

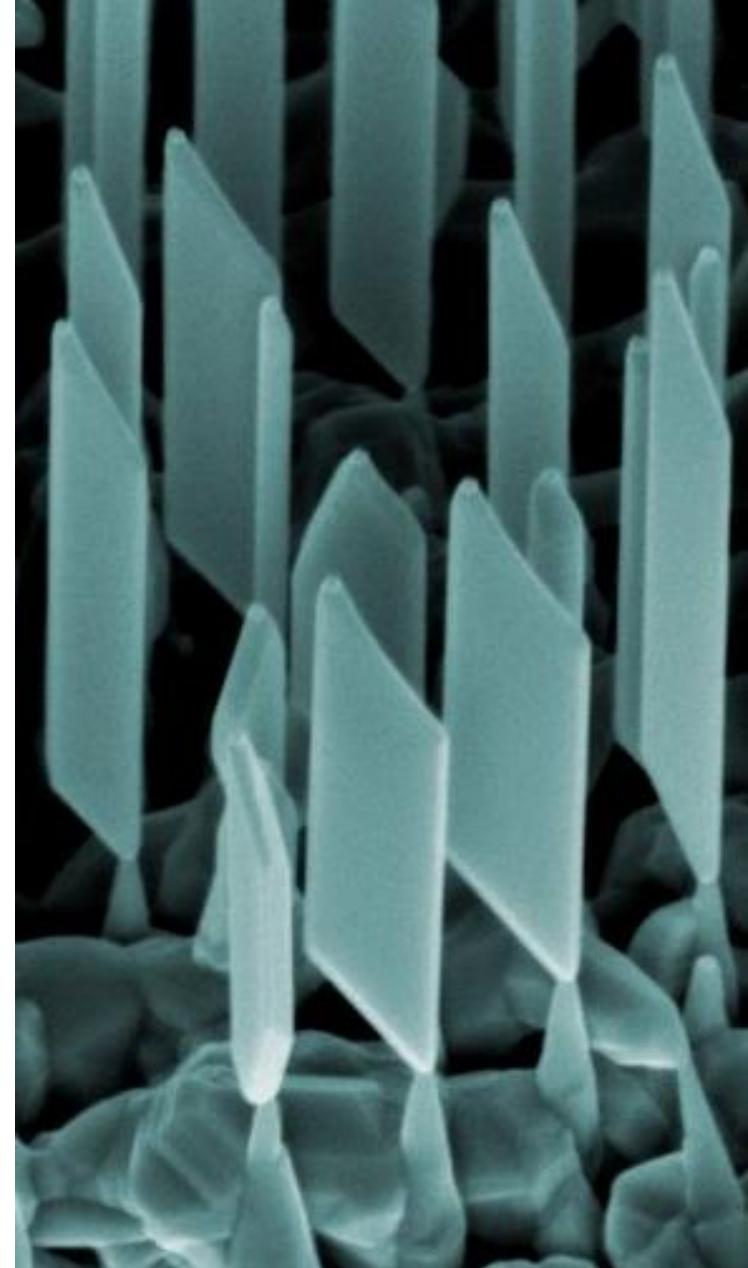


# Half-integer Shapiro Steps in Highly Transmissive InSb Nanoflag Josephson Junctions

Andrea Iorio<sup>1</sup>, Alessandro Crippa<sup>1</sup>, Bianca Turini<sup>1</sup>, Sedighe Salimian<sup>1</sup>,  
Matteo Carrega<sup>2</sup>, Luca Chirolli<sup>1</sup>, Valentina Zannier<sup>1</sup>, Lucia Sorba<sup>1</sup>,  
Elia Strambini<sup>1</sup>, Francesco Giazotto<sup>1</sup>, and **Stefan Heun**<sup>1</sup>

<sup>1</sup>*NEST, Istituto Nanoscienze-CNR and Scuola Normale Superiore, Pisa, Italy*

<sup>2</sup>*CNR-SPIN, Via Dodecaneso 33, 16146 Genoa, Italy*



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# InSb is appealing

Small bandgap       $E_g = 0.23 \text{ eV}$

Low effective mass     $m/m_o = 0.018$

Strong SOC             $E_{\text{SOC}} \sim 200 \mu\text{eV}$

# InSb is appealing but challenging to grow 2D



Lucia Sorba

Small bandgap

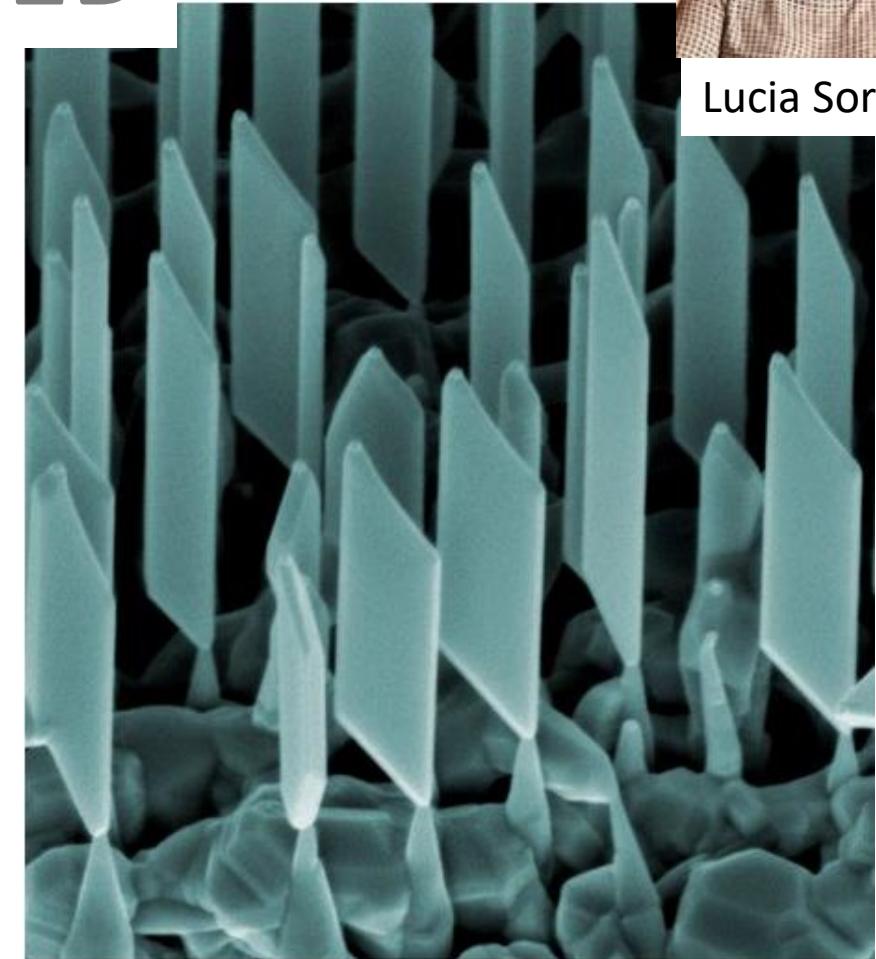
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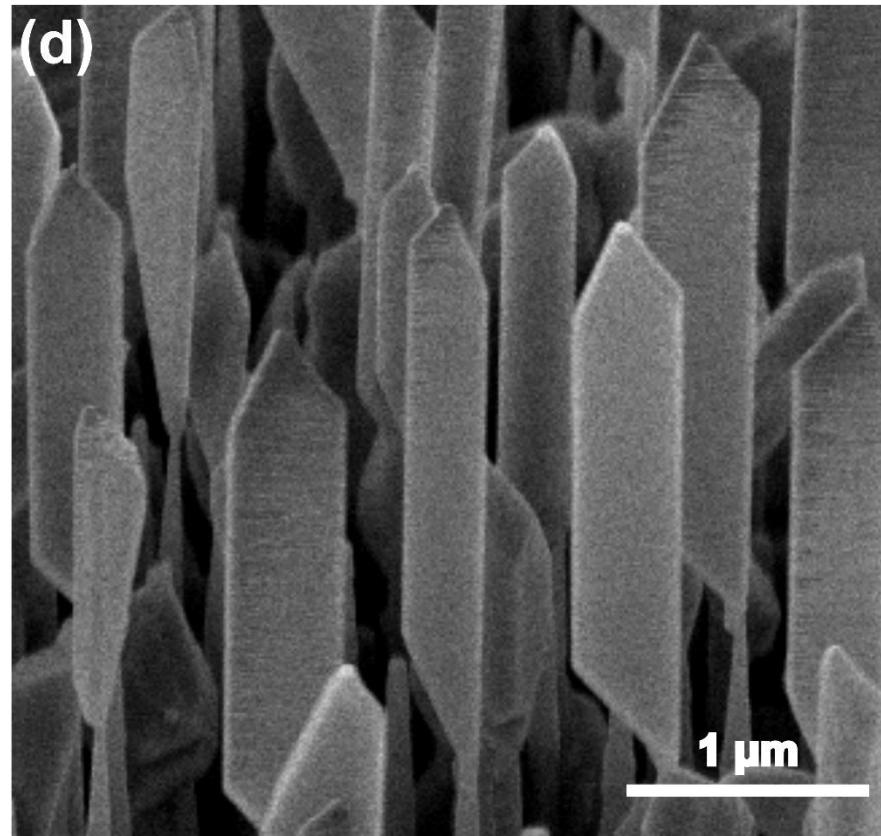
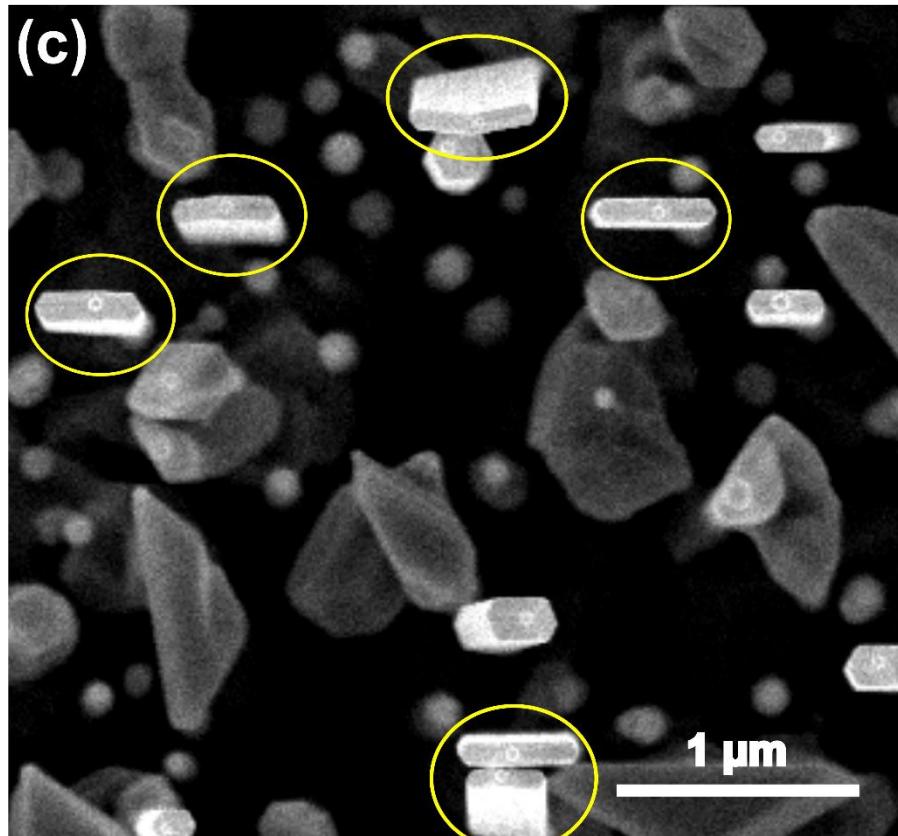
High-mobility 2D nanostructures



