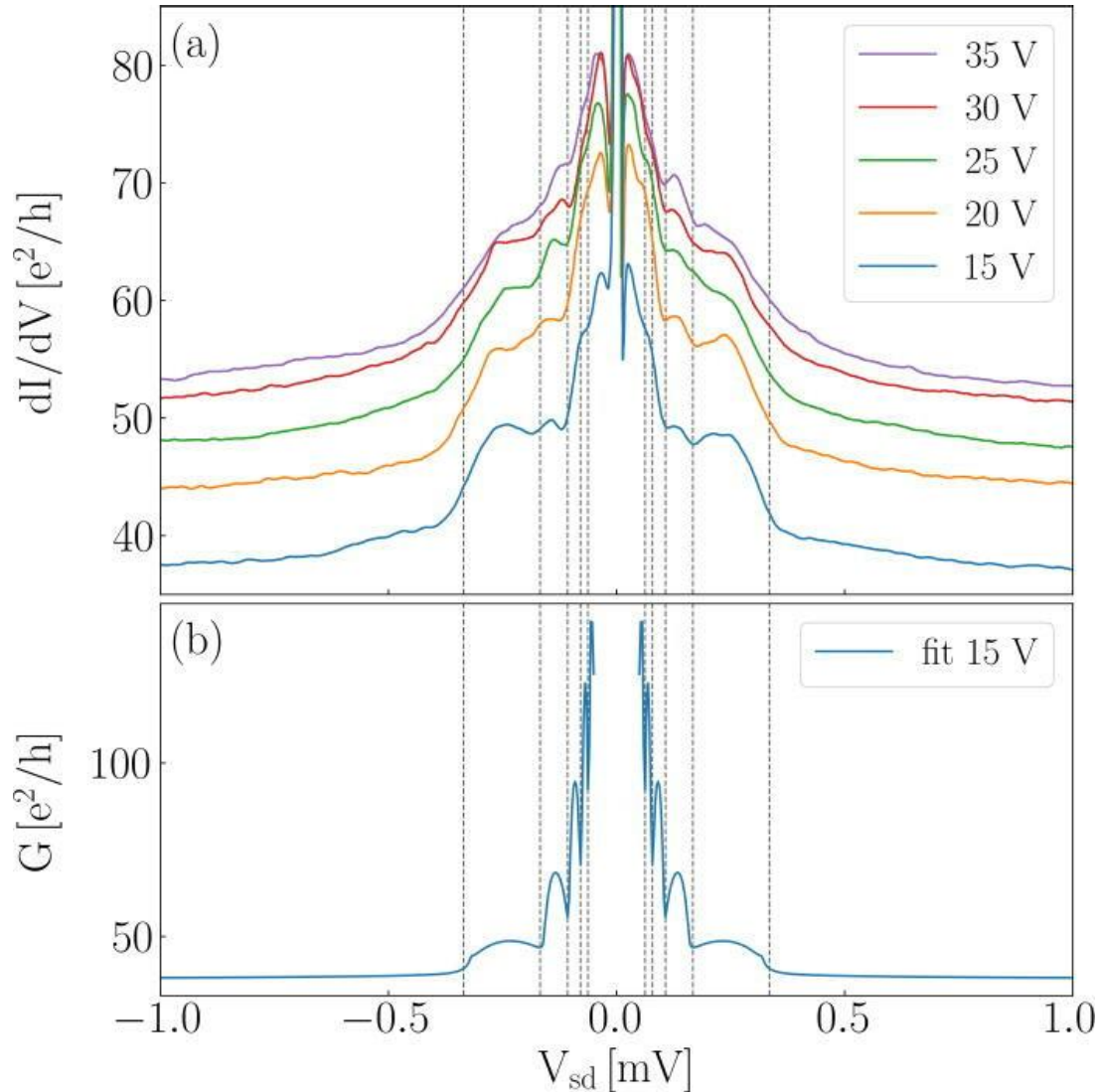
BALLISTIC REGIME

SHORT
JUNCTION

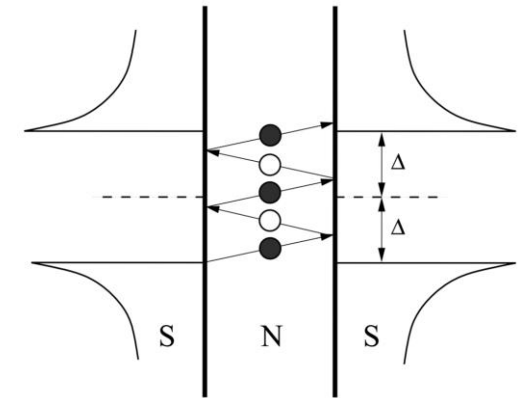
Gate-controlled supercurrent



Multiple Andreev reflections



Matching condition for
 $neV_n = 2\Delta^*$



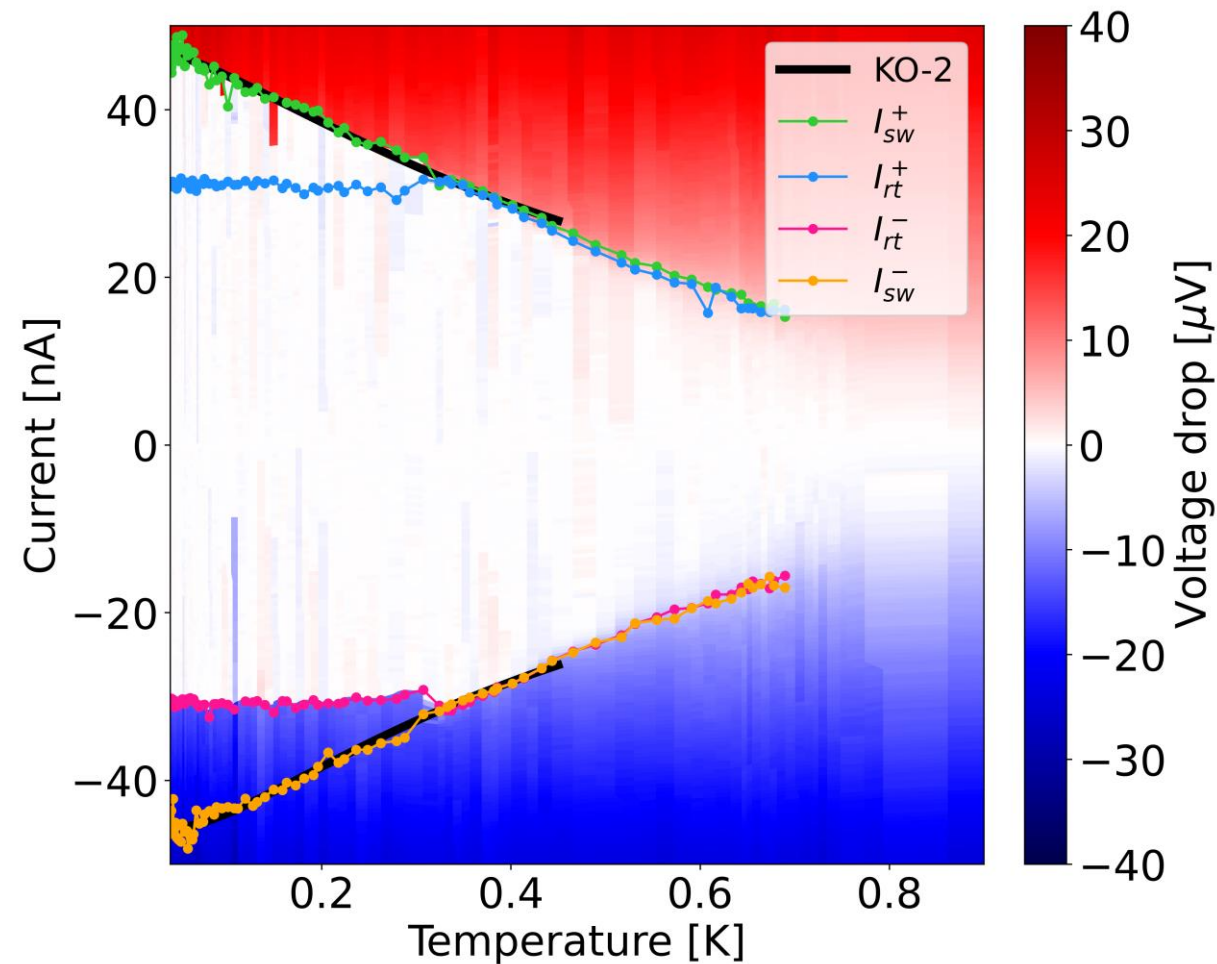
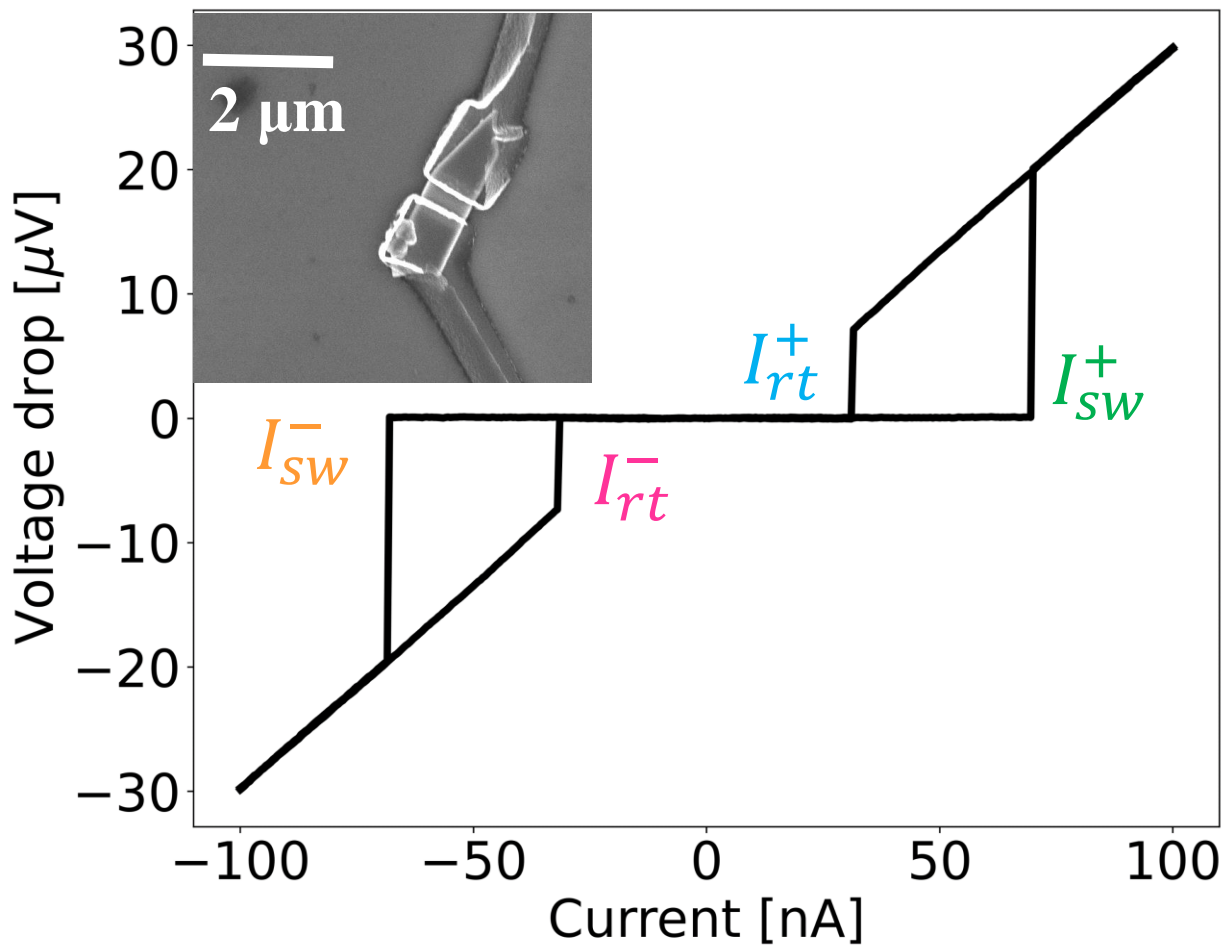
The model:

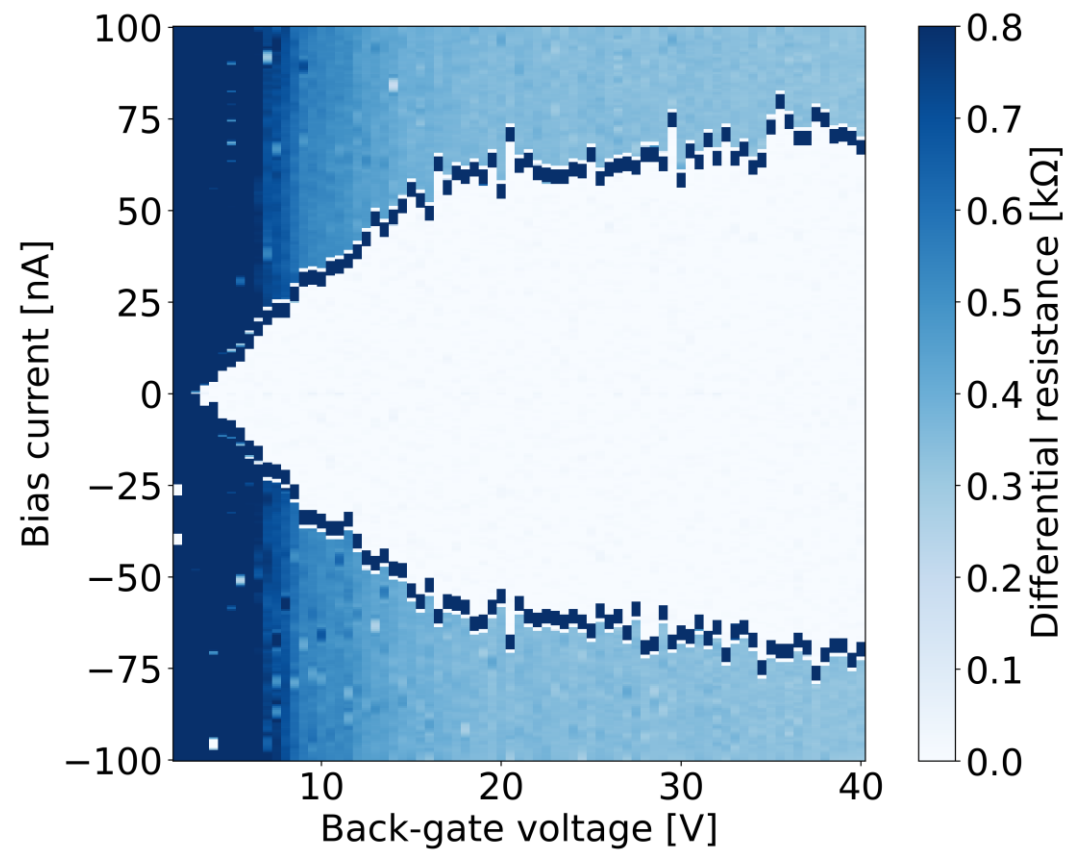
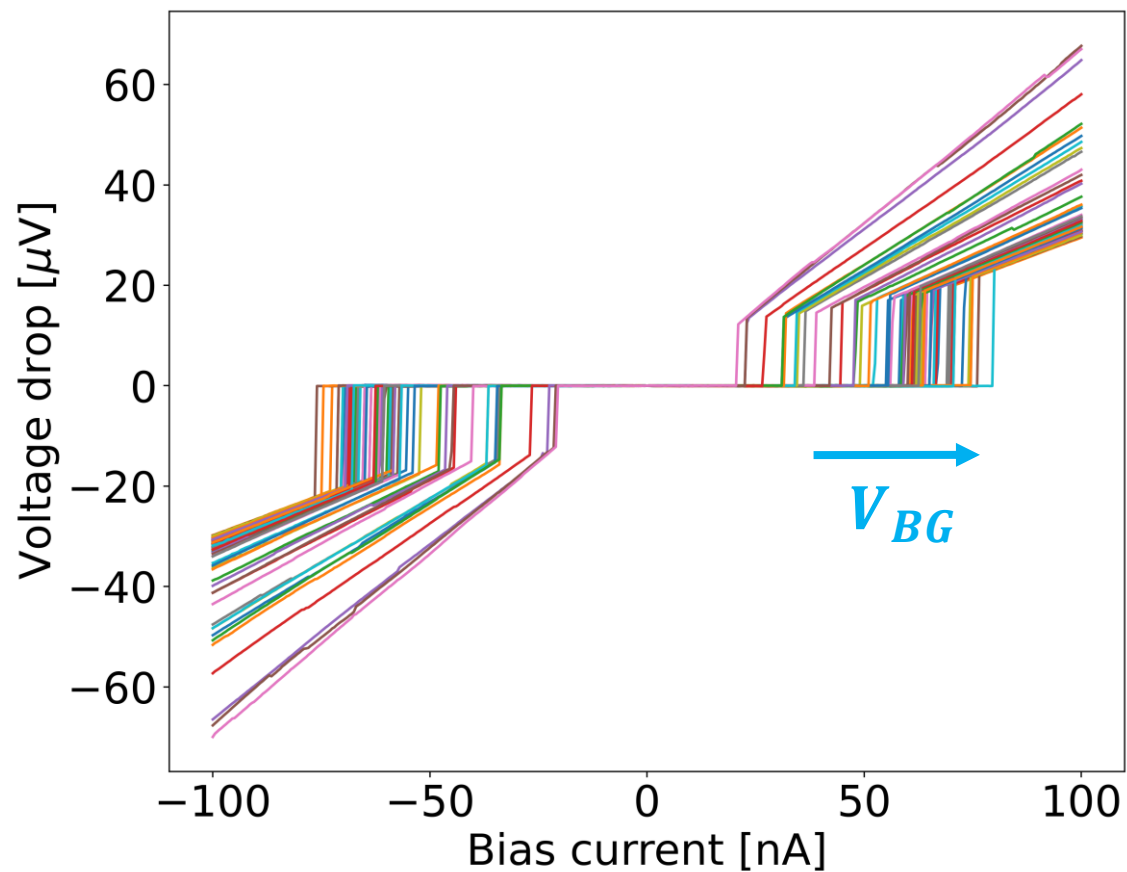
Best fit:

- M families of modes: $i=1, \dots, M$ 1
- N_i transport modes 40 (V_{BG})
- τ_i transmission coefficient 0.94
- Δ^* = superconducting gap 160 μeV