# Growth of InSb nanoflags by CBE



Isha Verma



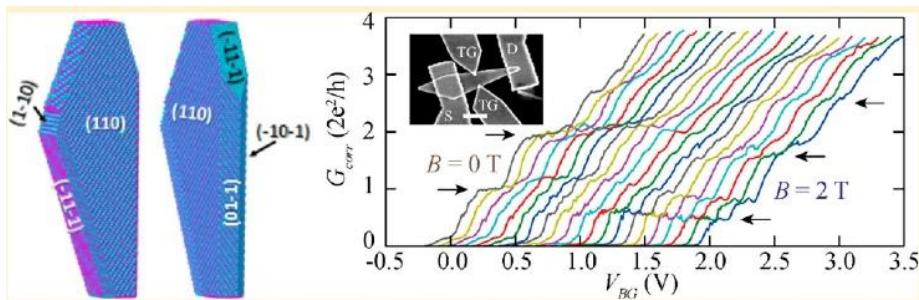
Defect-free InSb  
zinc blende  
lattice

**InSb nanoflags:**  
Length 2-3  $\mu$ m  
Width 500 nm  
Thickness 100 nm

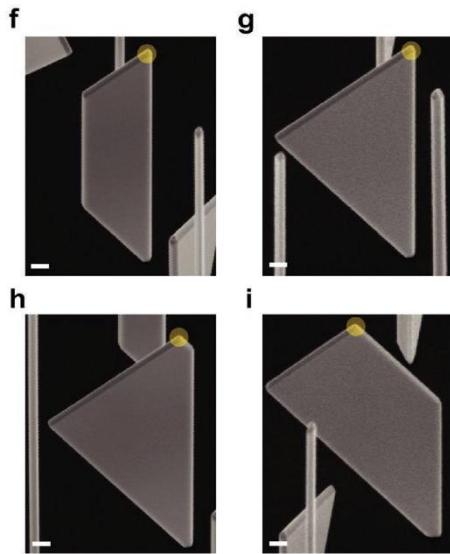
# A novel approach: 2D nanoflags (NFs)

## Twin-Induced InSb Nanosails: A Convenient High Mobility Quantum System

Maria de la Mata,<sup>†</sup> Renaud Leturcq,<sup>\*,‡,§</sup> Sébastien R. Plissard,<sup>||</sup> Chloé Rolland,<sup>‡</sup> César Magén,<sup>⊥</sup> Jordi Arbiol,<sup>\*,†,#</sup> and Philippe Caroff<sup>\*,‡,§,¶</sup>



*Nano Lett.* 16 (2016) 825



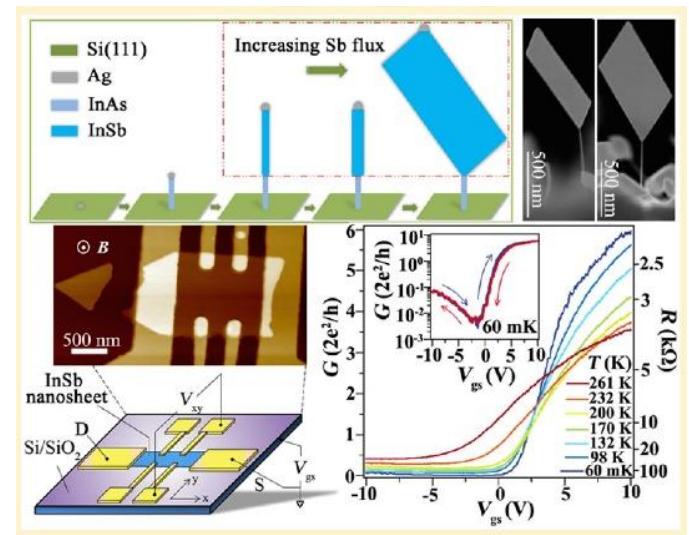
## Bottom-Up Grown 2D InSb Nanostructures

Sasa Gazibegovic,<sup>\*</sup> Ghada Badawy,<sup>\*</sup> Thijs L. J. Buckers, Philipp Leubner, Jie Shen, Folkert K. de Vries, Sebastian Koelling, Leo P. Kouwenhoven, Marcel A. Verheijen, and Erik P. A. M. Bakkers

*Adv. Mater.* 31 (2019) 1808181

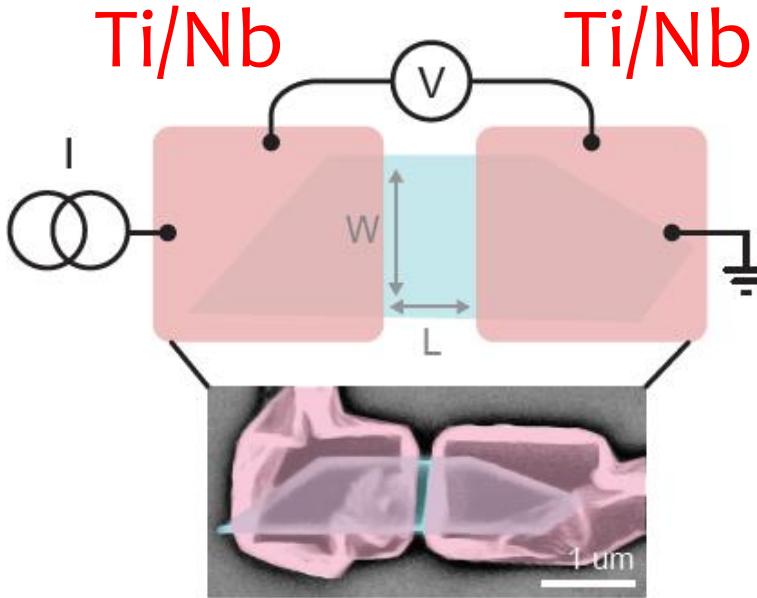
## Free-Standing Two-Dimensional Single-Crystalline InSb Nanosheets

D. Pan,<sup>†</sup> D. X. Fan,<sup>‡</sup> N. Kang,<sup>‡</sup> J. H. Zhi,<sup>‡</sup> X. Z. Yu,<sup>†</sup> H. Q. Xu,<sup>\*,‡</sup> and J. H. Zhao<sup>\*,†</sup>



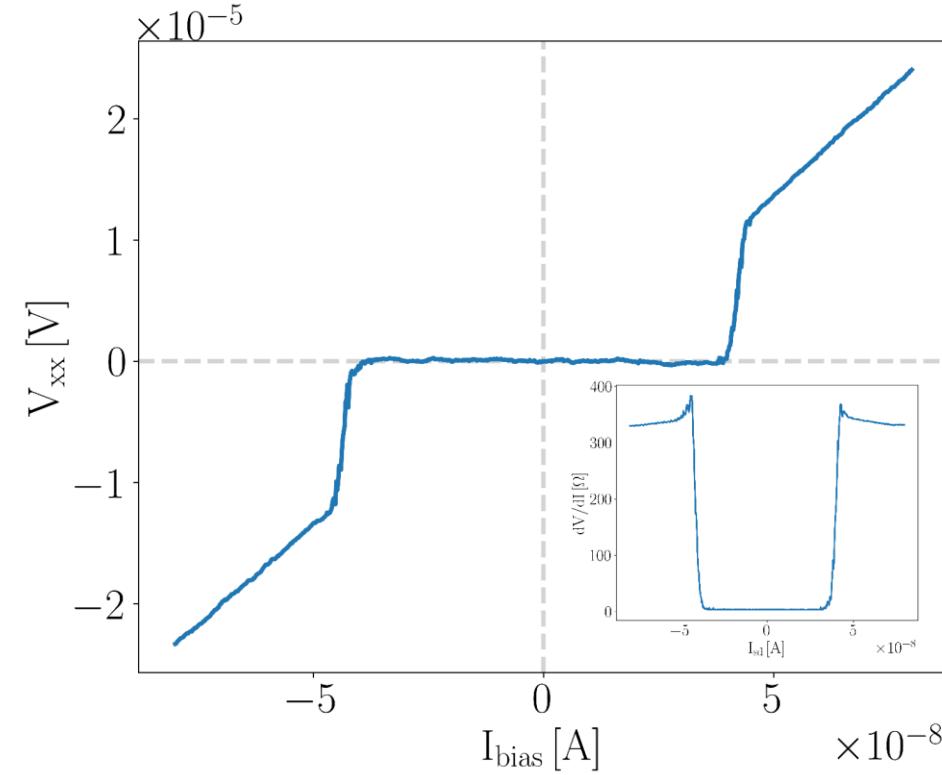
*Nano Lett.* 16 (2016) 834

# InSb nanoflag-based Josephson junctions



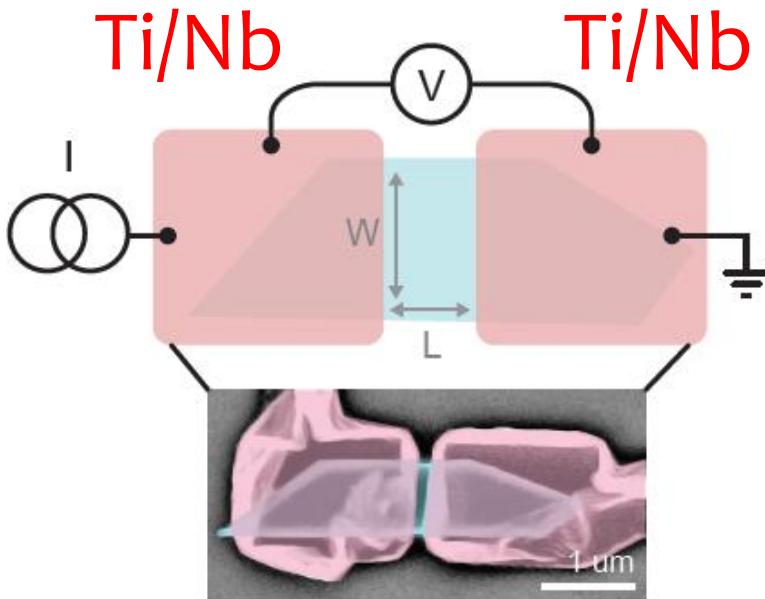
$\lambda_{\text{mfp}}$	500 nm
$L$	200 nm
$\xi_s$	750 nm