T= 250 mK

IV characteristics vs. temperature

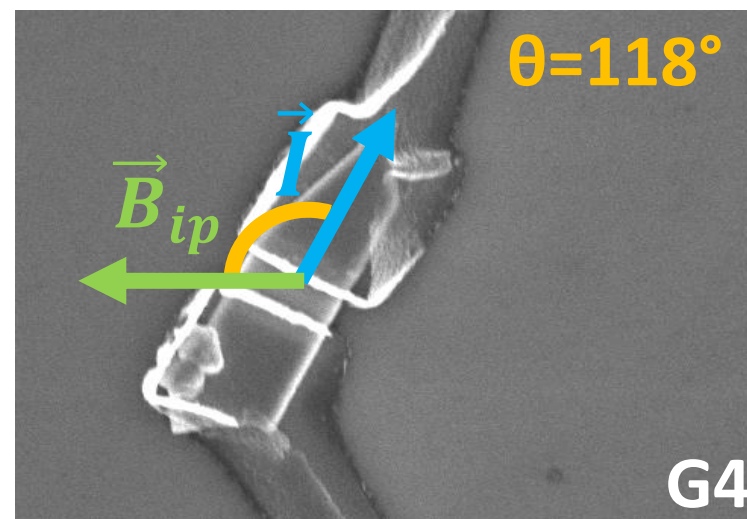
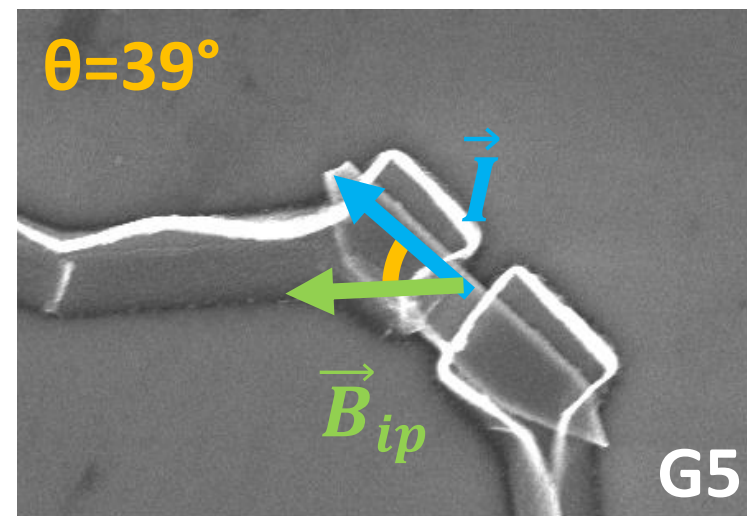
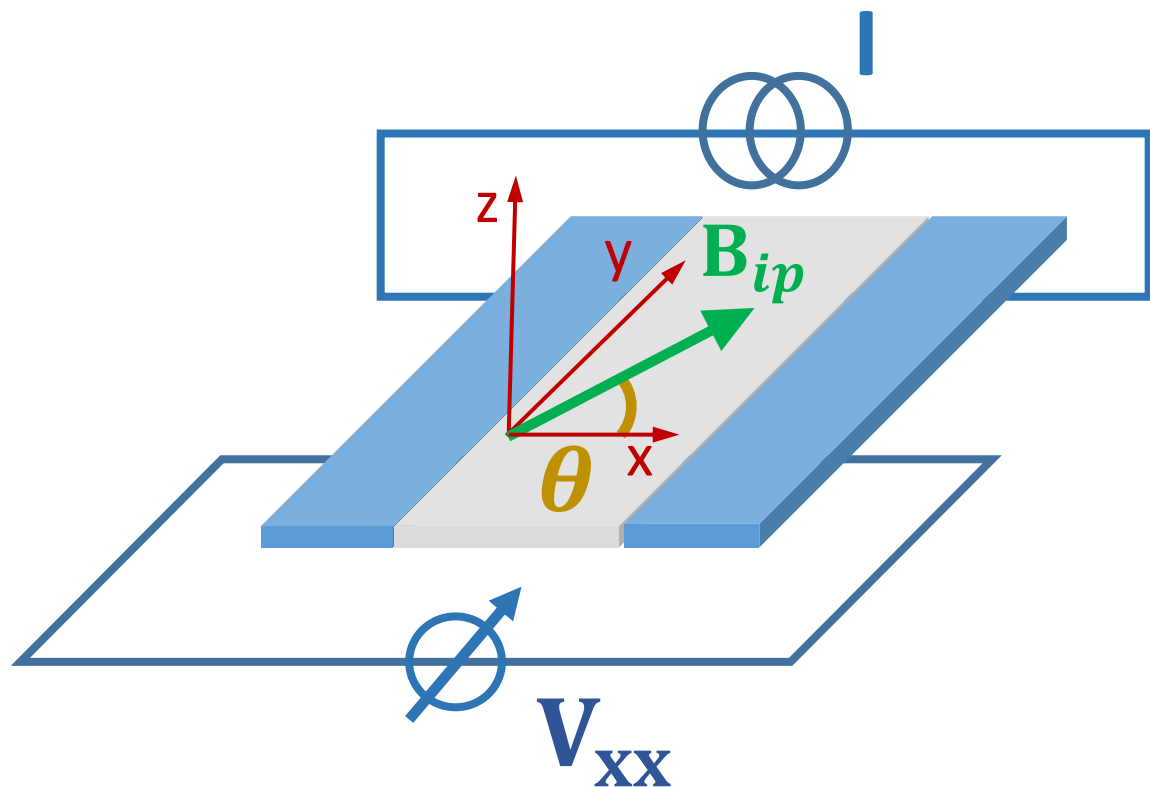




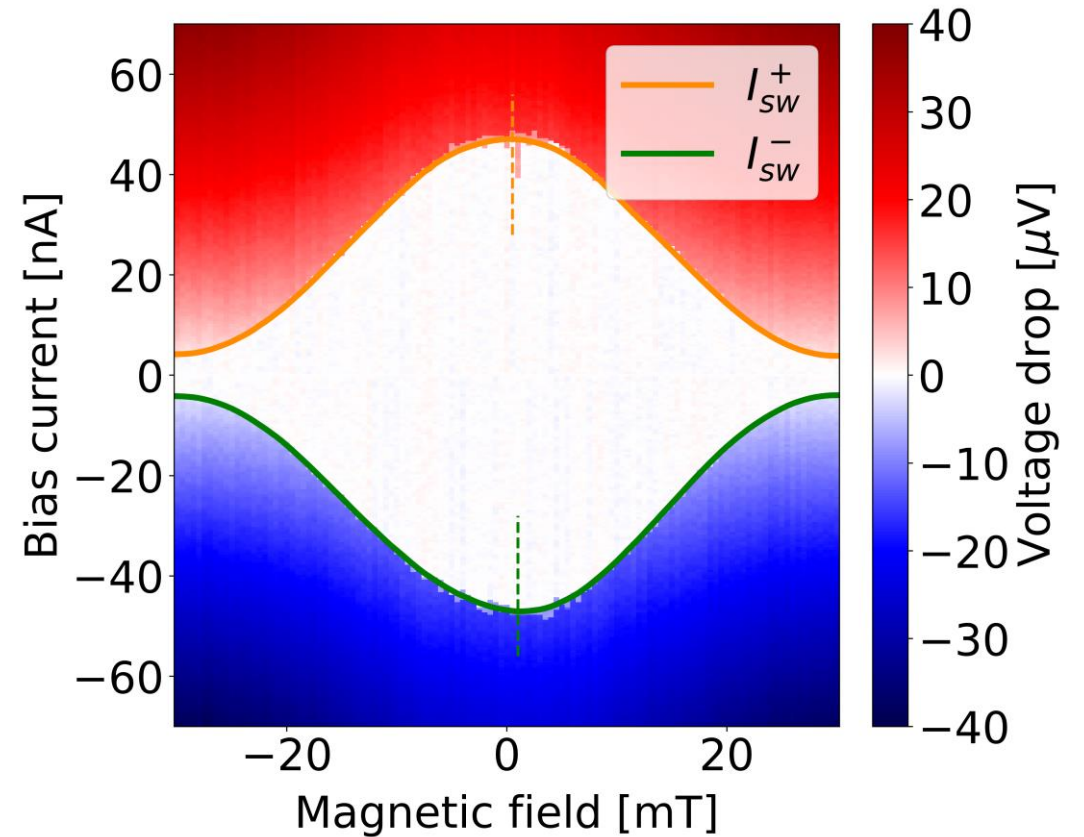
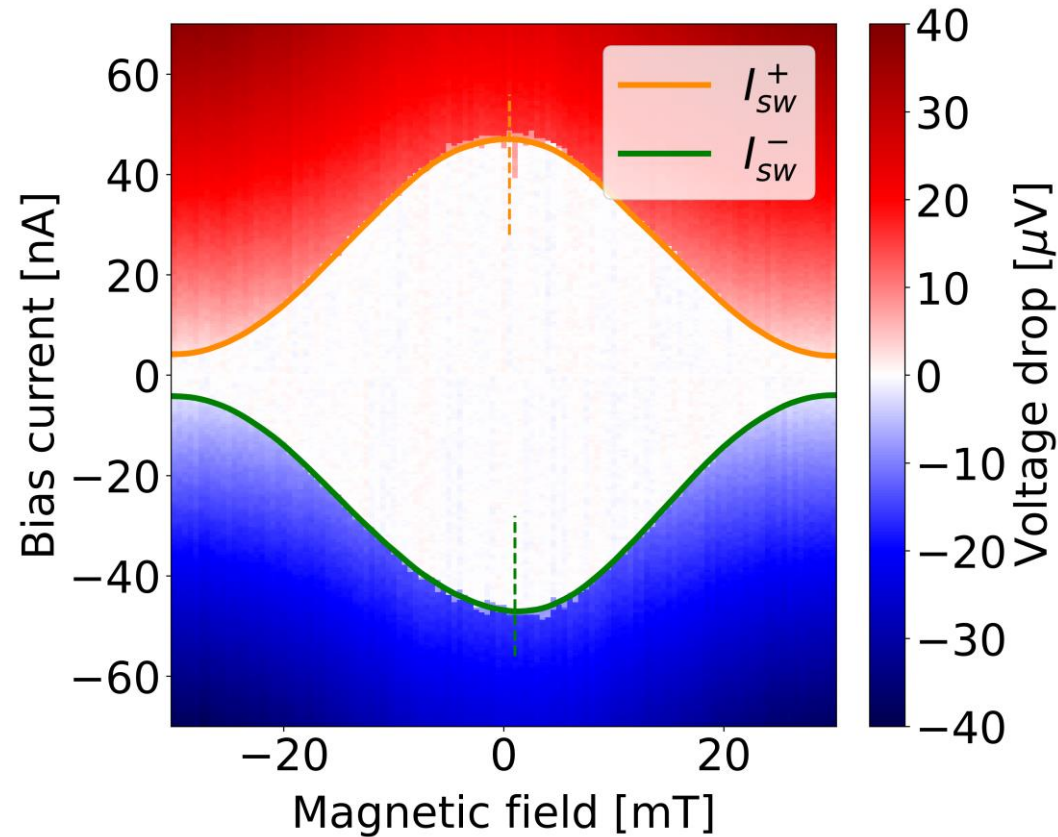
Outline of the talk

- ❖ Non-reciprocity in condensed matter systems
- ❖ InSb nanoflags for advanced devices
- ❖ Nanoflag-based Josephson junctions
- ❖ **Josephson diode effect in InSb nanoflags**

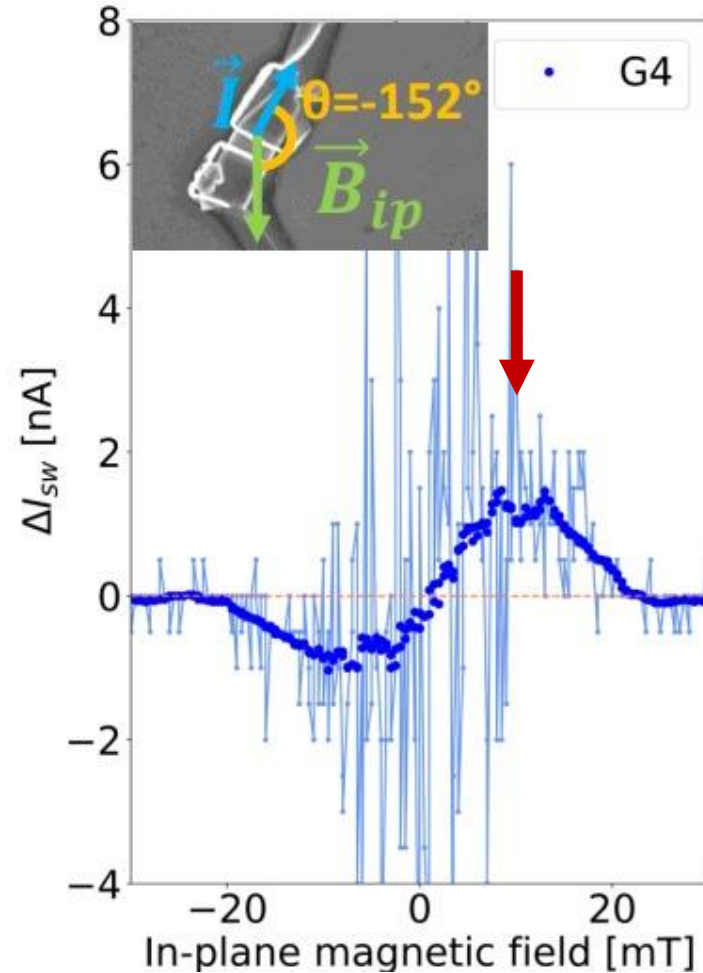
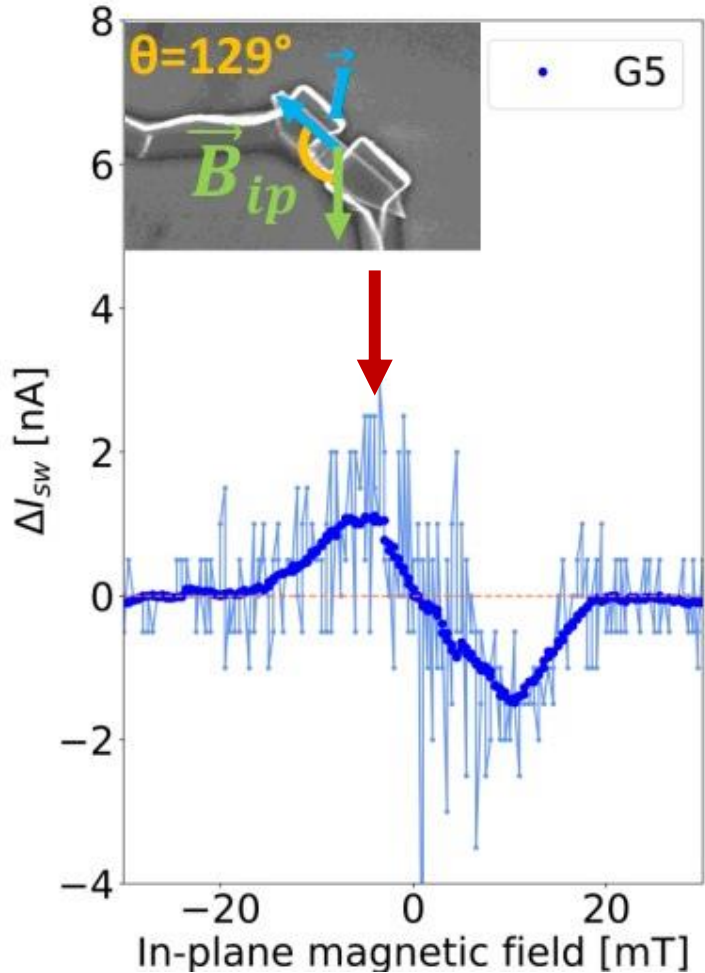
Design of the experiment



In-plane magnetic field effect



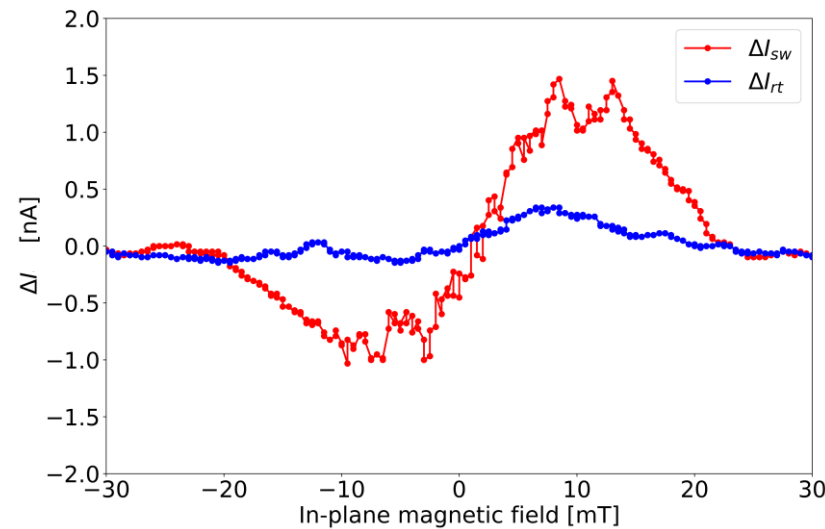
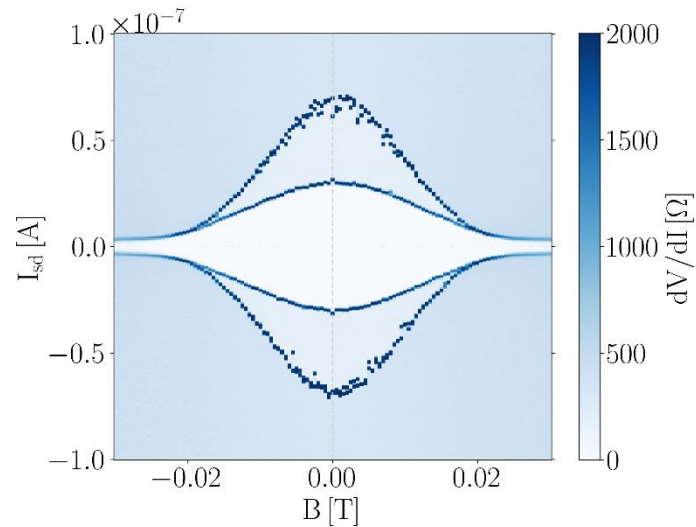
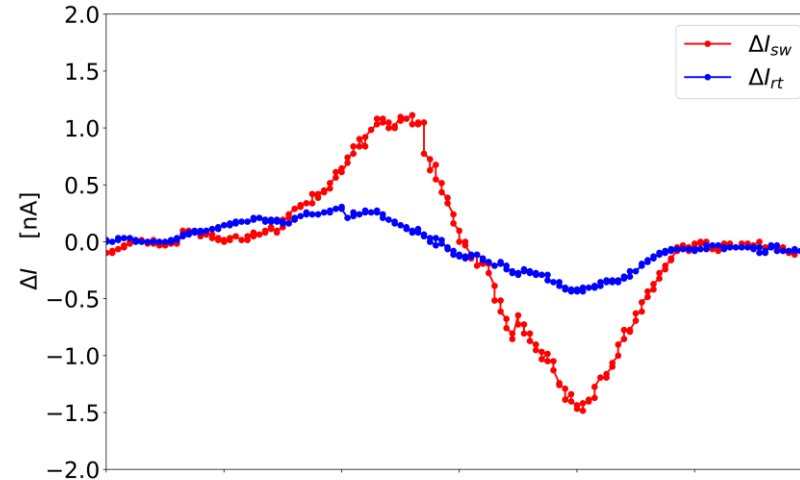
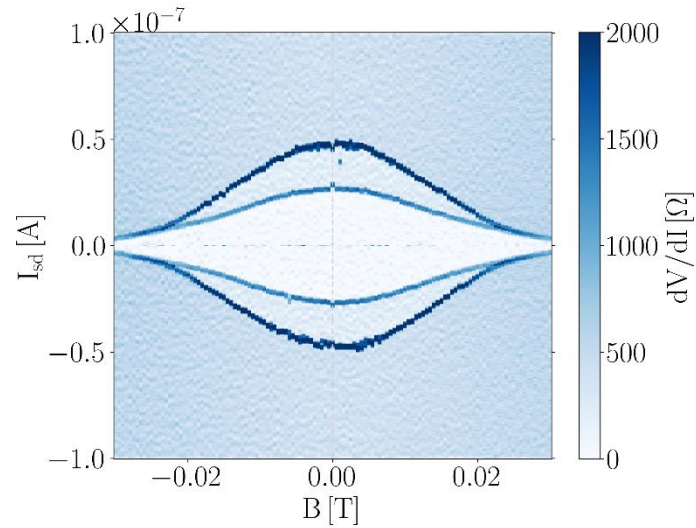
Switching current asymmetry



Main features:

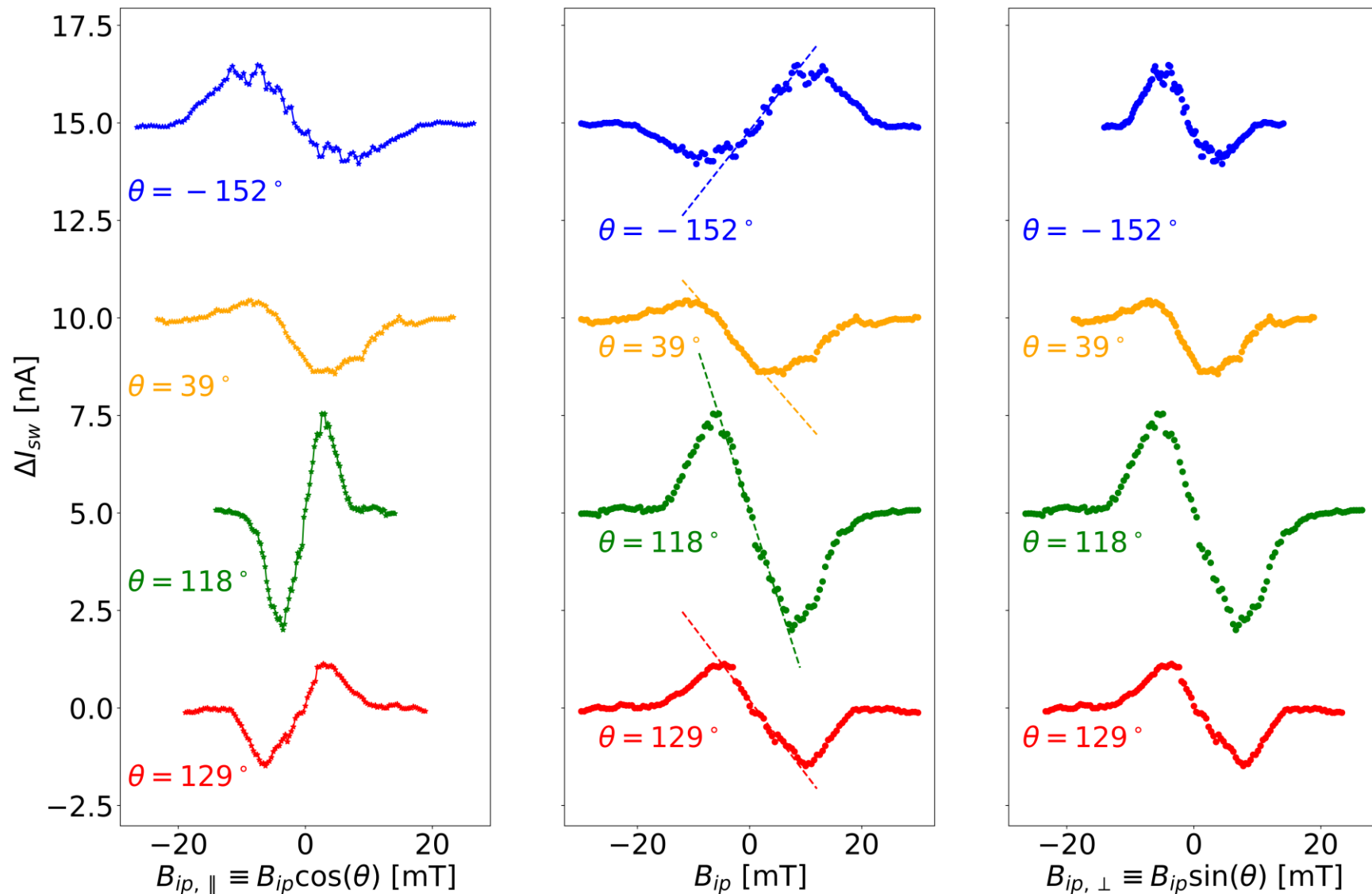
- antisymmetric behavior
- linear around $B = 0$
- rounded maximum
- suppression at $B \gtrsim 20$ mT
- θ -dependent polarity