short-ballistic junction

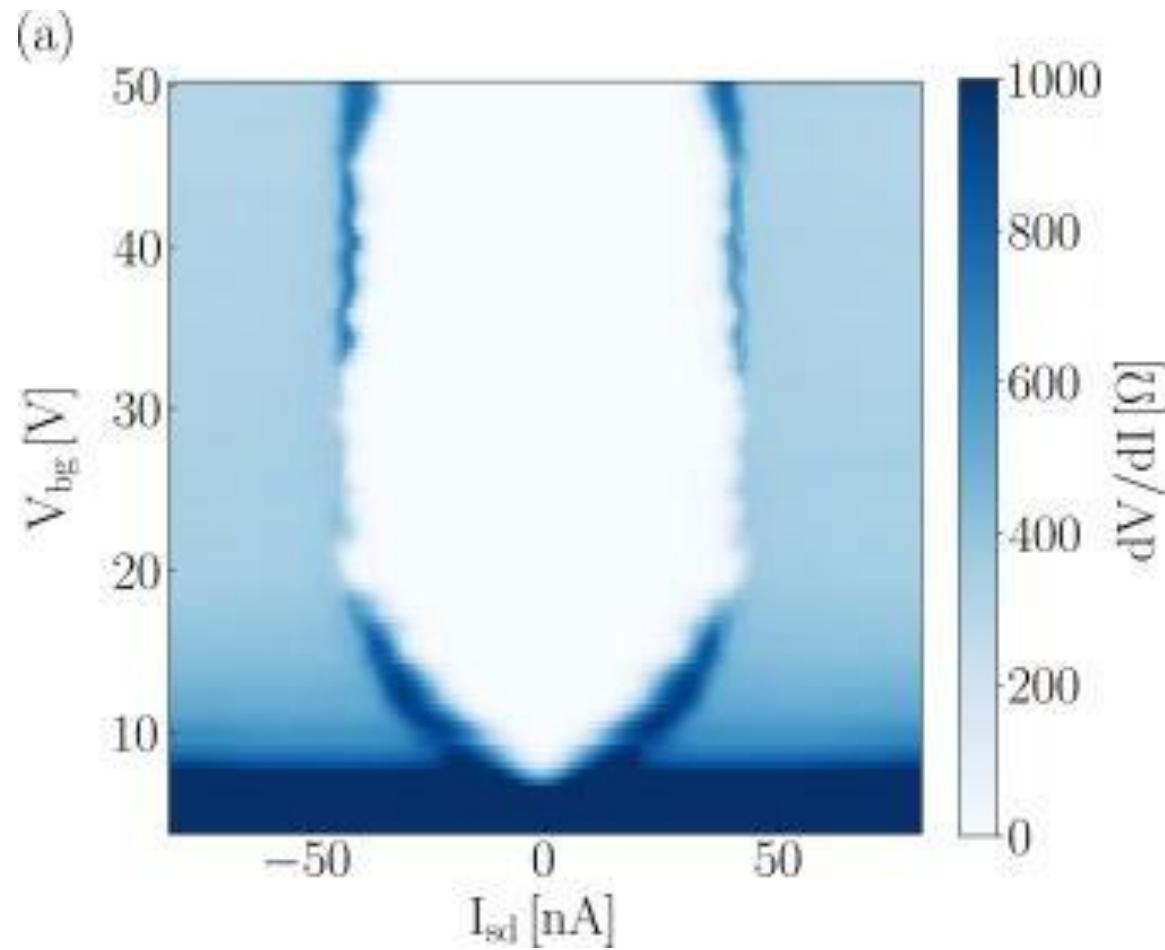


Sedighe Salimian

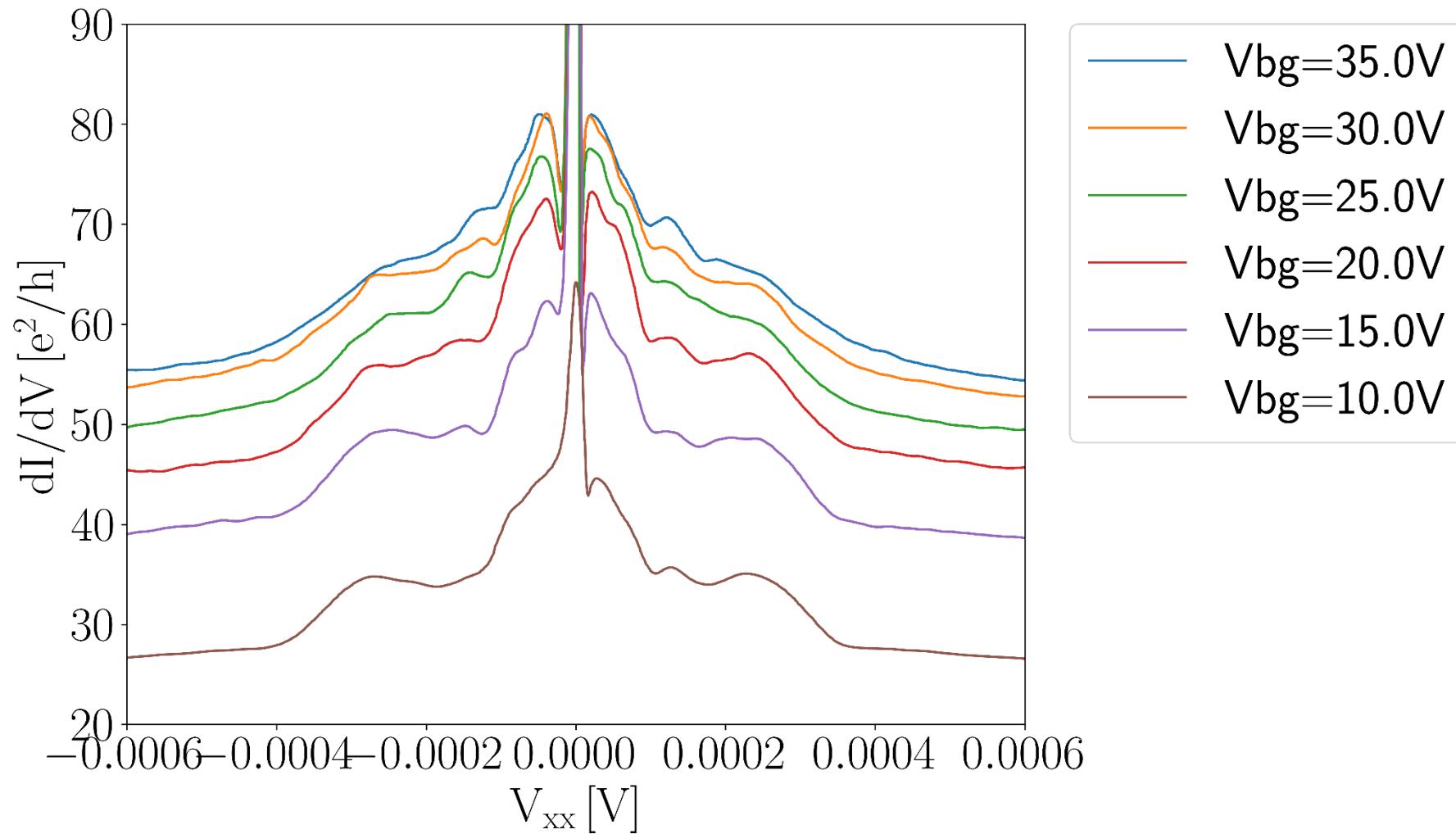
# Gate-tunable supercurrent



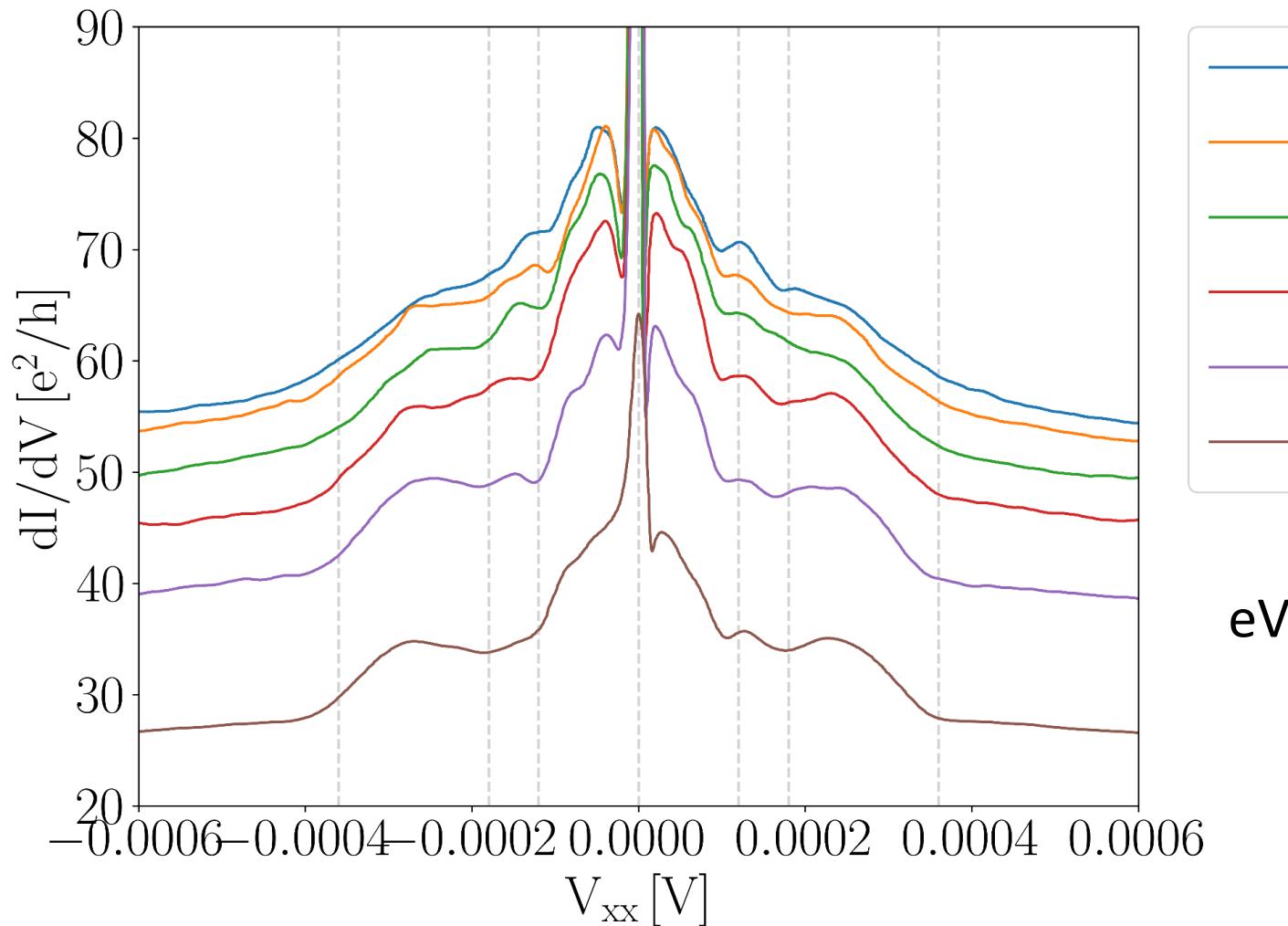
$\lambda_{\text{mfp}}$	500 nm
$L$	200 nm
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# Multiple Andreev Reflections



# Multiple Andreev Reflections



- $V_{bg}=35.0\text{V}$
- $V_{bg}=30.0\text{V}$
- $V_{bg}=25.0\text{V}$
- $V_{bg}=20.0\text{V}$
- $V_{bg}=15.0\text{V}$
- $V_{bg}=10.0\text{V}$



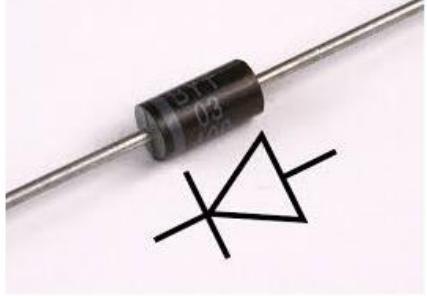
*Michał P. Nowak*

$$eV(n) = 2\Delta^*/n \quad (n=1, 2, 3 \dots)$$

$$\Delta^* \sim 160 \mu\text{eV}$$

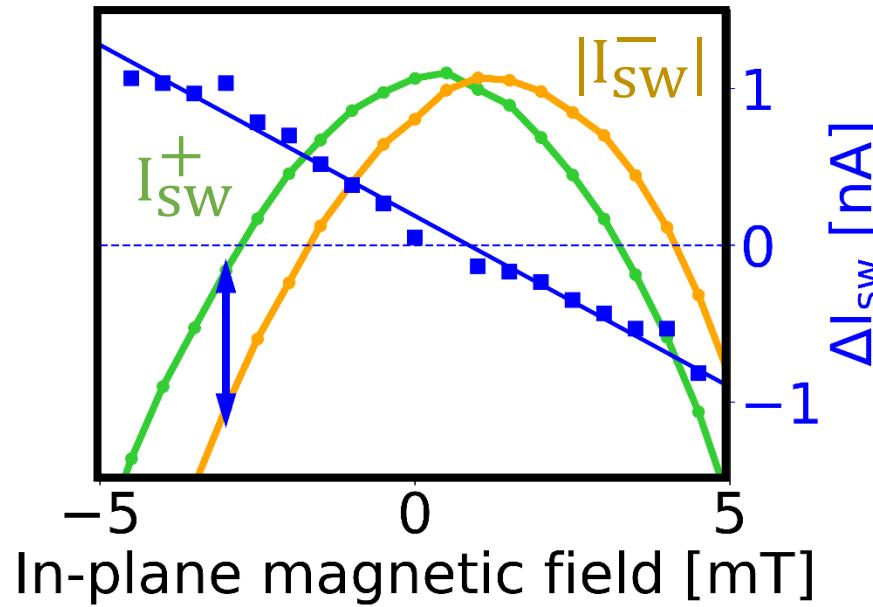
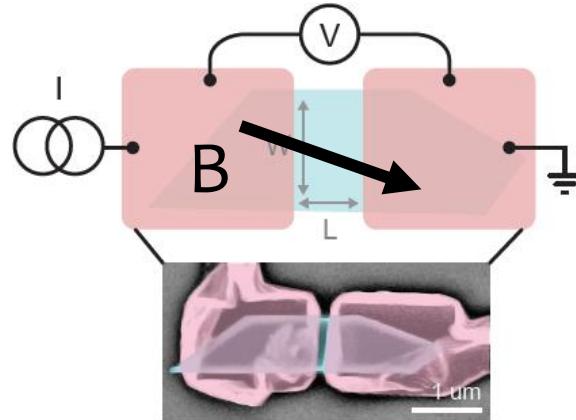
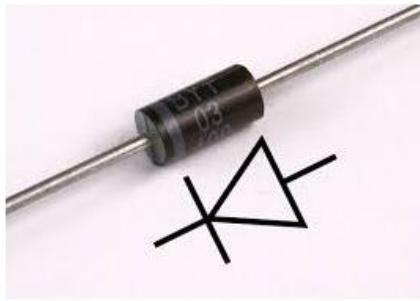
transparency  $\tau = 0.94$

# Josephson Diode Effect



Bianca Turini

# Josephson Diode Effect

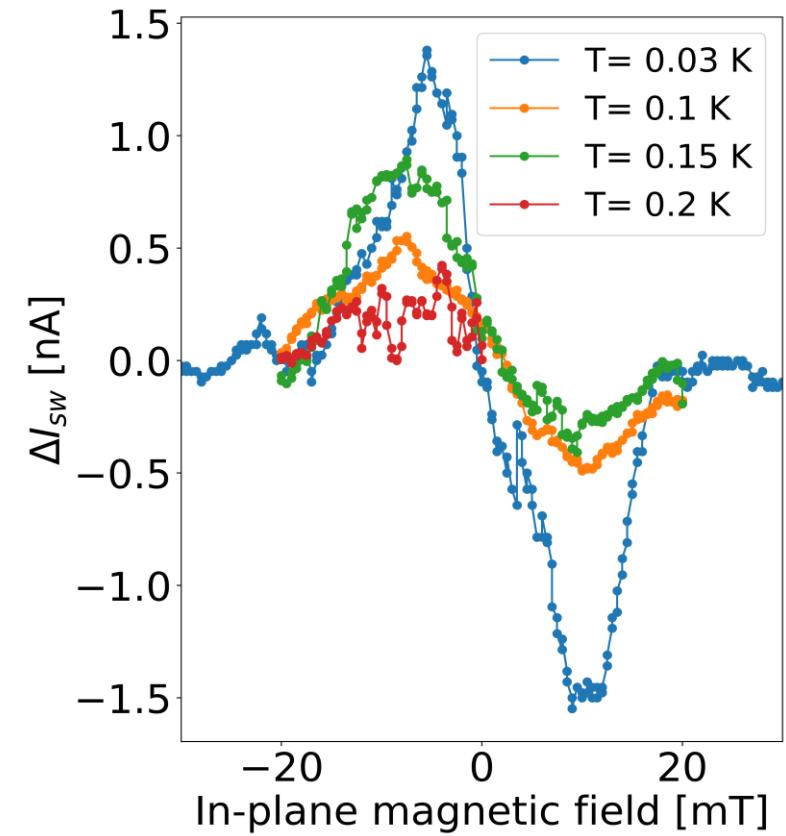
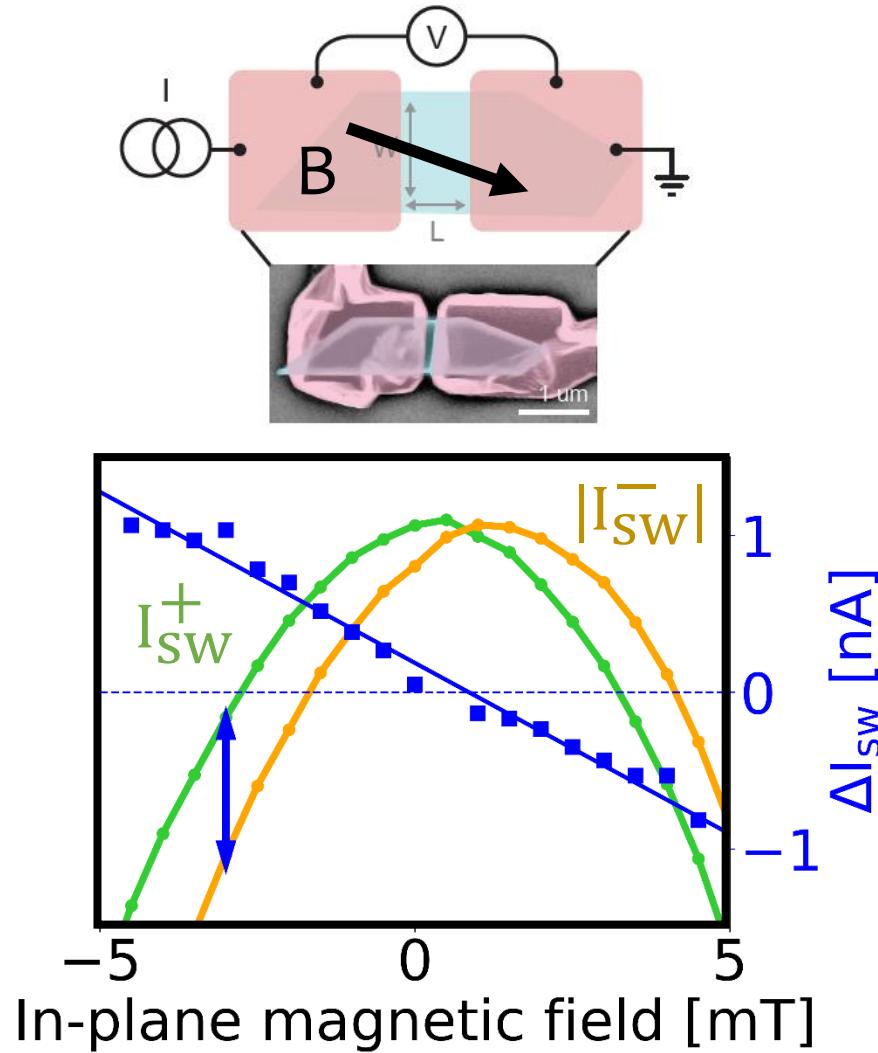
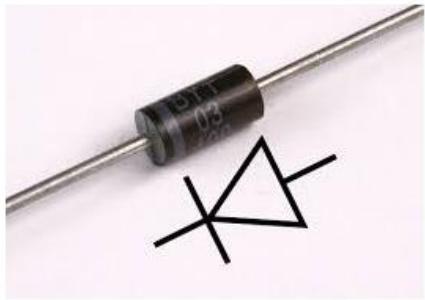