Retrapping current asymmetry



Different magnitude:
remappable on
T-dependence

Dependence on the angle

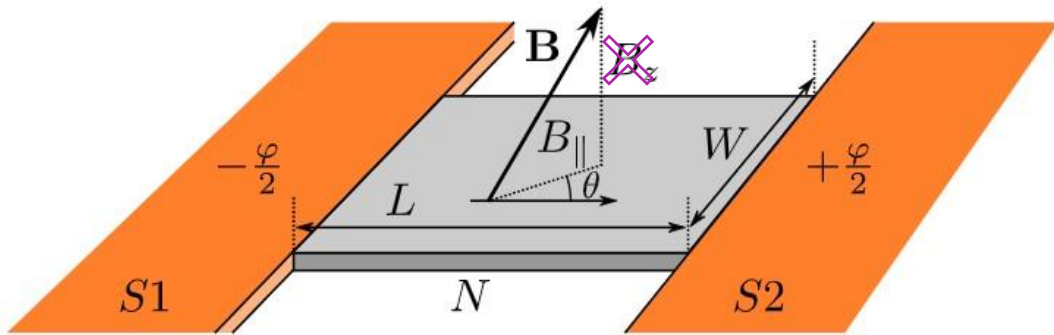


An educated guess:

$$\Delta I_{sw} \propto |\mathbf{B} \times \mathbf{I}|$$

Symmetry-breaking mechanism

How to break the equivalence $I_c^+ = I_c^-$?



$$H = H_0 + H_{SOI}(\alpha, \beta) + H_Z + H_S$$

α : Rashba SOI

β : Dresselhaus SOI

$$UH(\varphi)U^\dagger = H(-\varphi)$$

U

Broken by

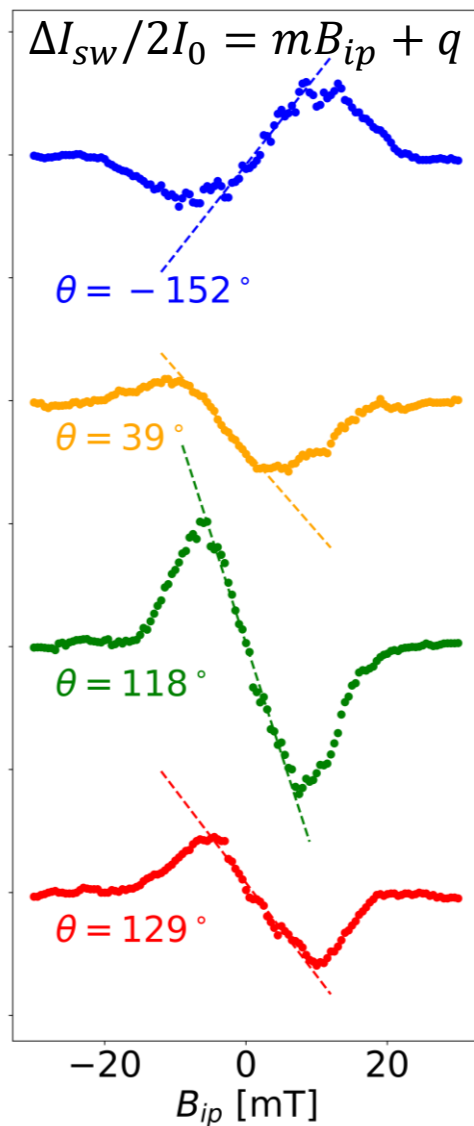
$\mathcal{P}_y \mathcal{P}_x$	α, β, V_x, V_y	✗	✗
$\sigma_z \mathcal{P}_y \mathcal{P}_x$	B_x, B_y, V_x, V_y	✗	✗
$\sigma_x \mathcal{P}_y T$	B_x, α, V_y	✗	✗
$\sigma_y \mathcal{P}_y T$	B_y, β, V_y	✗	✗

$$\alpha + B_{ip,\perp}$$

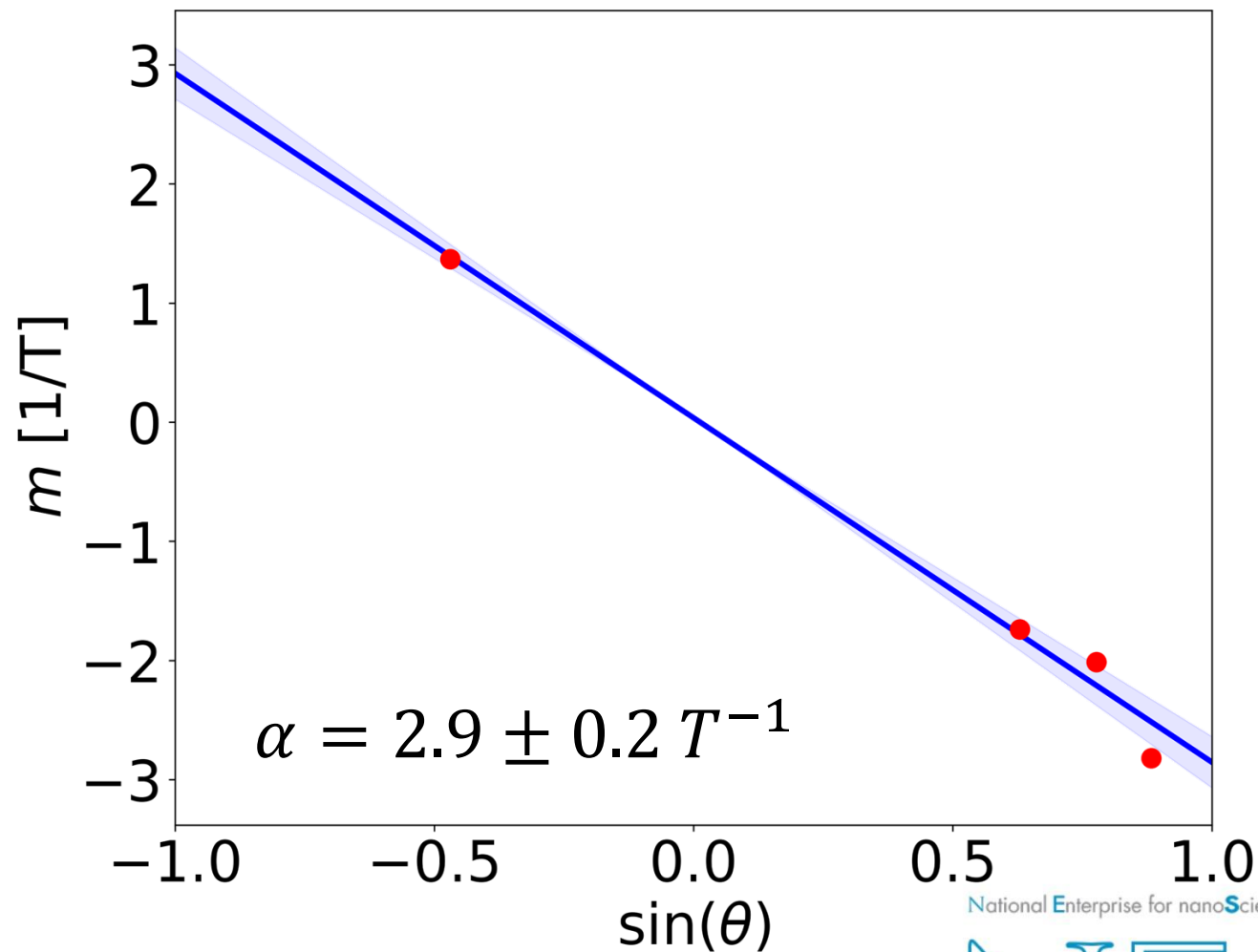
$$\beta + B_{ip,\parallel}$$

Rasmussen et al., *Physical Review B*, 93(15) (2016)

Dominant Rashba-type SOI



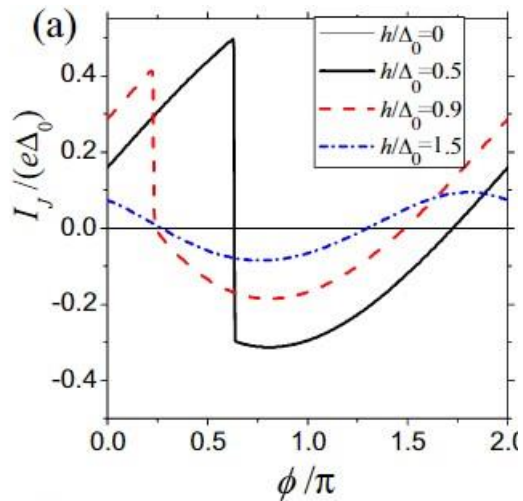
$$m = \alpha \sin(\theta) + \cancel{\beta} \Rightarrow \eta \propto B_{ip,\perp}$$