B. Turini et al., Nano Lett. 22, 8502 (2022).

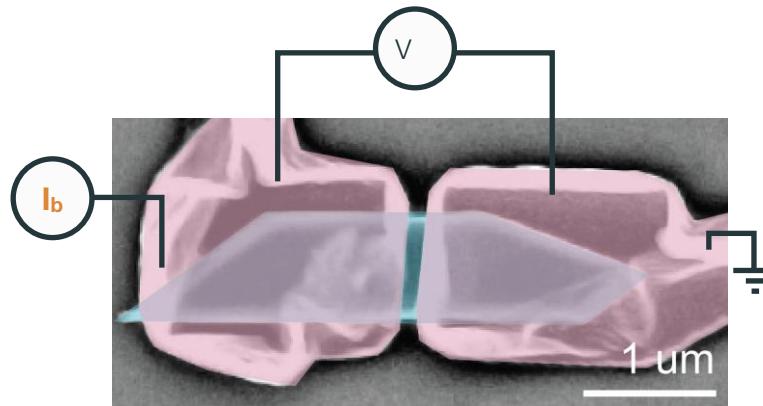


Bianca Turini

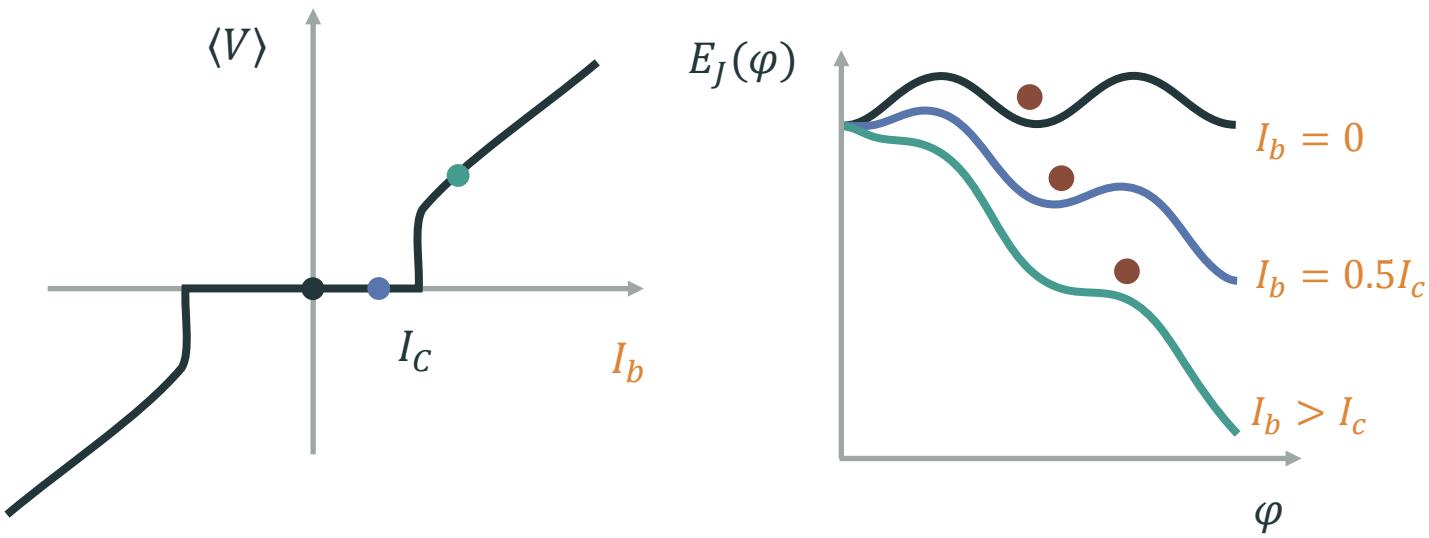
# Josephson Diode Effect



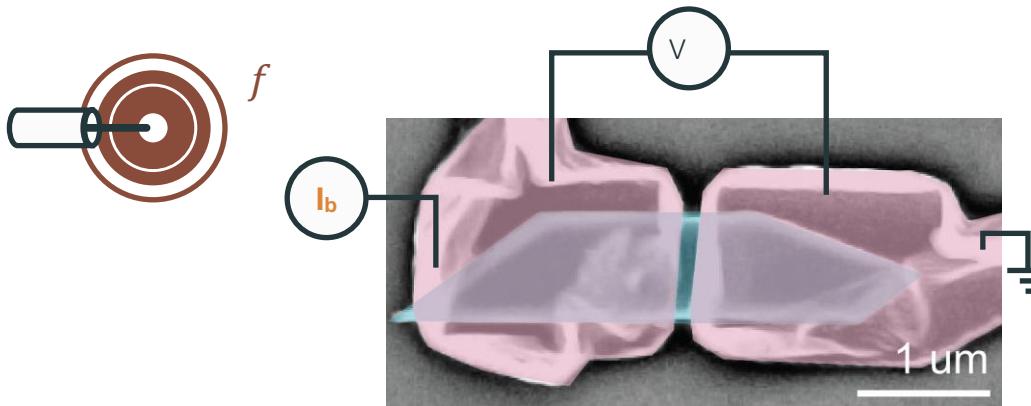
# Shapiro steps



$$V = \frac{\hbar}{2e} \dot{\varphi}$$



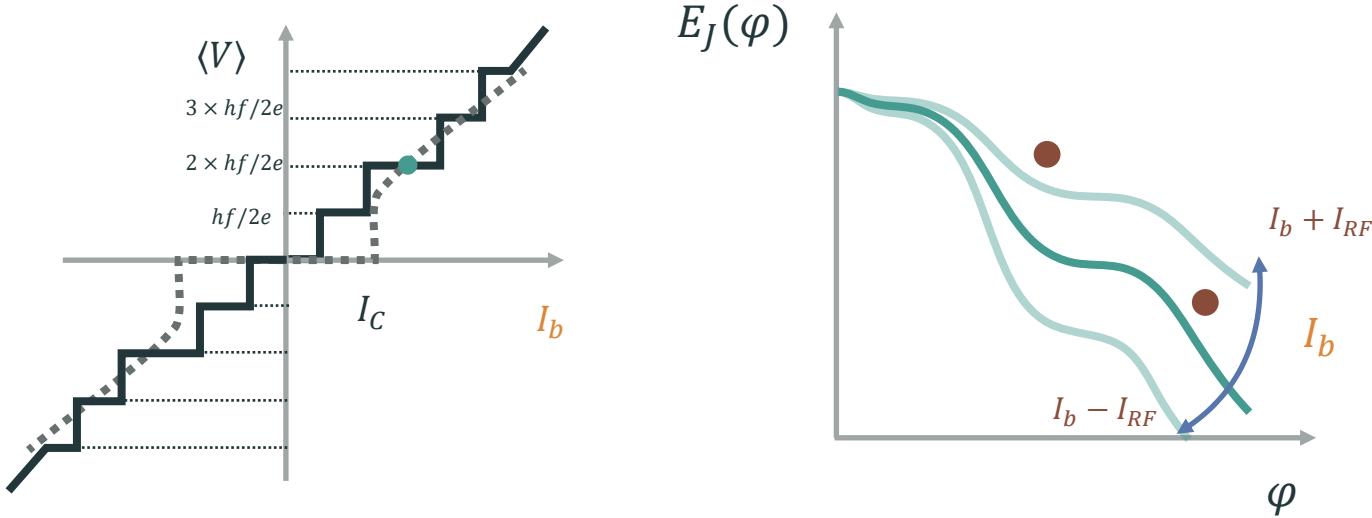
# Shapiro steps



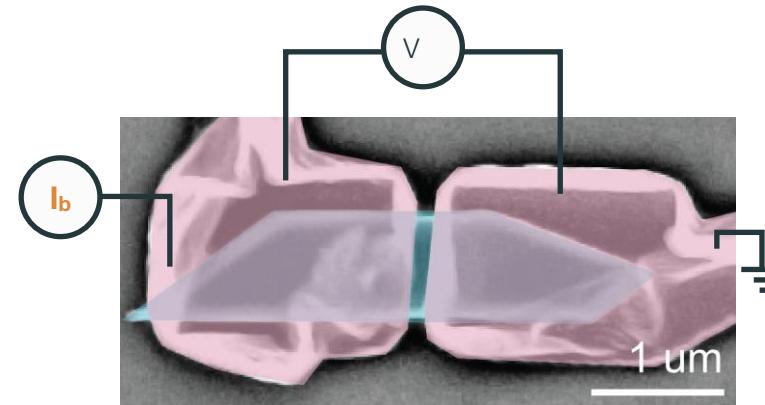
If particle rolls  $n$  minima in a period  $T = 2\pi/f$ , then  $\dot{\varphi} = 2\pi n f$

$$V = \frac{\hbar}{2e} \dot{\varphi}$$

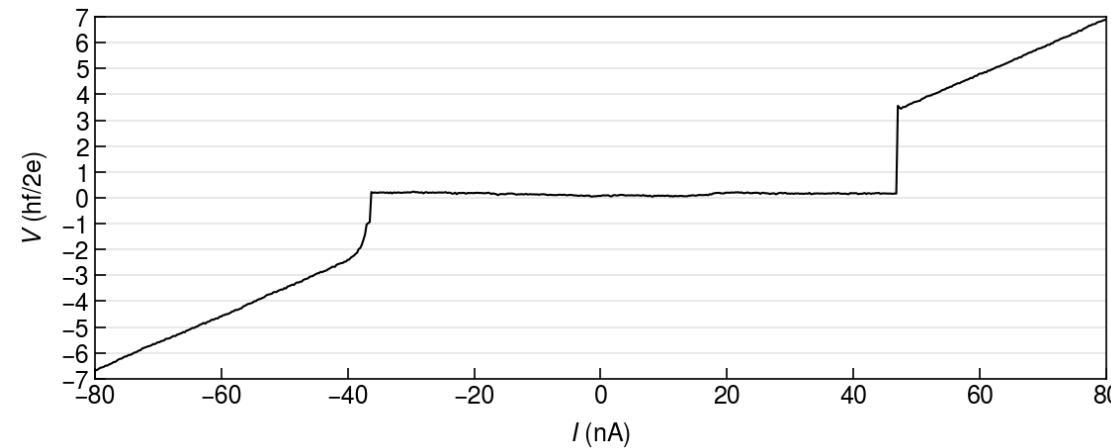
$$= \frac{hf}{2e} n$$



# Half-integer Shapiro steps



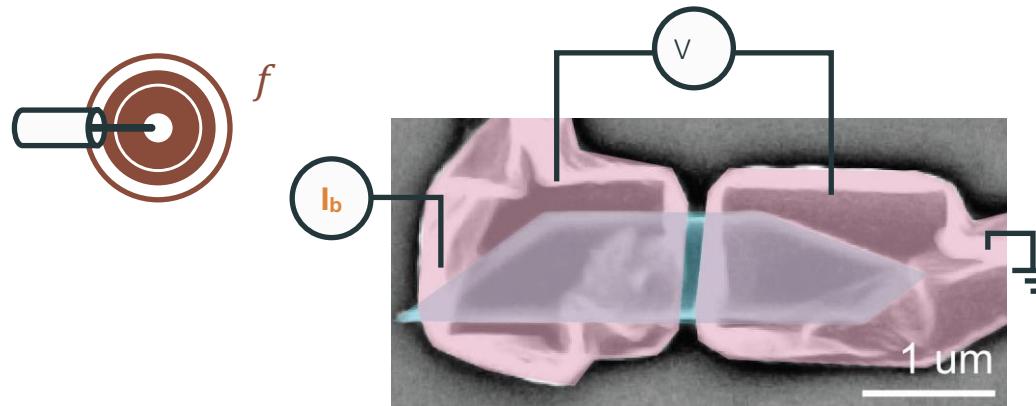
Andrea Iorio



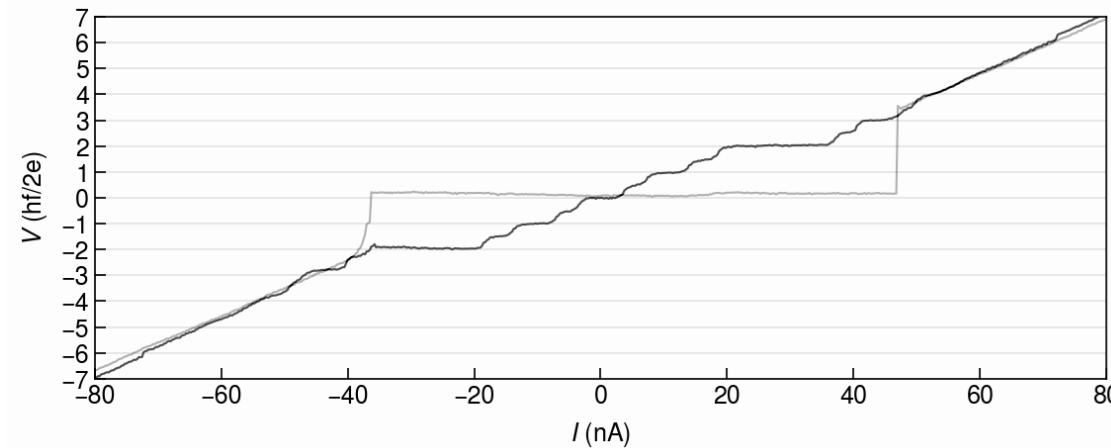
Shapiro steps – Quantized voltage plateaus  $V = \frac{hf}{2e} n$

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# Half-integer Shapiro steps



Andrea Iorio

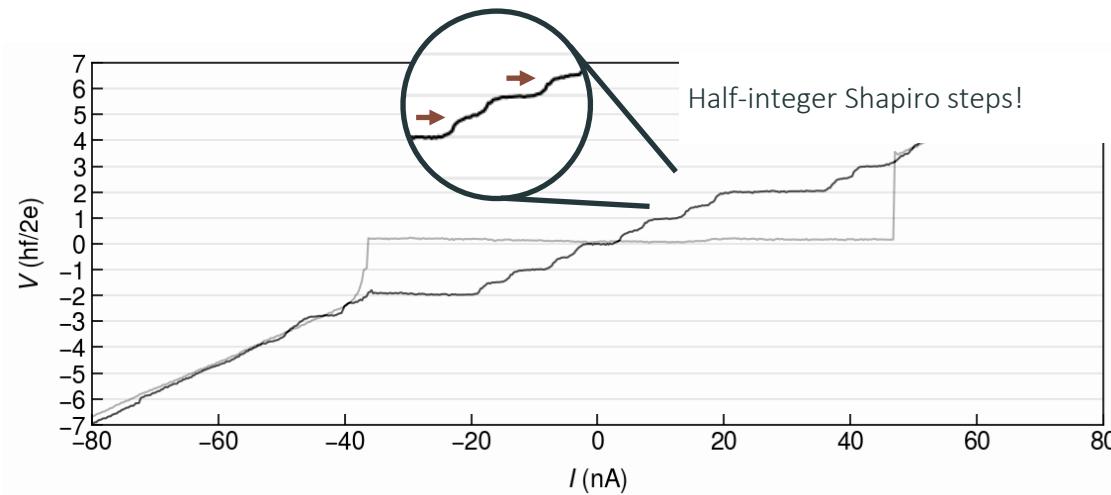
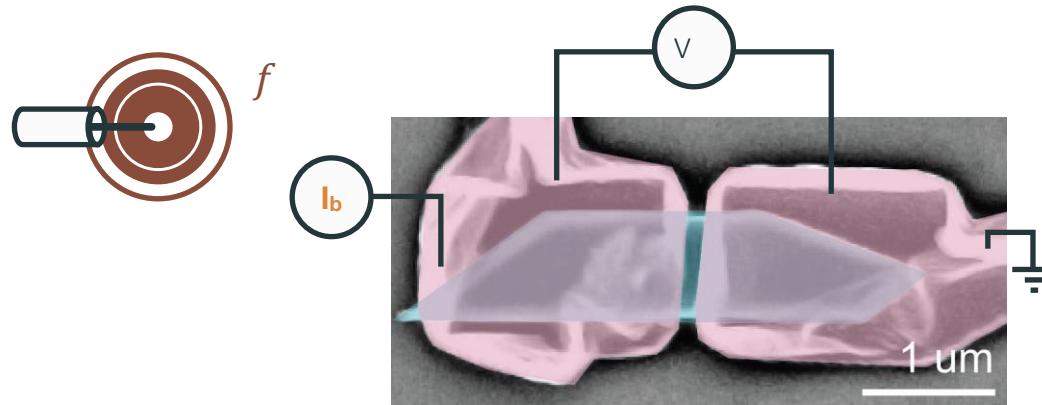


Shapiro steps – Quantized voltage plateaus  $V = \frac{hf}{2e} n$

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# Half-integer Shapiro steps