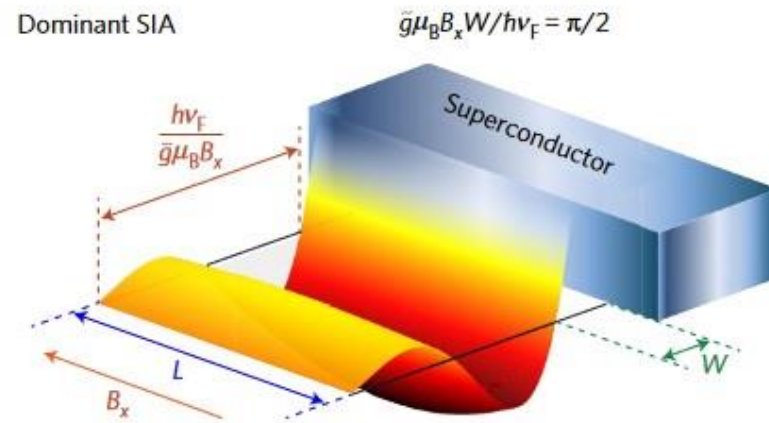
Finite momentum superconductivity

Strong RSOC + s-wave SC + $B_{ip,\perp}$: $qv_F = g^* \mu_B B_{ip,\perp}$

anomalous phase shift



spatial modulation of Δ^*



Josephson diode effect
in ballistic junctions

$$\eta \equiv \frac{I_c^+ - |I_c^-|}{I_c^+ + |I_c^-|} = \frac{2qv_F}{\pi\Delta^*}$$

$$\alpha_{th}(\text{InSb NF}) \sim 8.5 T^{-1}$$

Dolcini et al., *PRB* 92(3) (2015)

Hart et al., *Nature Physics*, 13(1), 87–93(2017)

Davydova et al., *Sci. Adv* (Vol. 8) (2022)

The CPR point of view

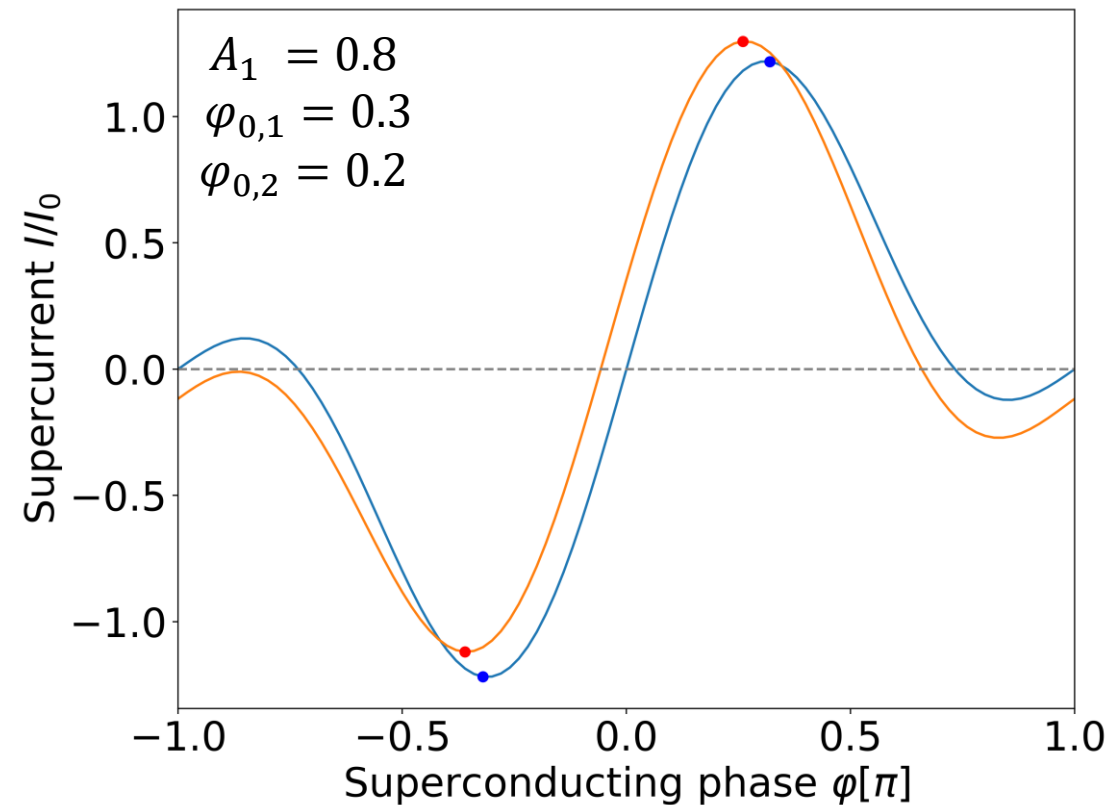
Josephson diode effect : ballistic junctions + anomalous CPR

➤ Skewed CPR

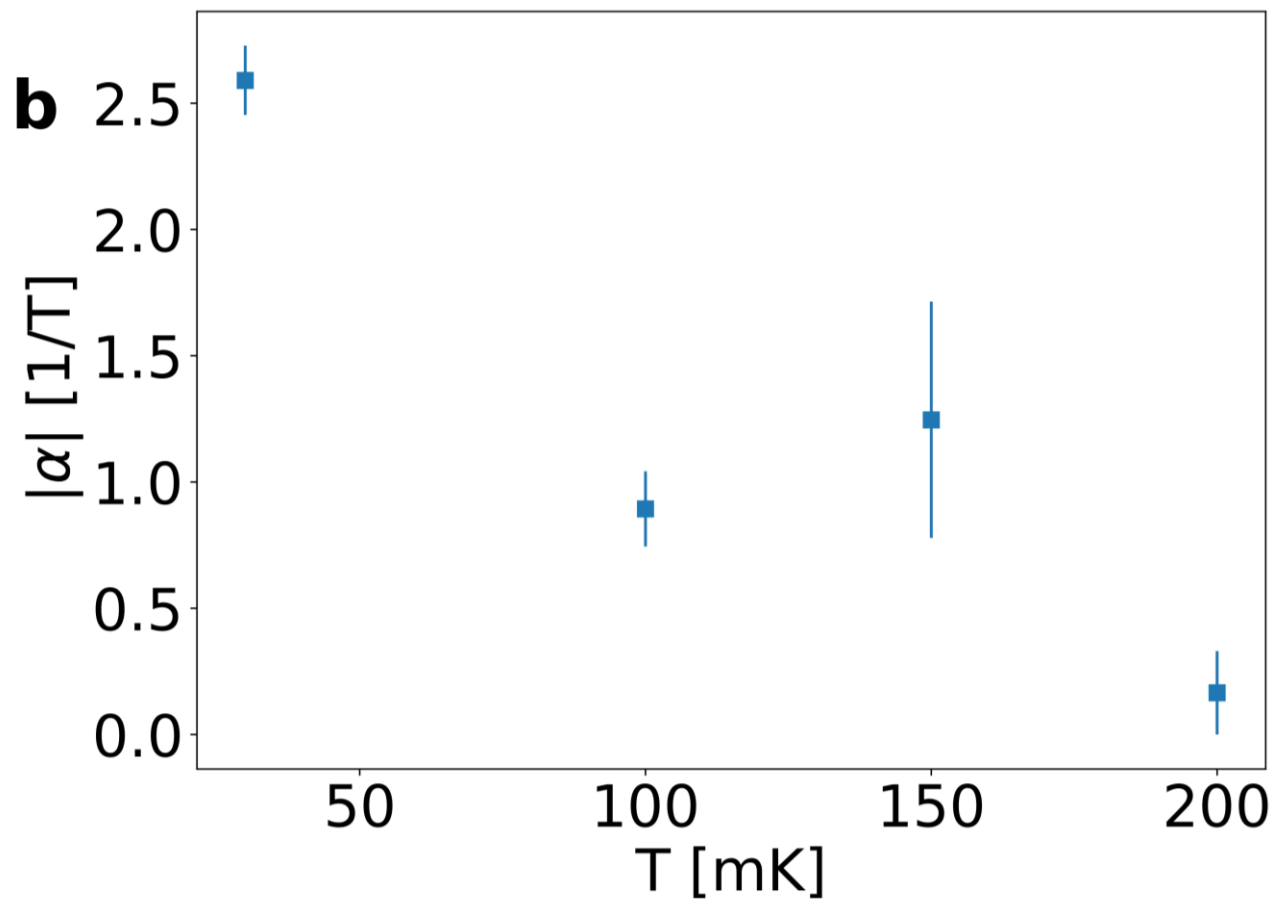
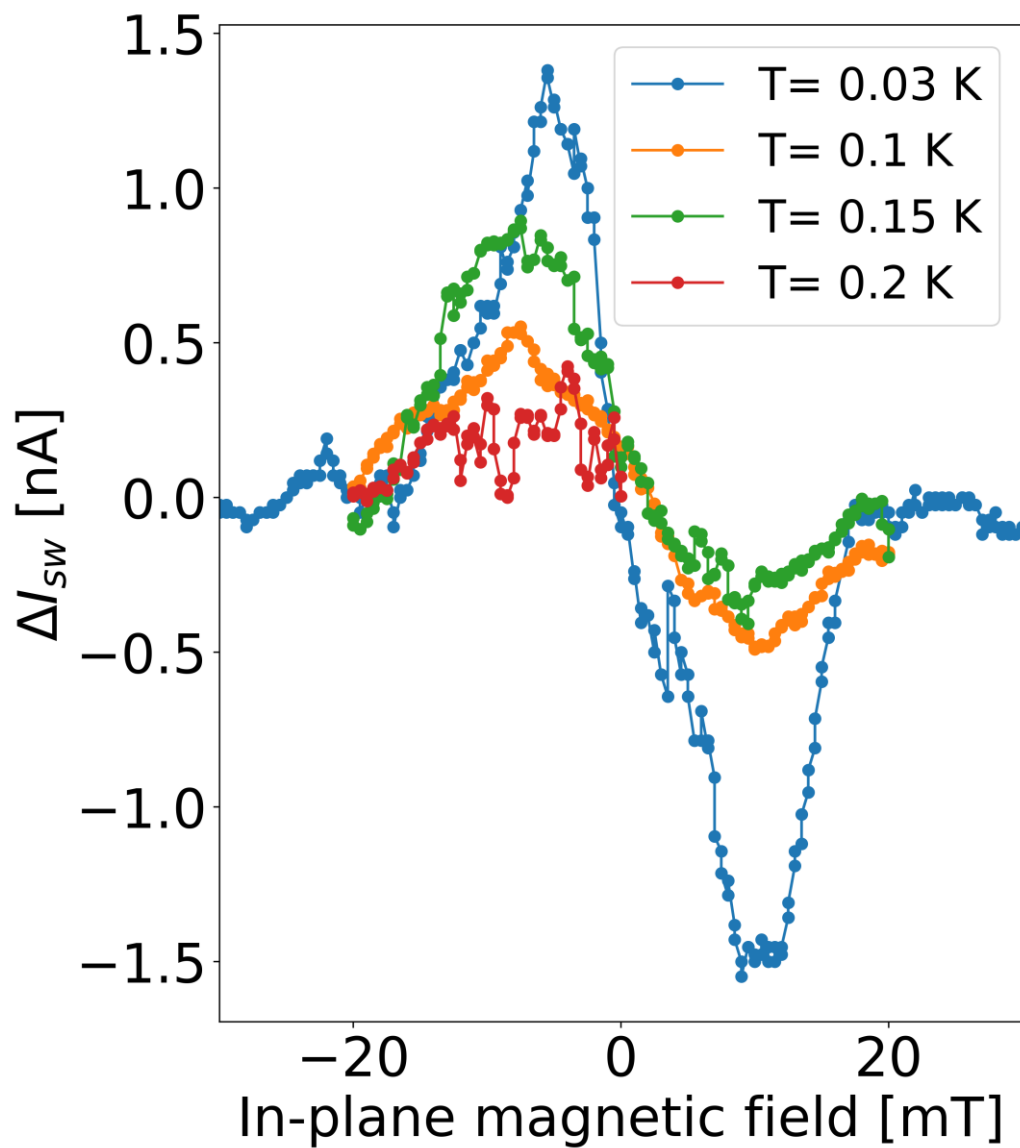
$$I = I_0 \sum_n c_n \sin(n\varphi)$$