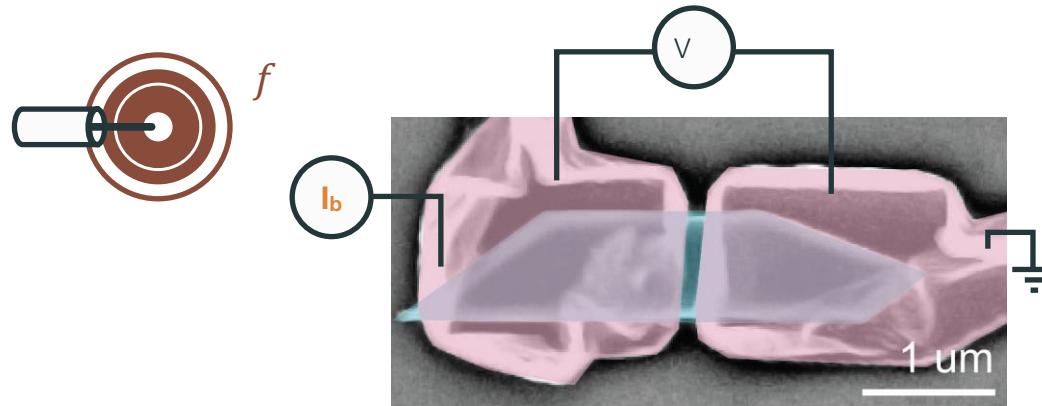


Shapiro steps – Quantized voltage plateaus  $V = \frac{hf}{2e} n$

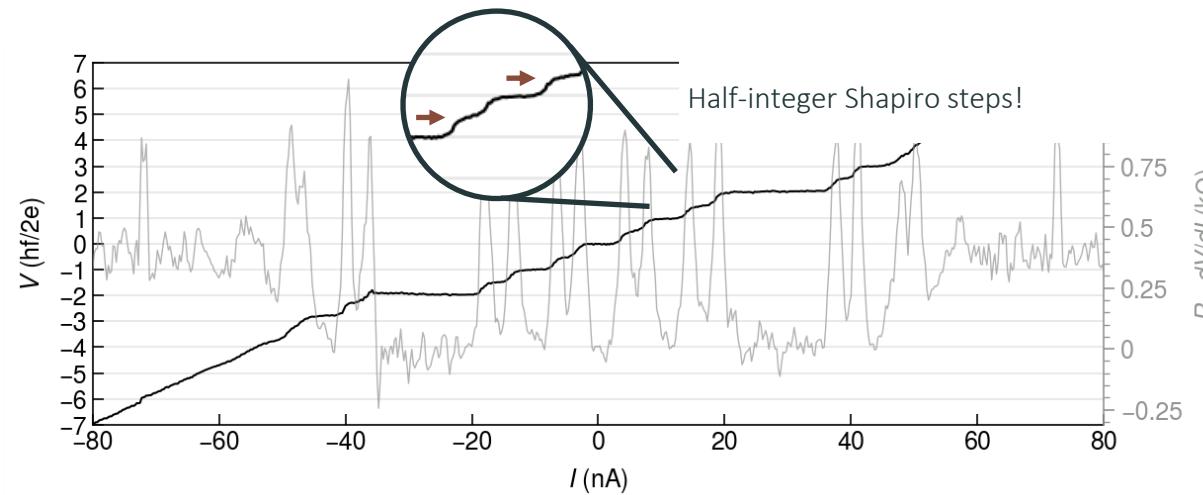


Andrea Iorio

# Half-integer Shapiro steps



Andrea Iorio

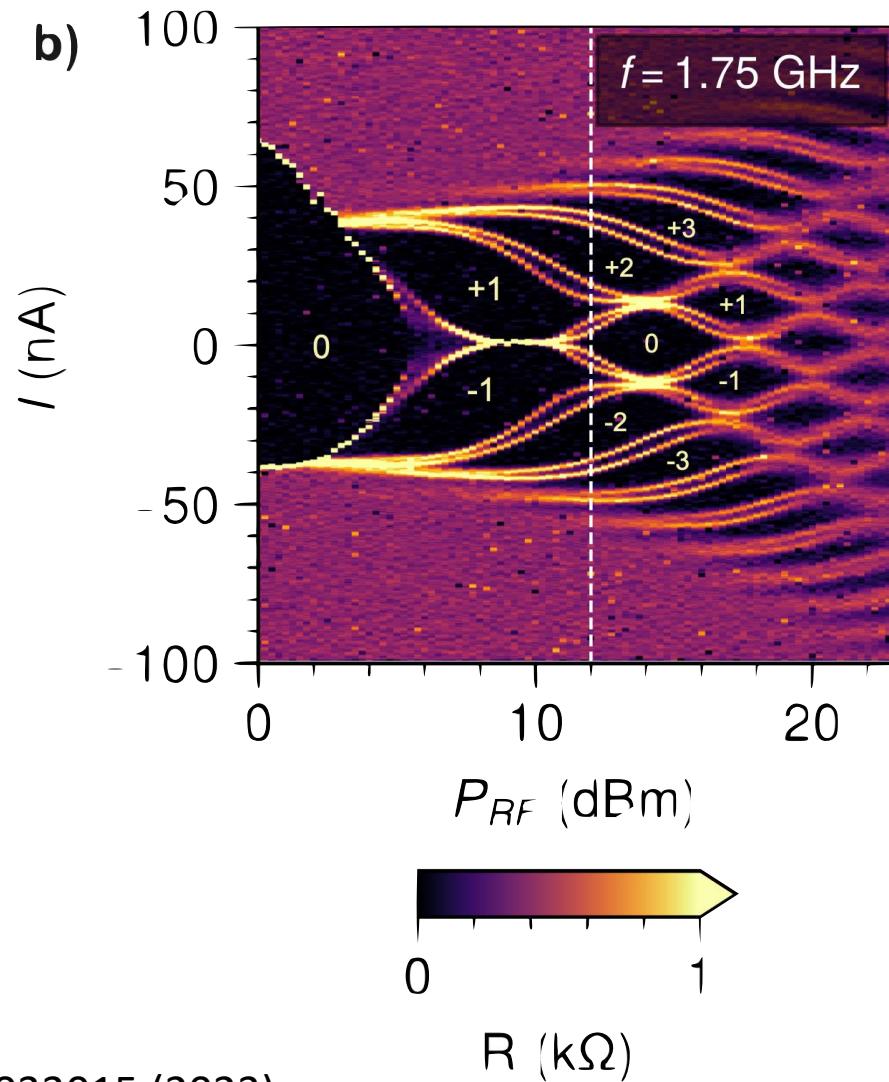


**Shapiro steps – Quantized voltage plateaus**  $V = \frac{hf}{2e} n$

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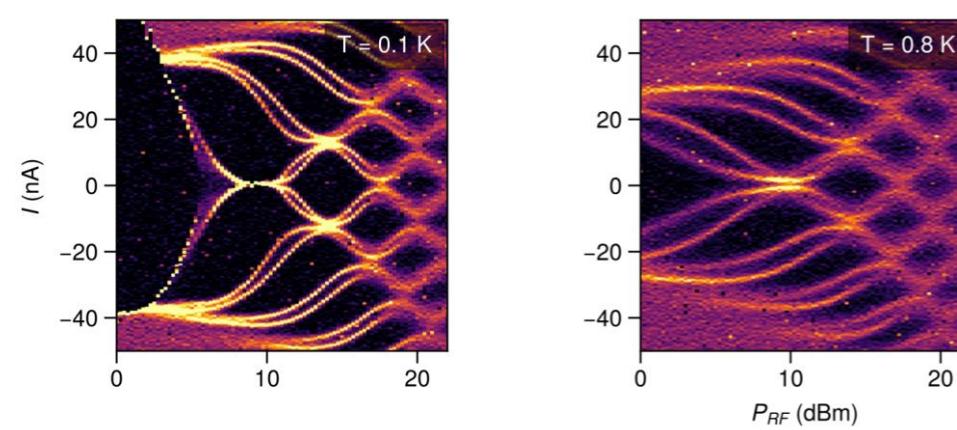
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# Half-integer Shapiro steps



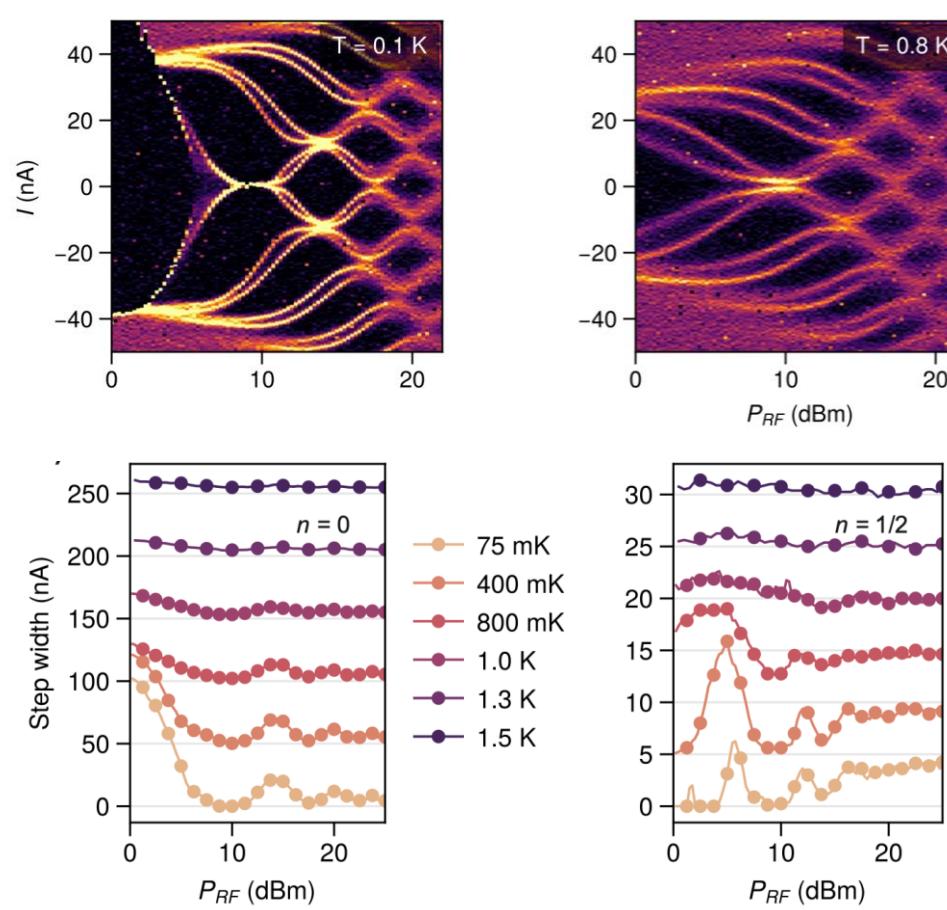
# Half-integer Shapiro steps

A non-monotonic temperature dependance



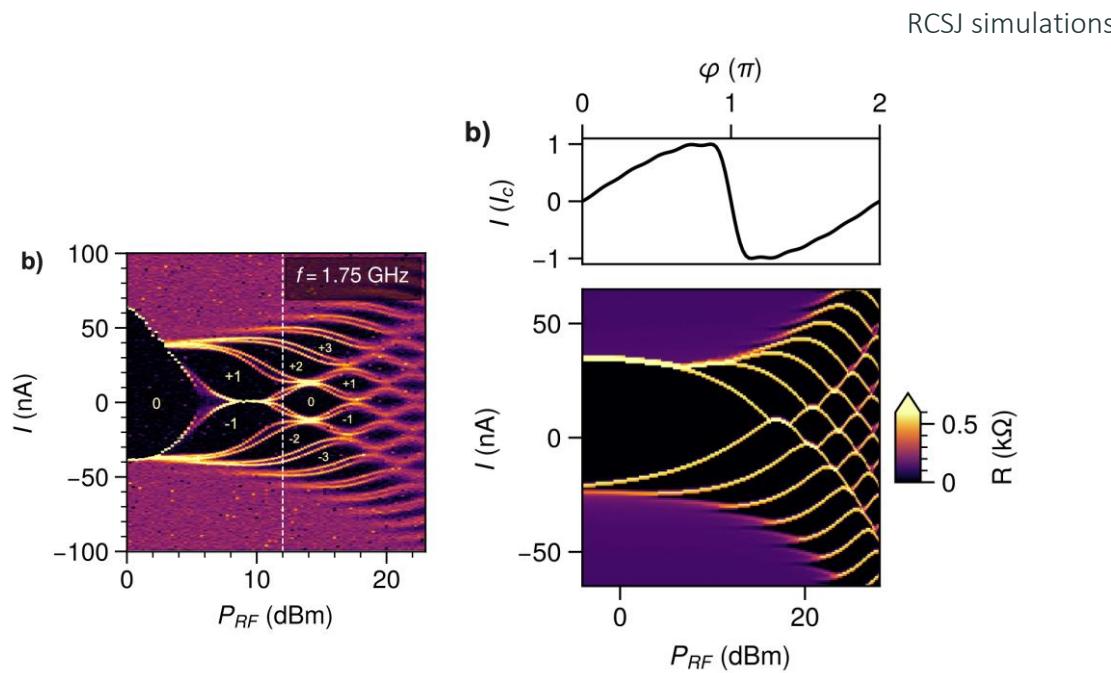
# Half-integer Shapiro steps

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# Half-integer Shapiro steps

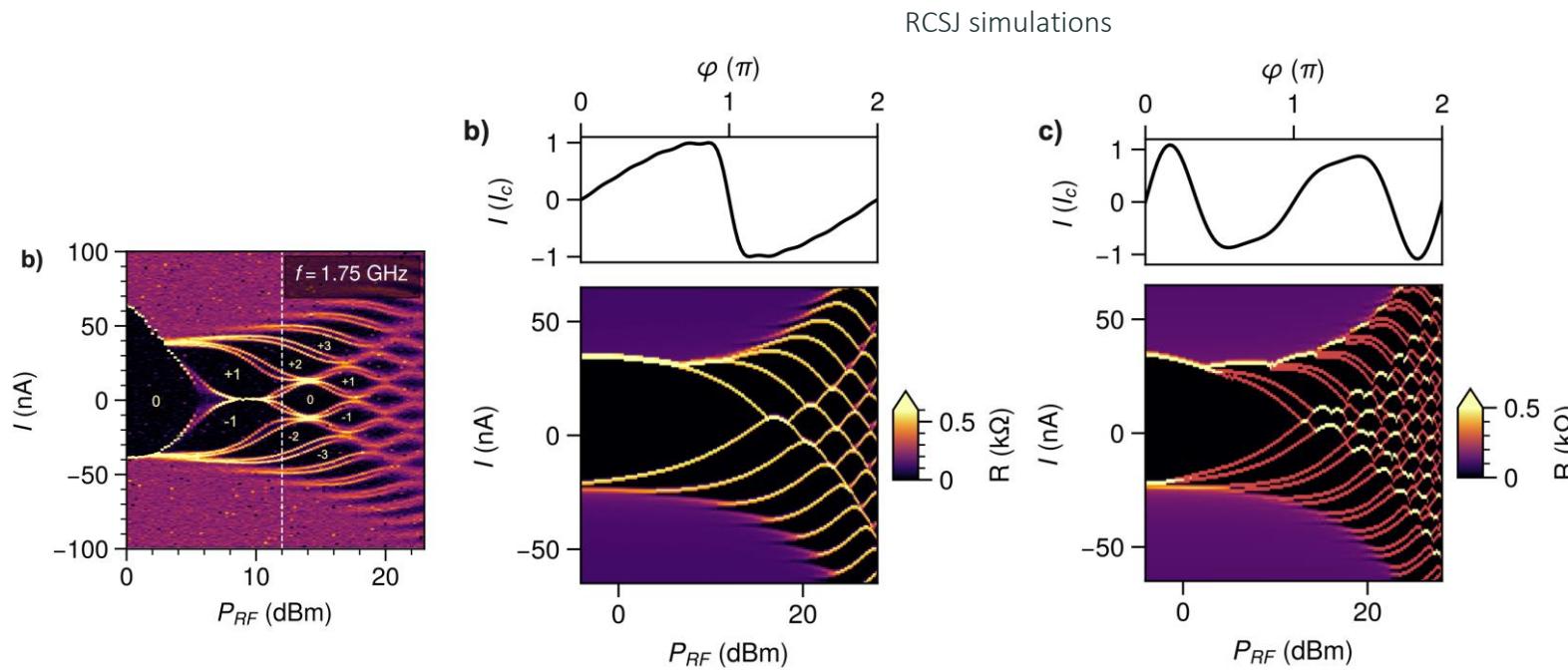
How to have half-integer steps?



# Half-integer Shapiro steps

How to have half-integer steps?

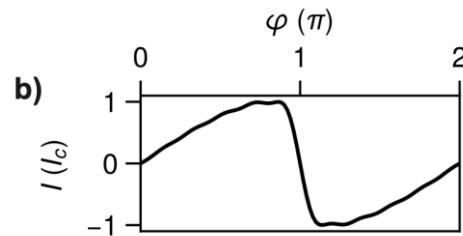
Need for a  $\sin(2\varphi)$  CPR



# Half-integer Shapiro steps

Potential mechanisms for  $\sin(2\varphi)$

Higher harmonic in the equilibrium CPR



✓ Common given explanation

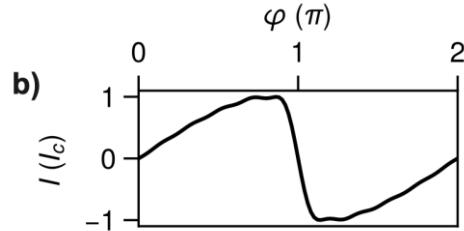
✗ Weaker half-steps

✗ Half-steps decrease with T

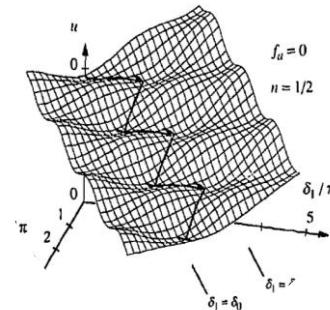
# Half-integer Shapiro steps

Potential mechanisms for  $\sin(2\varphi)$

Higher harmonic in the equilibrium CPR



SQUID-like



 Common given explanation

 Weaker half-steps

 Half-steps decrease with T

 Robust half-steps

 Different geometry

 B-field dependent

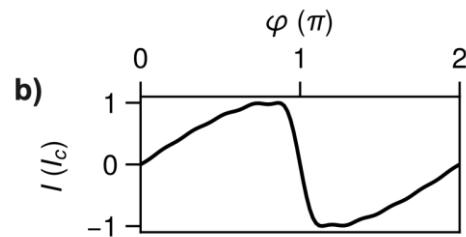
Physical basis for half-integral Shapiro steps in a dc SQUID. Physica C: Superconductivity 245.3-4 (1995)

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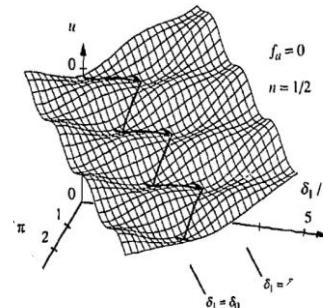
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Potential mechanisms for  $\sin(2\varphi)$

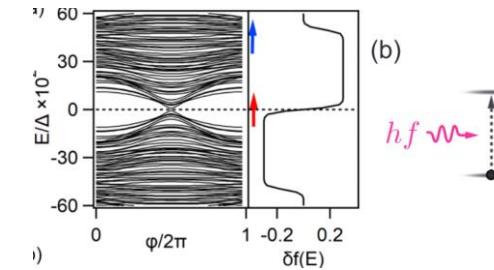
Higher harmonic in the equilibrium CPR



SQUID-like



Non-equilibrium excitations



 Common given explanation

 Weaker half-steps

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 Robust half-steps

 Different geometry

 B-field dependent

  $\sin(2\varphi)$  only when driving

 Half-steps non-monotonic in T

 Still some gaps with the theory

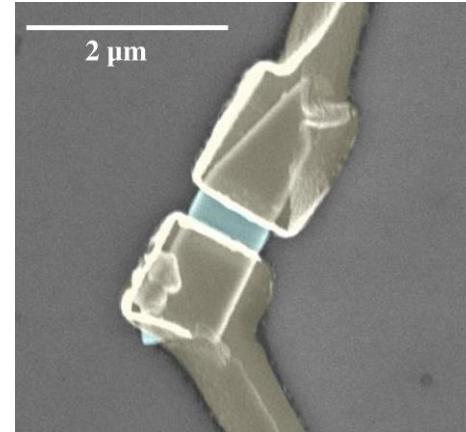
Physical basis for half-integral Shapiro steps in a dc SQUID. Physica C: Superconductivity 245.3-4 (1995)

Theory of microwave-assisted supercurrent in quantum point contacts. Physical review letters 105.11 (2010)  
Microwave photoassisted dissipation and supercurrent of a phase-biased graphene-superconductor ring. Physical Review Research 3.3 (2021)

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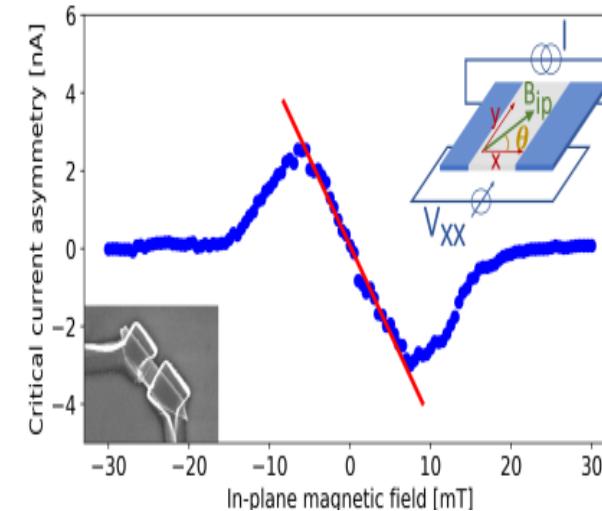
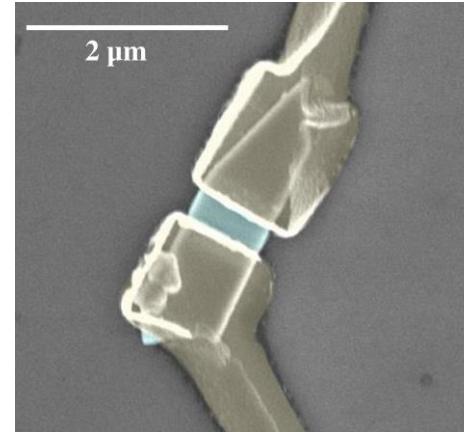
# Summary

- InSb nanoflag-based Josephson junctions:
  - High-transparency of the interfaces
  - Ballistic transport
  - Gate-controlled supercurrent
- Josephson diode effect:
  - First observation of the JDE in InSb
  - Magnetic field-driven rectification
  - Relevance of Rashba SOC in the system
- Half-integer Shapiro steps:
  - Shapiro steps are still an open-topic in SNS devices
  - Controllable manipulation of bound states excitations (Andreev qubits)



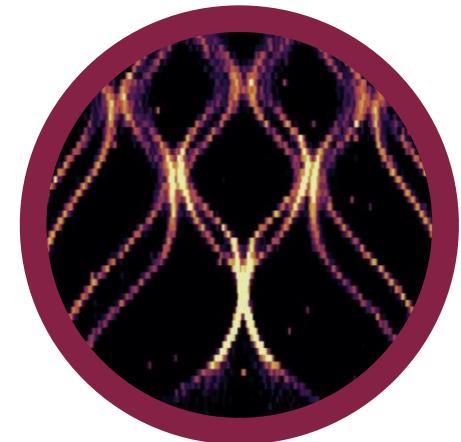
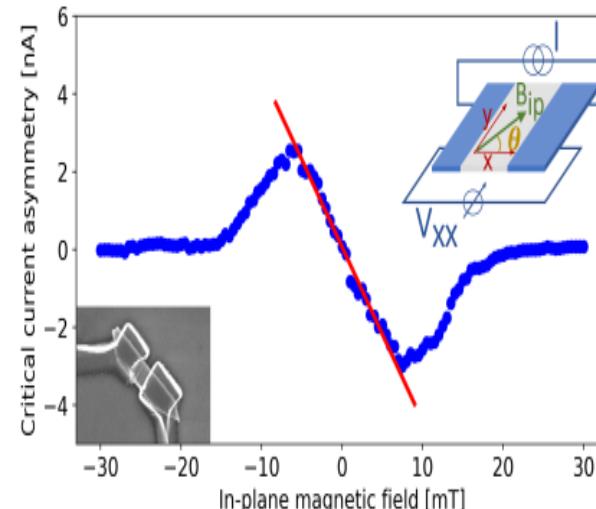
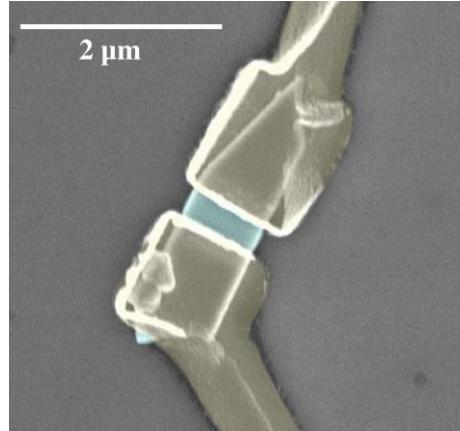
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# People Involved

## *Growth activity*



Isha Verma



Valentina  
Zannier



Lucia Sorba



Sedighe Salimian



Matteo Carrega  
Luca Chirolli

## *Devices*

## *Theory*

## Acknowledgments:



National Enterprise for nanoScience and nanoTechnology  
**NEST**

## *Transport*



Bianca Turini



Andrea Iorio



Alessandro  
Crippa



Elia Strambini



Francesco  
Giazotto



Fabio Beltram



Thank you for your attention!

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