➤ Anomalous phase shift

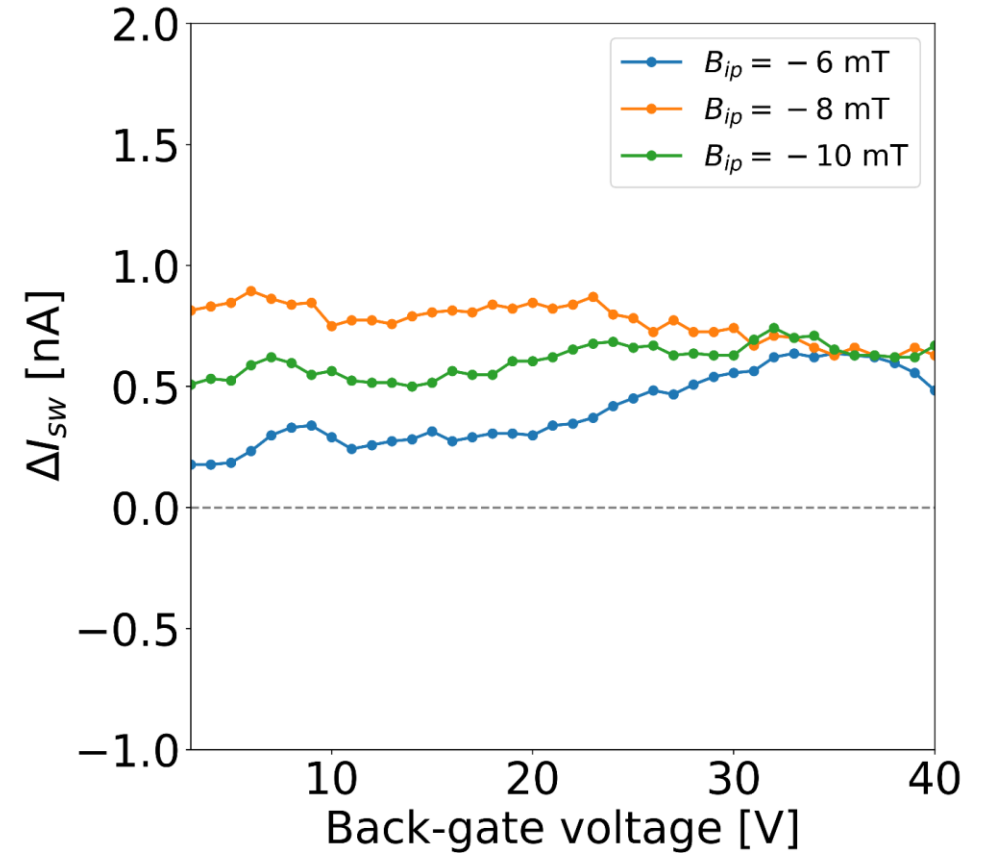
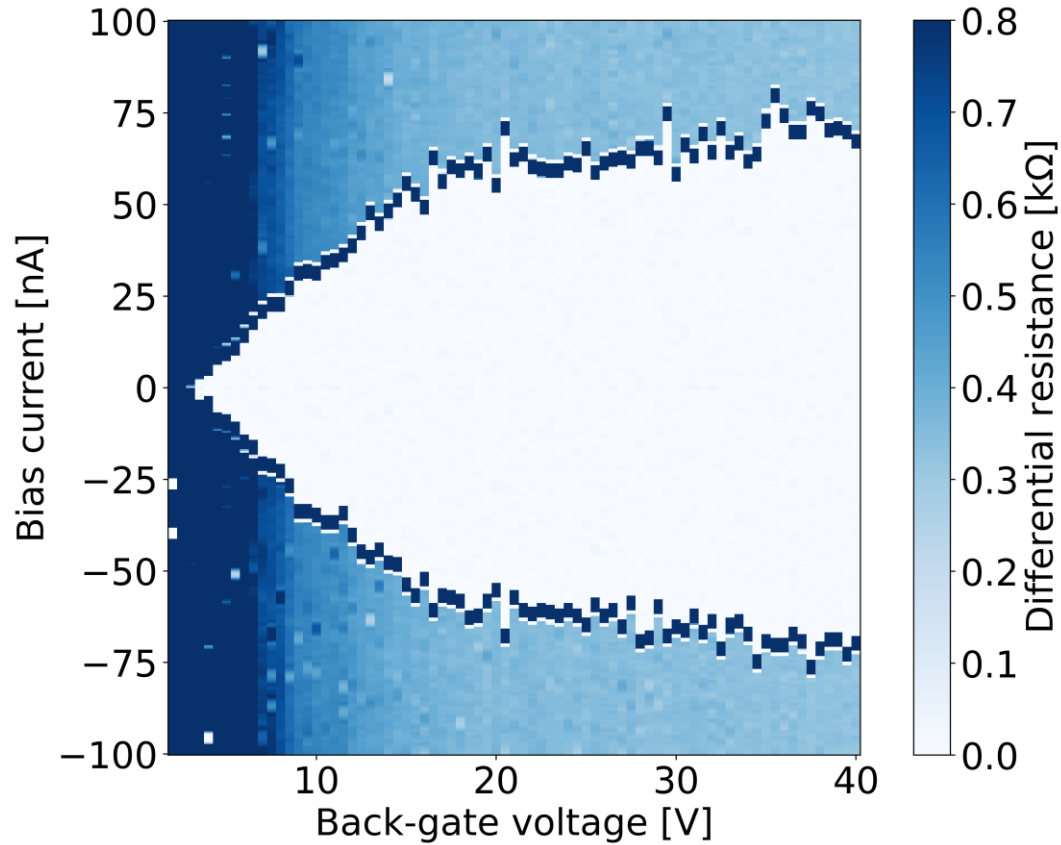
$$I = I_0 \sum_n c_n \sin(n\varphi + \varphi_{0,n})$$



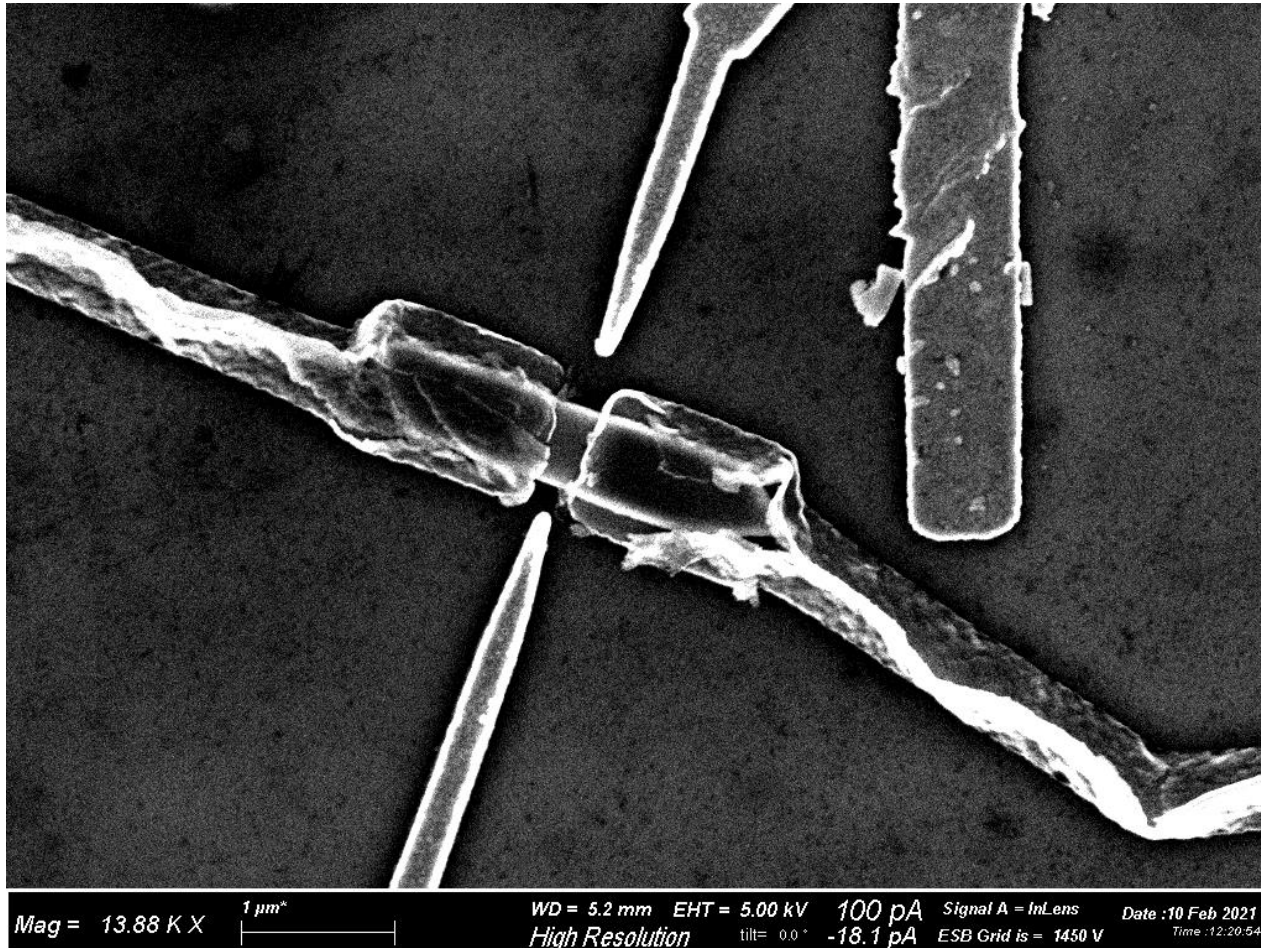
Dependence on the temperature



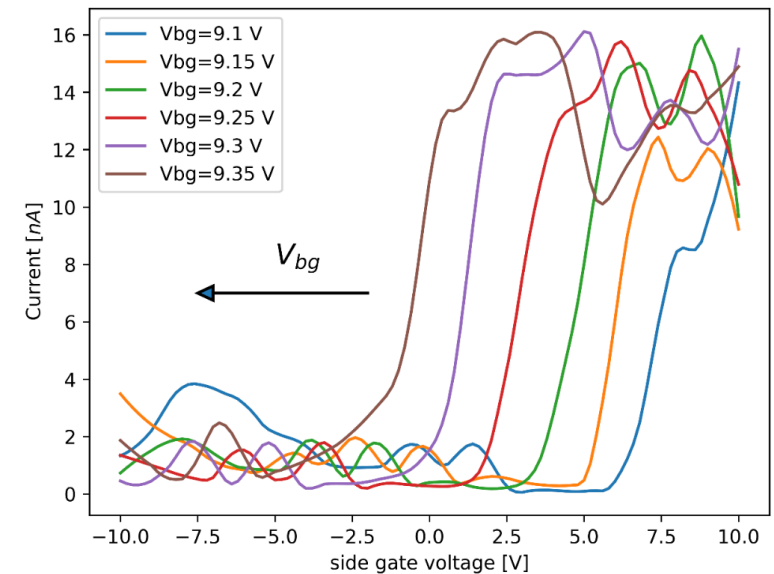
Effect of the back-gate



Outlook: gate-controlled SOI



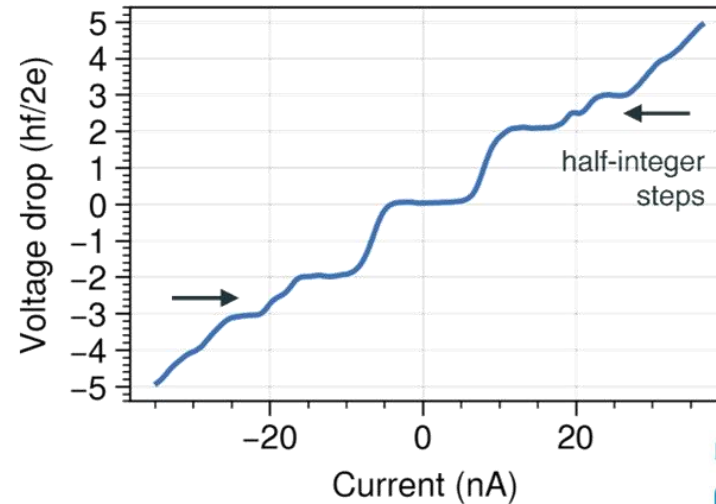
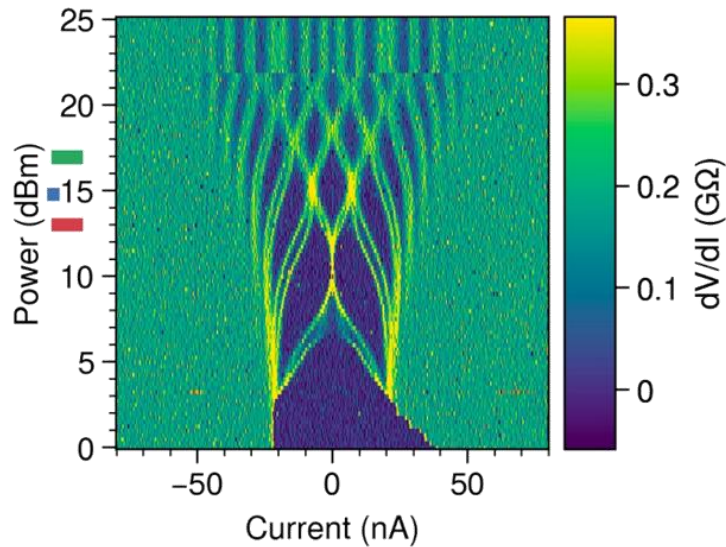
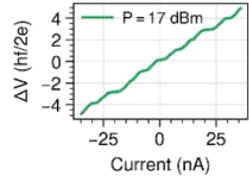
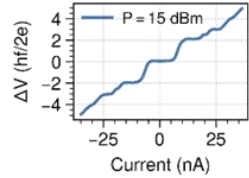
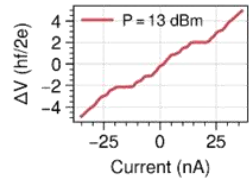
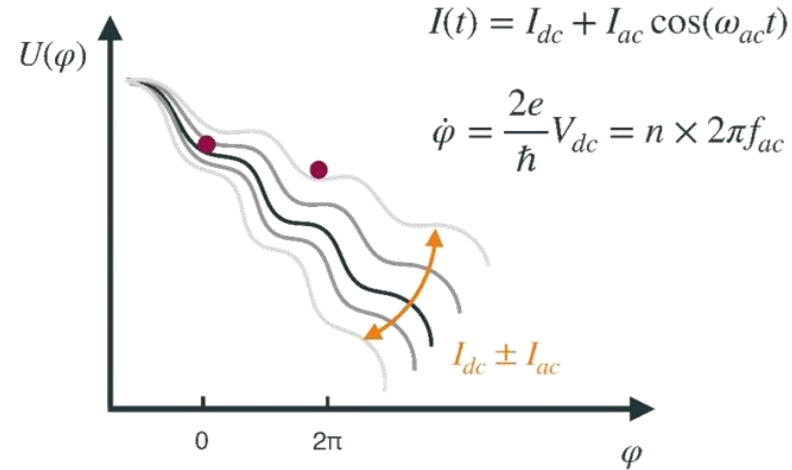
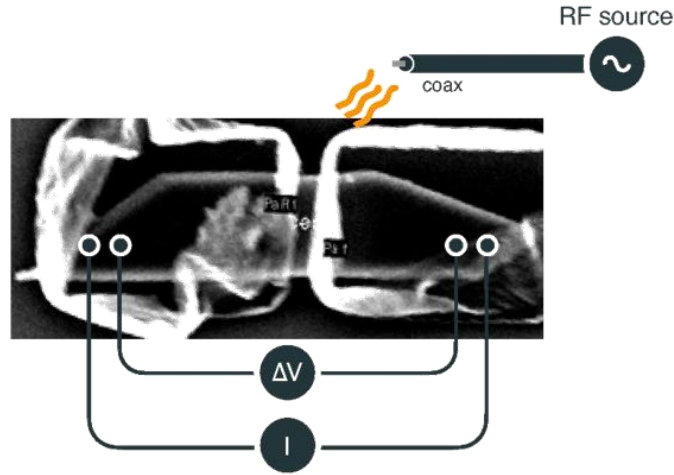
The idea: to tune the effective geometry and the SO coupling with side gates



Outlook: Shapiro steps

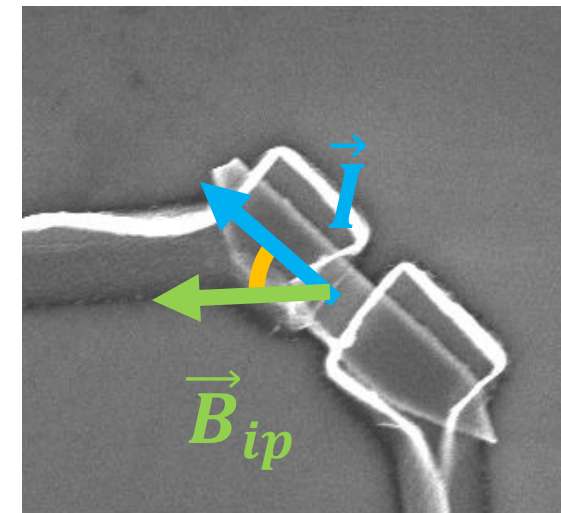
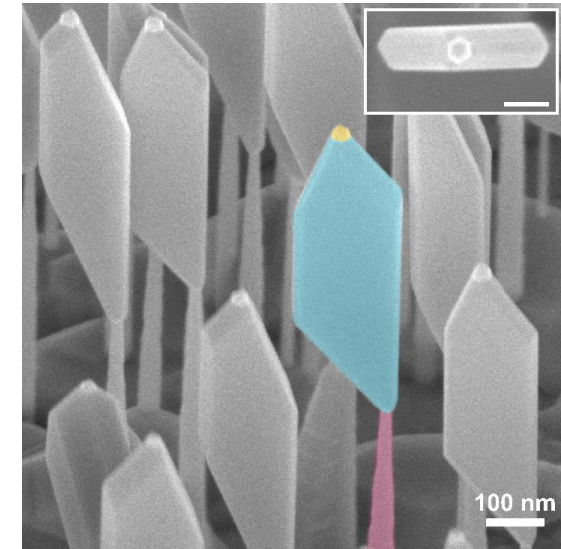


Andrea Iorio



Summary

- Free-standing InSb nanoflags via CBE:
 - defect-free quasi-2D ZB structures
 - high-mobility devices
- InSb nanoflag-based Josephson junction:
 - high-transparency of the interfaces
 - ballistic transport
 - gate-controlled supercurrent
- Josephson diode effect:
 - magnetic field-driven rectification
 - analysis of SOC in the system
 - evidence of finite-momentum superconductivity



People Involved

Growth activity



Valentina Zannier



Lucia Sorba

Devices



Sedighe Salimian

Theory

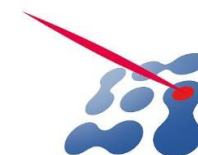


Matteo Carrega

Aknowledgments:



AndQC



SUPERTED

Transport measurements



Andrea Iorio



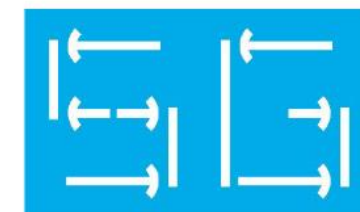
Elia Strambini



Francesco Giazotto



Stefan Heun



SUPER GATE

National Enterprise for nanoScience and nanoTechnology

NEST